

COMP 105 Assignment: Core ML

```
'a fun femptyEnv key = raise NotFound key val femptyEnv : 'a fenv = femptyEnv fun flookup (name, rho) = rho name fun
fbindVar (key,value,rho) = fn x => if (x = key) then value else rho x (***) PARTS 3 & 4: Environments & Polymorphism
***) fun isBound (key, rho) = (lookup(key,rho); true) handle NotFound key => false; fun extendEnv (keys, values, rho) =
pairfoldr bindVar rho (keys,values) (***) PART 3: blah fun fisBound (key, rho) = (flookup(key,rho); true) handle NotFound
key => false; fun fextendEnv (keys, values, rho) = pairfoldr fbindVar rho (keys,values) -->
```

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Due Monday, March 14, at 11:59 PM

The purpose of this assignment is to get you acclimated to programming in ML:

- On your own, you will write many small exercises.
- Possibly working with a partner, you will make a small change to the μ Scheme interpreter that is written in ML (in Chapter 6).

By the time you complete this assignment, you will be ready to tackle serious programming tasks in core ML.

Setup

For this assignment, you should use Moscow ML, which is in `/usr/sup/bin/mosml`.

You should make extensive use of the [Standard ML Basis Library](#). Jeff Ullman's text (Chapter 9) describes the 1997 basis, but today's compilers use the 2004 basis, which is a standard. You will find a few differences in I/O, arrays, and elsewhere; the most salient difference is in `TextIO.inputLine`.

The most convenient guide to the basis is the Moscow ML help system. type

```
- help "lib";
```

at the `mosml` interactive prompt.

If you use

```
ledit mosml -P full
```

as your interactive top-level loop, `mosml` will automatically load almost everything you might want from the standard basis.

Dire warnings

There are some functions and idioms that you must avoid. *Code violating any of these guidelines will earn No Credit.*

- When programming with lists, it is rarely necessary or desirable to use the `length` function. The entire assignment can and should be solved without using `length`.
- Use pattern matching to define functions. Do not use the functions `null`, `hd`, and `tl`.
- Do not define auxiliary functions at top level. Use `local` or `let` instead.
- Do not use `open`; if needed, use one-letter abbreviations for common structures.
- Do not use any imperative features unless the problem explicitly says it is OK.

Proper ML style

Ullman provides a gentle introduction to ML, and his book is especially good for programmers whose primary experience is in C-like languages. But, to put it politely, Ullman's ML is not idiomatic. *Much of what you see in Ullman should not be imitated.* Ramsey's textbook is a better guide to what ML should look like. We also direct you to these resources:

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- The [course supplement to Ullman](#)
- The voluminous [Style Guide for Standard ML Programmers](#)

Individual Problems (90%)

Working on your own, please solve the exercises **A, B, C, D, E, F, G, H, I, J, and K** described below.

Higher-order programming

- A. The function `compound` is somewhat like `fold`, but it works on binary operators.
1. Define the function

```
val compound : ('a * 'a -> 'a) -> int -> 'a -> 'a
```

that ``compounds'' a binary operator `rator` so that `compound rator n x` is `x` if `n=0`, `x rator x` if `n = 1`, and in general `x rator (x rator (... rator x))` where `rator` is applied exactly `n` times. `compound rator` need not behave well when applied to negative integers.

2. Use the `compound` function to define a Curried function for integer exponentiation

```
val exp : int -> int -> int
```

so that, for example, `exp 3 2` evaluates to 9. *Hint: take note of the description of `op` in Ullman S5.4.4, page 165.*

Don't get confused by infix vs prefix operators. Remember this:

- ◆ Fixity is a property of an identifier, not of a value.
- ◆ If `<$>` is an infix identifier, then `x <$> y` is syntactic sugar for `<$>` applied to a pair containing `x` and `y`, which can also be written as `op <$> (x, y)`.

