

## Review: Information revealed to self

Object knows its own representation (“instance variables”), invariants, private methods:

```
(class Fraction Number
  (num den) ;; representation (concrete!)
            ;; invariants: lowest terms, den > 0

  (method asFraction ()
    self)
  (method print ()
    (print num) (print #/) (print den))
  (method reciprocal ()
    (signReduce (setNum:den: (new Fraction) den num)))
```

## Information revealed to self: your turn

How would you implement `coerce:`?  
(Value of argument, representation of receiver)

```
...
(method asFraction ()
  self)
(method print ()
  (print num) (print #/) (print den))
(method reciprocal ()
  (signReduce (setNum:den: (new Fraction) den num)))
(method coerce: (aNumber)
  ...)
```

## Information revealed to self: your turn

How would you implement `coerce:`?  
(Value of argument, representation of receiver)

...

```
(method asFraction ())
```

```
  self)
```

```
(method print ())
```

```
  (print num) (print #/) (print den))
```

```
(method reciprocal ())
```

```
  (signReduce (setNum:den: (new Fraction) den num)))
```

```
(method coerce: (aNumber)
```

```
  asFraction aNumber)
```

## **Exposing information, part II**

**Alas! Cannot see representation of argument**

**How will you know “equal, less or greater”?**

## Exposing information, part II

**Alas! Cannot see representation of argument**

**Protocol says “like with like”? Use private methods**

```
(method num () num) ; private
```

```
(method den () den) ; private
```

```
(method = (f) ;; relies on invariant!
```

```
  (and: (= num (num f)) { (= den (den f)) })))
```

```
(method < (f)
```

```
  (< (* num (den f)) (* (num f) den)))
```

**Remember behavioral subtyping**

## **Private methods: Your turn**

**How will you multiply two fractions?**

## Private methods: Your turn

How will you multiply two fractions?

```
(method * (f)
  (divReduce
    (setNum:den: (new Fraction)
      (* num (num f))
      (* den (den f))))))
```

# An open system

**Number protocol: like multiplies with like**

**What about large and small integers?**

- **How to multiply two small integers?**
- **How to multiply two large integers?**

**How is algorithm known?**

**Each object knows its own algorithm:**

- **Small: Use machine-primitive multiplication**
- **Large: Multiply magnitudes; choose sign**

## Review: Two kinds of knowledge

I can send message to you:

- I know your **protocol**

I can inherit from you:

- I know my **subclass responsibilities**

# Knowledge of protocol

Three levels of knowledge:

1. I know only your **public methods**

Example: `select`:

2. You are like me: share **private methods**

Example: `*` and `+` on `Fraction`

3. I must get to know you: **double dispatch**

Example: `*` and `+` on **mix of integers**

# Double dispatch: extending open systems

I claim:

- Large integers and small integers both `Integer`
- Messages `=`, `<`, `+`, `*` ought to mix freely
- Large and small integers have **different private protocol**

Private for large integers: `magnitude`

Private for small integers: `mul:withOverflow`

# Double dispatch code operation & protocol

## Example messages:

- I answer the small-integer protocol, add me to yourself
- I answer the large-positive integer protocol, multiply me by yourself

## Message encodes

- Operation to be performed
- Protocol accepted by **argument**

## Your turn: responding to double dispatch

How do you act?

1. As small integer, you receive “add small integer  $n$  to `self`”
2. As small integer, you receive “multiply large positive integer  $N$  by `self`”
3. As large positive integer, you receive “add small integer  $n$  to `self`”
4. As large positive integer, you receive “multiply large positive integer  $N$  by `self`”

## Your turn: using double dispatch

On what class does each method go?

