

CS 114: Network Security

Lecture 6 - Key Agreement and PKI

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Spring 2023

(some slides courtesy of Prof. Micah Sherr)



Administrivia

- Exam 1 on Feb 16th in class.
- Homework 1, part 2 due Feb. 28th at 11:59pm
 - There's a written component this time!
 - pcap file has been uploaded
 - HW 1 p1 reference solution posted soon

Public Key Cryptography

- Each key pair consists of a public and private component: k^+ (public key), k^- (private key)

$$D_{k^-} (E_{k^+} (m)) = m$$

- Public keys are distributed (typically) through public key certificates
- Anyone can communicate secretly with you ***if they have your certificate***

RSA Key Generation

- Choose distinct primes p and q
- Compute $n = pq$
- Compute $\Phi(n) = \Phi(pq) = (p-1)(q-1)$
- Randomly choose $1 < e < \Phi(pq)$ such that e and $\Phi(pq)$ are coprime. e is the **public key exponent**
- Compute $d = e^{-1} \bmod(\Phi(pq))$. d is the **private key exponent**

$$E_{k^+}(M) : C = M^e \bmod n$$

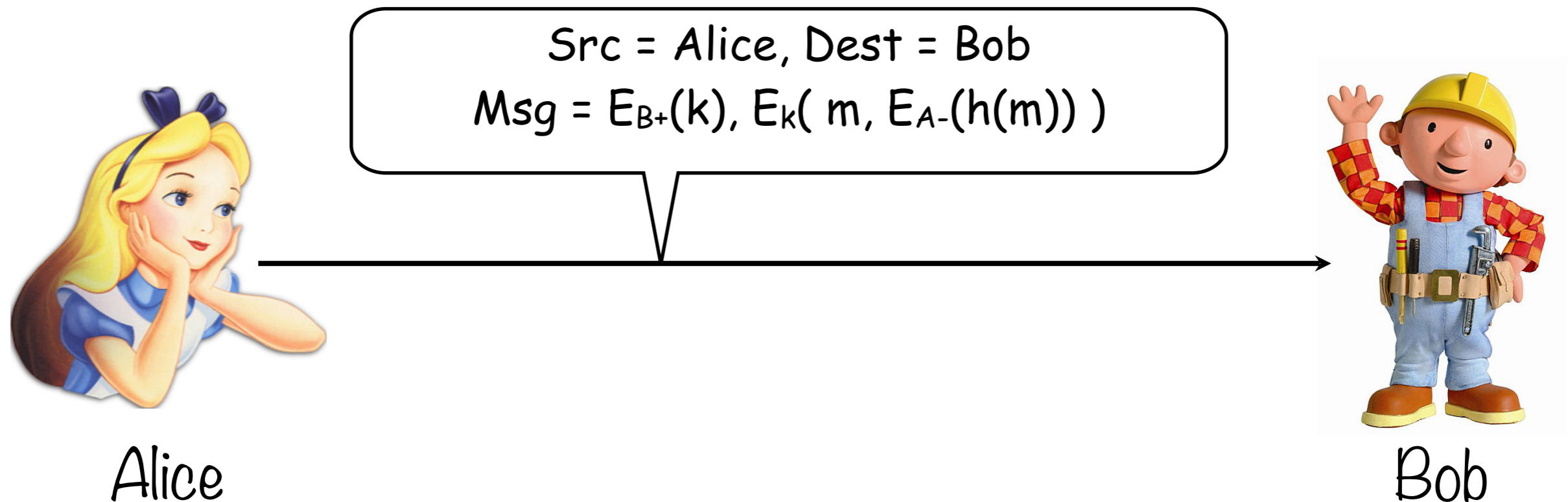
$$D_{k^-}(C) : M = C^d \bmod n$$

Properties of a Digital Signature

- **No forgery possible**
- **No alteration/Integrity**
- **Non-repudiation**

Hybrid Cryptosystems

Define $m = \text{"CSI 14 is awesome"}$

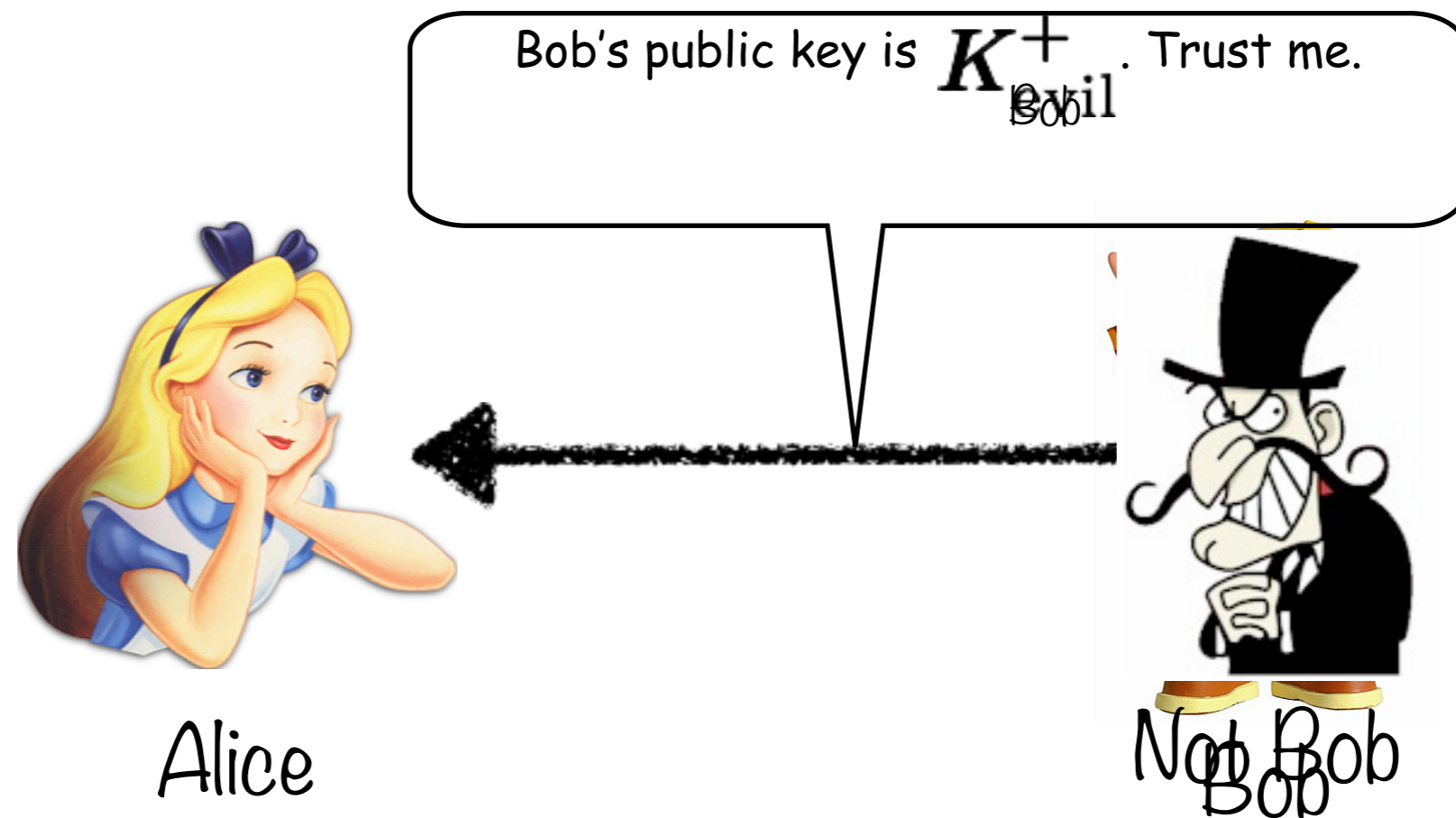


(A^+, A^-) is Alice's long-term public-private key pair.

(B^+, B^-) is Bob's long-term public-private key pair.

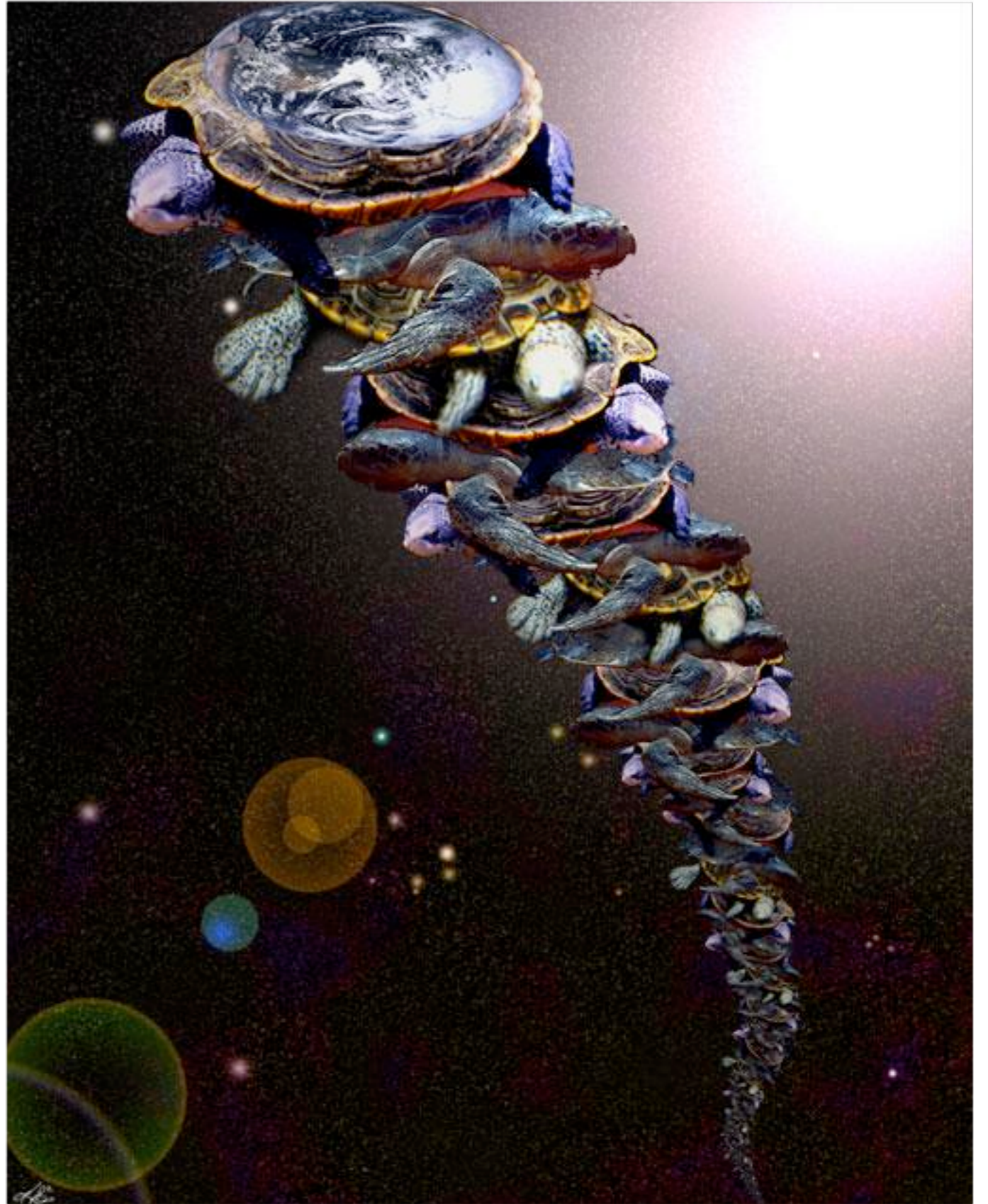
k is the session key; sometimes called the **ephemeral key**.