Patterns

- B. Write a function `firstVowel` that takes a list of lower-case letters and returns `true` if the first character is a vowel (aeiou) and `false` if the first character is not a vowel or if the list is empty. Use the wildcard symbol `_` whenever possible, and avoid `if`. *Remember that the ML character syntax is `#"x"`, as described in Ullman, page 13.*
- C. Write the function `null`, which when applied to a list tells whether the list is empty. Avoid `if`, and make sure the function takes constant time. Make sure your function has the same type as the `null` in the Standard Basis.

Lists

- D. `foldl` and `foldr` are predefined with type

```
('a * 'b -> 'b) -> 'b -> 'a list -> 'b
```

They are like the μ Scheme versions except the ML versions are Curried.

1. Implement `rev` (the function known in μ Scheme as "reverse") using `foldl` or `foldr`.
2. Implement `minlist`, which returns the smallest element of a non-empty list of integers. Your solution should work regardless of the representation of integers (e.g., it should not matter how many bits the module `Int` uses to represent integers). Your solution can fail (e.g., by `raise Match`) if given an empty list of integers. Use `foldl` or `foldr`.

Do not use recursion in any of your solutions.

- E. Implement `foldl` and `foldr` using recursion. Do not create unnecessary cons cells. Do not use `if`.
- F. Define a function

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```
val pairfoldr : ('a * 'b * 'c -> 'c) -> 'c -> 'a list * 'b list -> 'c
```

that applies a three-argument function to a pair of lists of equal length, using the same order as `foldr`. Use `pairfoldr` to implement `zip`.

G. Define a function

```
val flatten : 'a list list -> 'a list
```

which takes a list of lists and produces a single list containing all the elements in the correct order. For example,

```
<sample>+= [<-D->]
- flatten [[1], [2, 3, 4], [], [5, 6]];
> val it = [1, 2, 3, 4, 5, 6] : int list
```

To get full credit for this problem, your function should use no unnecessary cons cells.

Exceptions

H. Write a (Curried) function

```
val nth : int -> 'a list -> 'a
```

to return the n th element of a list. (Number elements from 0.) If `nth` is given arguments on which it is not defined, raise a suitable exception. You may define one or more suitable exceptions or you may choose to use an appropriate one from the initial basis. (If you have doubts about what's appropriate, play it safe and define an exception of your own.)

I expect you to implement `nth` yourself and not simply call `List.nth`.

I. Environments

1. Define a type 'a `env` and functions

```
<sample>+= [<-D->]
type 'a env = (* you fill in this part with a suitable list type *)
exception NotFound of string
val emptyEnv : 'a env = (* ... *)
val bindVar : string * 'a * 'a env -> 'a env = (* ... *)
val lookup : string * 'a env -> 'a = (* ... *)
```

Defines `bindVar`, `emptyEnv`, `env`, `lookup`, `NotFound` (links are to index).

such that you can use 'a `env` for a type environment or a value environment. On an attempt to look up an identifier that doesn't exist, raise the exception `NotFound`. Don't worry about efficiency.

2. Do the same, except make type 'a `env` = string -> 'a, and let

```
<sample>+= [<-D->]
fun lookup (name, rho) = rho name
```

Defines `lookup` (links are to index).

3. Write a function

```
val isBound : string * 'a env -> bool
```

that works with both representations of environments. That is, write a *single* function that works regardless of whether environments are implemented as lists or as functions. You will need imperative features, like sequencing (the semicolon). Don't use `if`.

4. Write a function

```
val extendEnv : string list * 'a list * 'a env -> 'a env
```

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that takes a list of variables and a list of values and adds the corresponding bindings to an environment. It should work with both representations. Do *not* use recursion. *Hint: you can do it in two lines using the higher-order list functions defined above.*

You should put these functions in the same file; don't worry about the later ones shadowing the earlier ones.

Algebraic data types

J. Search trees.

ML can easily represent binary trees containing arbitrary values in the nodes:

```
<sample>+= [<-D->]
datatype 'a tree = NODE of 'a tree * 'a * 'a tree
                | LEAF
```

Defines `tree` (links are to index).

To make a search tree, we need to compare values at nodes. The standard idiom for comparison is to define a function that returns a value of type `order`. As discussed in Ullman, page 325, `order` is *predefined* by

```
<sample>+= [<-D->]
datatype order = LESS | EQUAL | GREATER      (* do not include me in your code *)
```

Defines `order` (links are to index).

Because `order` is predefined, if you include it in your program, you will hide the predefined version (which is in the initial basis) and other things may break mysteriously. So don't include it.

We can use the `order` type to define a higher-order insertion function by, e.g.,

```
<sample>+= [<-D->]
fun insert cmp =
  let fun ins (x, LEAF) = NODE (LEAF, x, LEAF)
        | ins (x, NODE (left, y, right)) =
            (case cmp (x, y)
             of LESS    => NODE (ins (x, left), y, right)
              | GREATER => NODE (left, y, ins (x, right))
              | EQUAL   => NODE (left, x, right))
    in ins
  end
```

Defines `insert` (links are to index).

This higher-order insertion function accepts a comparison function as argument, then returns an insertion function. (The parentheses around `case` aren't actually necessary here, but I've included them because if you leave them out when they *are* needed, you will be very confused by the resulting error messages.)

We can use this idea to implement polymorphic sets in which we store the comparison function in the set itself. For example,

```
<sample>+= [<-D->]
datatype 'a set = SET of ('a * 'a -> order) * 'a tree
fun nullset cmp = SET (cmp, LEAF)
```

Defines `nullset`, `set` (links are to index).

◆ Write a function

```
val addelt : 'a * 'a set -> 'a set
```

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that adds an element to a set.

- ◆ Write a function

```
val treeFoldr : ('a * 'b -> 'b) -> 'b -> 'a tree -> 'b
```

that folds a function over every element of a tree, rightmost element first. Calling `treeFoldr op :: [] t` should return the elements of `t` in order. Write a similar function

```
val setFold : ('a * 'b -> 'b) -> 'b -> 'a set -> 'b
```

The function `setFold` should visit every element of the set exactly once, in an unspecified order.

An immutable, persistent alternative to linked lists

- K. This problem asks you to define your own representation of a new abstraction: the *list with finger*. A *list with finger* is a *nonempty* sequence of values, together with a "finger" that points at one position in the sequence. The abstraction provides constant-time insertion and deletion at the finger.

This is a challenge problem. The other problems on the homework all involve old wine in new bottles. To solve this problem, you have to *think* of something new.

1. Define a representation for type `'a flist`. (Before you can define a representation, you will want to study the rest of the parts of this problem, plus the test cases.)

Document your representation by saying, in a short comment, what sequence is meant by any value of type `'a flist`.

2. Define function

```
val singletonOf : 'a -> 'a flist
```

which returns a sequence containing a single value, whose finger points at that value.

3. Define function

```
val atFinger : 'a flist -> 'a
```

which returns the value that the finger points at.

4. Define functions

```
val fingerLeft  : 'a flist -> 'a flist
val fingerRight : 'a flist -> 'a flist
```

Calling `fingerLeft xs` creates a new list that is like `xs`, except the finger is moved one position to the left. If the finger belonging to `xs` already points to the leftmost position, then `fingerLeft xs` should raise the same exception that the Basis Library raises for array access out of bounds. Function `fingerRight` is similar. Both functions must run in **constant time and space**.

Please think of these functions as "moving the finger", but remember **no mutation is involved**. Instead of changing an existing list, each function creates a new list.

5. Define functions

```
val deleteLeft  : 'a flist -> 'a flist
val deleteRight : 'a flist -> 'a flist
```

Calling `deleteLeft xs` creates a new list that is like `xs`, except the value `x` to the left of the finger has been removed. If the finger points to the leftmost position, then `deleteLeft` should raise the same exception that the Basis Library raises for array access out of bounds. Function `deleteRight` is similar. Both functions must run in **constant time and space**. As before, no mutation is involved.

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6. Define functions