A. (method + (aNumber)

(addSmallIntegerTo: aNumber self))

B. (method \* (anInteger)

(multiplyByLargePositiveInteger: anInteger self))

(See the “double dispatch”: + then

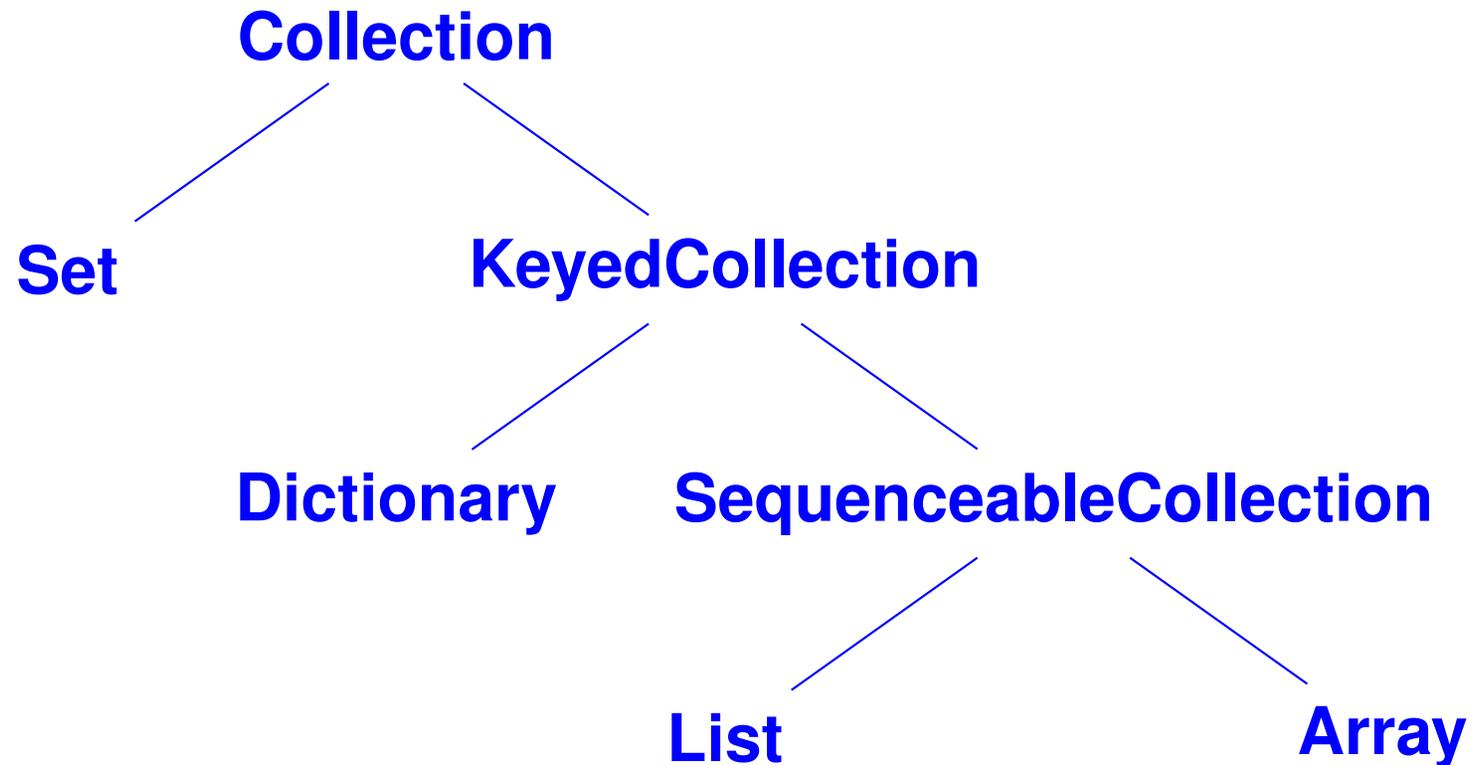
addSmallIntegerTo:)

# Information-hiding summary

## Three levels

1. I use your public protocol
2. We are alike; I add **our** private protocol
3. Your protocol is revealed by double dispatch