```
val insertLeft : 'a * 'a flist -> 'a flist
val insertRight : 'a * 'a flist -> 'a flist
```

Calling `insertLeft` (`x`, `xs`) creates a new list that is like `xs`, except the value `x` is inserted to the left of the finger. Function `insertRight` is similar. Both functions must run in **constant time and space**. As before, no mutation is involved. (These functions are related to "cons".)

7. Define functions

```
val ffoldl : ('a * 'b -> 'b) -> 'b -> 'a flist -> 'b
val ffoldr : ('a * 'b -> 'b) -> 'b -> 'a flist -> 'b
```

which do the same thing as `foldl` and `foldr`, but ignore the position of the finger.

Here is a simple test case, which should produce a list containing the numbers 1 through 5 in order. You can use `ffoldr` to confirm.

```
val test = singletonOf 3
val test = insertLeft (1, test)
val test = insertLeft (2, test)
val test = insertRight (4, test)
val test = fingerRight test
val test = insertRight (5, test)
```

You'll want to test the `delete` functions as well.

Hints: The key is to come up with a good representation for "list with finger." Once you have a good representation, the code is easy: over half the functions can be implemented in one line each, and no function requires more than two lines of code.

Pair Problem (10%)

You may work with a partner on this problem.

The goal of this problem is to give you practice working with an algebraic data type that plays a central role in programming languages: expressions. In the coming month, you will write many functions that consume expressions; this problem will help you get off to a good start. It will also give you a feel for the kinds of things compiler writers do.

This problem asks you to explore the fact that a compiler doesn't need to store an entire environment in a closure; it only needs to store the free variables of its lambda expression. For the details you will want the [handout on free variables](#), which is also available as Section 6.10 in your textbook.

You'll solve the problem in a prelude and four parts:

- The prelude is to go to your copy of the book code and copy the file `bare/uscheme-ml/mlscheme.sml` to your working directory. (This code contains all of the interpreter from Chapter 6.) Then make *another* copy and name it `mlscheme-improved.sml`. You will edit `mlscheme-improved.sml`.
- The first part is to implement the free-variable predicate

```
val freeIn : exp -> name -> bool.
```

This predicate tells when a variable appears free in an expression. It implements the proof rules on page 224 of the [handout](#).

I recommend that you **compile early and often** using

```
/usr/sup/bin/mosmlc -c mlscheme-improved.sml
```

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- The second part is to write a function that takes a pair consisting of a LAMBDA body and an environment, and returns a better pair containing the same LAMBDA body paired with an environment that contains only the free variables of the LAMBDA. (In the handout, on page 225, this environment is explained as the *restriction* of the environment to the free variables.) You should call this function `improve` and give it the type

```
val improve : (name list * exp) * 'a env -> (name list * exp) * 'a env
```

- The third part is to use `improve` in the evaluation case for LAMBDA, which appears in the book on page 349. You simply apply `improve` to the pair that is already there, so your improved interpreter looks like this:

```
(* more alternatives for ev for ((mlscheme)) 349c *)
| ev (LAMBDA (xs, e)) = ( errorIfDups ("formal parameter", xs, "lambda")
                        ; CLOSURE (improve ((xs, e), rho))
                        )
```

- The fourth and final part is to see if it makes a difference. Compile both versions of the μ Scheme interpreter using MLton, which is an optimizing, native-code compiler for Standard ML.

```
mlton -verbose 1 -output mlscheme          mlscheme.sml
mlton -verbose 1 -output mlscheme-improved mlscheme-improved.sml
```

(If plain `mlton` doesn't work, try `/usr/sup/bin/mlton`.)

I have provided a script that you can use to measure the improvement. I also recommend that you compare the performance of the ML code with the performance of the C code in the course directory.

```
◆ time run-exponential-arg-max 22 ./mlscheme
◆ time run-exponential-arg-max 22 ./mlscheme-improved
◆ time run-exponential-arg-max 22 /comp/105/bin/uscheme
```

Hints:

- Focus on function `freeIn`. This is the only recursive function and the only function that requires case analysis on expressions. And it is the only function that requires you to understand the concept of free variables. You will be using **all** of these concepts on future assignments.

In Standard ML, the μ Scheme function `exists?` is called `List.exists`. You'll have lots of opportunities to use it. If you don't use it, you're making extra work for yourself.

In addition to `List.exists`, you may have a use for `map`, `foldr`, `foldl`, or `List.filter`.

You might also have a use for these functions:

```
fun fst (x, y) = x
fun snd (x, y) = y

fun member (y, []) = false
  | member (y, z::zs) = y = z orelse member (y, zs)
```

- The code for LETSTAR is gnarly, and writing it adds little to the experience. Here are two algebraic laws which may help:

```
freeIn (LETX (LETSTAR, [], e)) y = freeIn e y

freeIn (LETX (LETSTAR, b::bs, e)) y = freeIn (LETX (LET, [b], LETX (LETSTAR, bs, e))) y
```

- It's easier to write `freeIn` if you use nested functions. Mostly the variable `y` doesn't change, so you needn't pass it everywhere. You'll see the same technique used in the `eval` and `ev` functions in the chapter.
- If you can apply what you have learned on the `scheme` and `hofs` assignments, you should be able to write `improve` on one line, without using any explicit recursion.
- Let the compiler help you: **compile early and often**.

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The implementation of `freeIn` in the solutions is 21 lines of ML.

Extra credit

order) * ('a * 'a -> 'a) list -> 'a -> int -> 'a set such that reachable (Int.compare, [op +, op -, op *, op div]) 5 5 computes the set of all integers computable using the given operators and exactly five 5's. (You don't have to bother giving the answers to the questions above, since they're easy to get with `setFold`.) My solution is under 20 lines of code, but it makes heavy use of the `setFold`, `nullset`, `addelt`, and `pairfoldr` functions defined earlier.

Hints:

- In order to be able to use `Int.compare`, you will either have to run `mosml -P full` or else tell Moscow ML interactively to load `"Int"`;
- Begin your function definition this way:

```
fun reachable (cmp, operators) five n =
  (* produce set of expressions reachable with exactly n fives *)
```

- Use **dynamic programming**.
- Create a list of length $k-1$ in which element i is a set containing all the integers that can be computed using exactly i elements. Now compute the k th element of the list by combining 1 with $k-1$, 2 with $k-2$, etcetera.
- Try doing the above by passing a list and its reverse, then use `pairfoldr` with a suitable function.
- The initial list contains a set with exactly one element (in the example above, 5).
- Make sure your solution has the completely general type given above, so you could use it with different operations and with different representations of numbers.

-->

VARARGS

Extend μ Scheme to support procedures with a variable number of arguments. Do so by giving the name `...` (three dots) special significance when it appears as the last formal parameter in a lambda. For example:

```
-> (val f (lambda (x y ...)) (+ x (+ x (foldl + 0 ...))))
-> (f 1 2 3 4 5) ; inside f, rho = { x |-> 1, y |->, ... |-> '(3 4 5) }
15
```

In this example, it is an error for `f` to get fewer than two arguments. If `f` gets at least two arguments, any additional arguments are placed into an ordinary list, and the list is used to initialize the location of the formal parameter associated with `...`

1. Implement this new feature inside of `mlscheme.sml`. I recommend that you begin by changing the definition of `lambda` on page 344 to

```
and lambda = name list * { varargs : bool } * exp
```

The type system will tell you what other code you have to change. For the parser, you may find the following function useful:

```
fun newLambda (formals, body) =
  case rev formals
  of "... " :: fs' => LAMBDA (rev fs', {varargs=true}, body)
  | _              => LAMBDA (formals, {varargs=false}, body)
```

The type of this function is