# “Collection hierarchy”



## Collection mutators

`add: newObject` **Add argument**

`addAll: aCollection` **Add every element of arg**

`remove: oldObject` **Remove arg, error if absent**

`remove:ifAbsent: oldObject exnBlock`

**Remove the argument, evaluate `exnBlock` if absent**

`removeAll: aCollection` **Remove every element of arg**

## Collection observers

`isEmpty` **Is it empty?**

`size` **How many elements?**

`includes: anObject` **Does receiver contain arg?**

`occurrencesOf: anObject` **How many times?**

`detect: aBlock` **Find and answer element**

**satisfying** `aBlock` (cf  `$\mu$ Scheme exists?`)

`detect:ifNone: aBlock exnBlock` **Detect,**

**recover if none**

`asSet` **Set of receiver's elements**

## Collection iterators

**do:** aBlock For each element **x**, evaluate (value  
aBlock **x**).

**inject:into:** thisValue binaryBlock

**Essentially  $\mu$ Scheme** foldl

**select:** aBlock **Essentially  $\mu$ Scheme** filter

**reject:** aBlock **Filter for *not* satisfying** aBlock

**collect:** aBlock **Essentially  $\mu$ Scheme** map

## Implementing collections

```
(class Collection Object
  () ; abstract
  (method do: (aBlock)
    (subclassResponsibility self))
  (method add: (newObject)
    (subclassResponsibility self))
  (method remove:ifAbsent (oldObj exnBlock)
    (subclassResponsibility self))
  (method species ()
    (subclassResponsibility self))
  <other methods of class Collection>
)
```

## Reusable methods

```
<other methods of class Collection>=
(method addAll: (aCollection)
  (do: aCollection [block(x) (add: self x)])
  aCollection)
(method size () [locals temp]
  (set temp 0)
  (do: self [block(_) (set temp (+ temp 1))])
  temp)
```

**These methods always work**

**Subclasses can override (redefine) with more efficient versions**

## species **method**

Create “collection like the reciever”

Example: filtering

```
<other methods of class Collection>=  
(method select: (aBlock) [locals temp]  
  (set temp (new (species self)))  
  (do: self [block (x)  
    (ifTrue: (value aBlock x)  
      {(add: temp x)}))])  
temp)
```

# Subtyping mathematically

Always transitive

$$\frac{\tau_1 <: \tau_2 \quad \tau_2 <: \tau_3}{\tau_1 <: \tau_3}$$

Key rule is **subsumption**:

$$\frac{e : \tau \quad \tau <: \tau'}{e : \tau'}$$

(*implicit* subsumption: no cast)

# Subtyping is not inheritance

Subtype understands *more* messages:

---

$$\{m_1 : \tau_1, \dots, m_n : \tau_n, \dots, m_{n+k} : \tau_{n+k}\} <: \{m_1 : \tau_1, \dots, m_n : \tau_n\}$$

If an object understands messages  $m_1, \dots, m_n$ , and possibly more besides, you can use it where  $m_1, \dots, m_n$  are expected

- Methods must **behave** as expected

**Behavioral subtyping** (in Ruby, “duck typing”)

## The four crucial Collection methods

```
(class Collection Object
  () ; abstract
  (method do: (aBlock)
    (subclassResponsibility self))
  (method add: (newObject)
    (subclassResponsibility self))
  (method remove:ifAbsent (oldObj exnBlock)
    (subclassResponsibility self))
  (method species ()
    (subclassResponsibility self))
  <other methods of class Collection>
)
```

```

(class Set Collection
  (members) ; list of elements
  (class-method new () (initSet (new super)))
  (method initSet () ; private method
    (set members (new List))
    self)
  (method do: (aBlock) (do: members aBlock))
  (method remove:ifAbsent: (item exnBlock)
    (remove:ifAbsent: members item exnBlock))
  (method add: (item)
    (ifFalse: (includes: members item)
      { (add: members item) })
    item)
  (method species () Set)
  (method asSet () self) ; extra efficient
)

```

```

(class Set Collection
  (members) ; list of elements
  (class-method new () (initSet (new super)))
  (method initSet () ; private method
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    self)
  (method do: (aBlock) (do: members aBlock))
  (method remove:ifAbsent: (item exnBlock)
    (remove:ifAbsent: members item exnBlock))
  (method add: (item)
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