```
name list * exp -> name list * {varargs : bool} * exp;
```

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thus it is designed exactly for you to adapt old syntax to new syntax; you just drop it into the parser wherever LAMBDA was used.

2. As a complement to the `varargs lambda`, write a new `call` primitive such that

```
(call f '(1 2 3))
```

is equivalent to

```
(f 1 2 3)
```

Sadly, you won't be able to use `PRIMITIVE` for this; you'll have to invent a new kind of thing that has access to the internal `eval`.

3. Demonstrate these utilities by writing a higher-order function `cons-logger` that counts `cons` calls in a private variable. It should operate as follows:

```
-> (val c1 (cons-logger))
-> (val log-cons (car c1))
-> (val conses-logged (cdr c1))
-> (conses-logged)
0
-> (log-cons f e1 e2 ... en) ; returns (f e1 e2 ... en), incrementing
                             ; private counter whenever cons is called
-> (conses-logged)
99 ; or whatever else is the number of times cons is called
    ; during the call to log-cons
```

4. Rewrite the `APPLY-CLOSURE` rule to account for the new abstract syntax and behavior. To help you, simplified [LaTeX for the original rule](#) is online.

What to submit: Individual Problems

You should submit two or three files, depending upon whether you did the extra credit:

- a `README` file containing
 - ◆ the names of the people with whom you collaborated
 - ◆ the numbers of the problems that you solved
 - ◆ the number of hours you worked on the assignment.
- `warmup.sml` containing the solutions to Exercises A to K. At the start of each problem, please label it with a short comment, like

```
(***** Problem A *****)
```

To receive credit, your `warmup.sml` file must compile and execute in the Moscow ML system. For example, we must be able to compile your code *without warnings or errors*:

```
% /usr/sup/bin/mosmlc -c warmup.sml
%
```

- (optionally) `varargs.sml` containing your solution to the extra credit.

How to submit: Individual Problems

When you are ready, run `submit105-ml-solo` to submit your work. Note you can run this script multiple times; we will grade the last submission.

What to submit: Pair Problem

You should submit one file: `mlscheme-improved.sml`. You should include the output of the commands listed in part (4) in comments in this file.

How to submit: Pair Problems

When you are ready, run `submit105-ml-pair` to submit your work. Note you can run this script multiple times; we will grade the last submission.

Hints

- Some useful list patterns include the following patterns that match lists of *exactly* 0, 1, 2, or 3 elements:

```
<patterns>= [D->]
[]
[x]
[x, y]
[a, b, c]
```

and also these patterns, which match lists of *at least* 0, 1, 2, or 3 elements:

```
<patterns>+= [<-D]
xs
x::xs
x1::x2::xs
a::b::c::xs
```

When using these patterns, remember that *function application has higher precedence than any infix operator!* This property is as true in patterns as it is anywhere else.

- The following table may help you transfer your knowledge of μ Scheme to ML:

μ Scheme	ML
val	val
define	fun
lambda	fn

- For your reference, [sample code](#) is available.
- Make sure your solutions have the right types.* On this assignment, it is a *very* common mistake to define functions of the wrong type. You can protect yourself a little bit by loading declarations like the following *after* loading your solution:

```
<sample>+= [<-D]
(* first declaration for sanity check *)
val compound : ('a * 'a -> 'a) -> int -> 'a -> 'a = compound
val exp : int -> int -> int = exp
val fib : int -> int = fib
val firstVowel : char list -> bool = firstVowel
val null : 'a list -> bool = null
val rev : 'a list -> 'a list = rev
val minlist : int list -> int = minlist
val foldl : ('a * 'b -> 'b) -> 'b -> 'a list -> 'b = foldl
val foldr : ('a * 'b -> 'b) -> 'b -> 'a list -> 'b = foldr
val zip : 'a list * 'b list -> ('a * 'b) list = zip
val pairfoldr : ('a * 'b * 'c -> 'c) -> 'c -> 'a list * 'b list -> 'c = pairfoldr
val unzip : ('a * 'b) list -> 'a list * 'b list = unzip
val flatten : 'a list list -> 'a list = flatten
val nth : int -> 'a list -> 'a = nth
val emptyEnv : 'a env = emptyEnv
val bindVar : string * 'a * 'a env -> 'a env = bindVar
val lookup : string * 'a env -> 'a = lookup
val isBound : string * 'a env -> bool = isBound
val extendEnv : string list * 'a list * 'a env -> 'a env = extendEnv
val addelt : 'a * 'a set -> 'a set = addelt
val treeFoldr : ('a * 'b -> 'b) -> 'b -> 'a tree -> 'b = treeFoldr
val setFold : ('a * 'b -> 'b) -> 'b -> 'a set -> 'b = setFold
```

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```
val scons : 'a * 'a seq -> 'a seq = scons
val ssnoc : 'a * 'a seq -> 'a seq = ssnoc
val sappend : 'a seq * 'a seq -> 'a seq = sappend
val listOfSeq : 'a seq -> 'a list = listOfSeq
val seqOfList : 'a list -> 'a seq = seqOfList
val singletonOf : 'a -> 'a flist = singletonOf
val atFinger : 'a flist -> 'a = atFinger
val fingerLeft : 'a flist -> 'a flist = fingerLeft
val fingerRight : 'a flist -> 'a flist = fingerRight
val deleteLeft : 'a flist -> 'a flist = deleteLeft
val deleteRight : 'a flist -> 'a flist = deleteRight
val insertLeft : 'a * 'a flist -> 'a flist = insertLeft
val insertRight : 'a * 'a flist -> 'a flist = insertRight
val ffoldl : ('a * 'b -> 'b) -> 'b -> 'a flist -> 'b = ffoldl
val ffoldr : ('a * 'b -> 'b) -> 'b -> 'a flist -> 'b = ffoldr
(* last declaration for sanity check *)
```

Defines [addelt](#), [atFinger](#), [bindVar](#), [compound](#), [deleteLeft](#), [deleteRight](#), [emptyEnv](#), [exp](#), [extendEnv](#), [ffoldl](#), [ffoldr](#), [fib](#), [fingerLeft](#), [fingerRight](#), [firstVowel](#), [flatten](#), [foldl](#), [foldr](#), [insertLeft](#), [insertRight](#), [isBound](#), [listOfSeq](#), [lookup](#), [minlist](#), [nth](#), [null](#), [pairfoldr](#), [rev](#), [sappend](#), [scons](#), [seqOfList](#), [setFold](#), [singletonOf](#), [ssnoc](#), [treeFoldr](#), [unzip](#), [zip](#) (links are to index).

I don't promise to have all the functions and their types here. Making sure that every function has the right type is **your** job, not mine.

Avoid common mistakes

Here is a list of common mistakes to avoid:

- If you *redefine a type* that is already in the initial basis, code will fail in baffling ways. (If you find yourself baffled, exit the interpreter and restart it.)
- Redefining a function at the top-level is fine *unless that function captures one of your own functions in its closure*. Example:

```
fun f x = ... stuff that is broken ...
fun g (y, z) = ... stuff that uses 'f' ...
fun f x = ... new, correct version of 'f' ...
```

You now have a situation where *g is broken, and the resulting error is very hard to detect*. Stay out of this situation; instead, *load fresh definitions from a file using the use function*.

- *Never put a semicolon after a definition*. I don't care if Jeff Ullman does it; it's wrong! You should have a semicolon only if you are deliberately using imperative features.
- It's a common mistake to become very confused about *where you need to use op*. Ullman covers `op` in Section 5.4.4, page 165.
- It's a common mistake to *include redundant parentheses in your code*. To avoid this mistake, follow the directions in the [course supplement to Ullman](#).

How your work will be evaluated

The criteria are analogous to those for the `scheme` and `hofs` assignments.

Index and cross-reference

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