How do we *verify* we're using the correct public key?



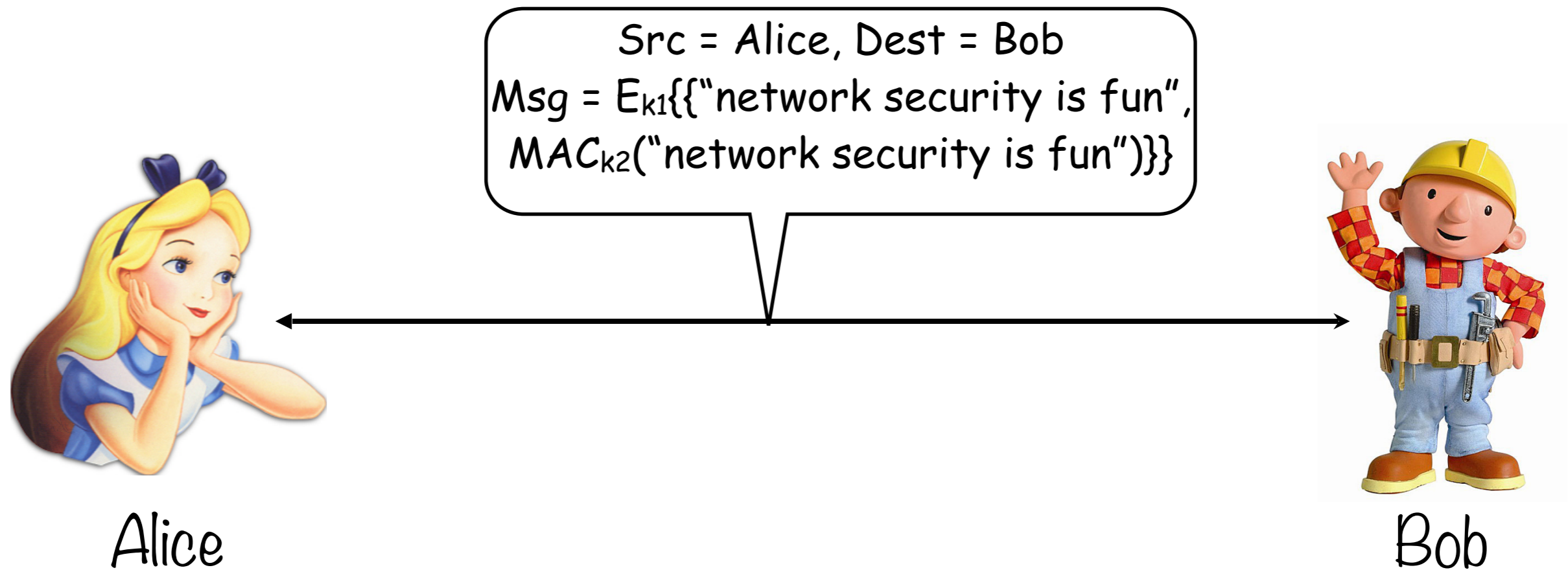
Short answer:
We can't.

It's turtles all
the way down.



Key Agreement, Part I: Sharing a Private Key

Encryption and Message Authenticity



Key Distribution

- Suppose Alice has an channel for communicating with Bob.
- Alice and Bob wish to use this channel to established a shared secret.
- However, Eve is able to learn everything sent over the channel.
- If Alice and Bob have no other channel to use, can they establish a shared secret that Eve does not know?

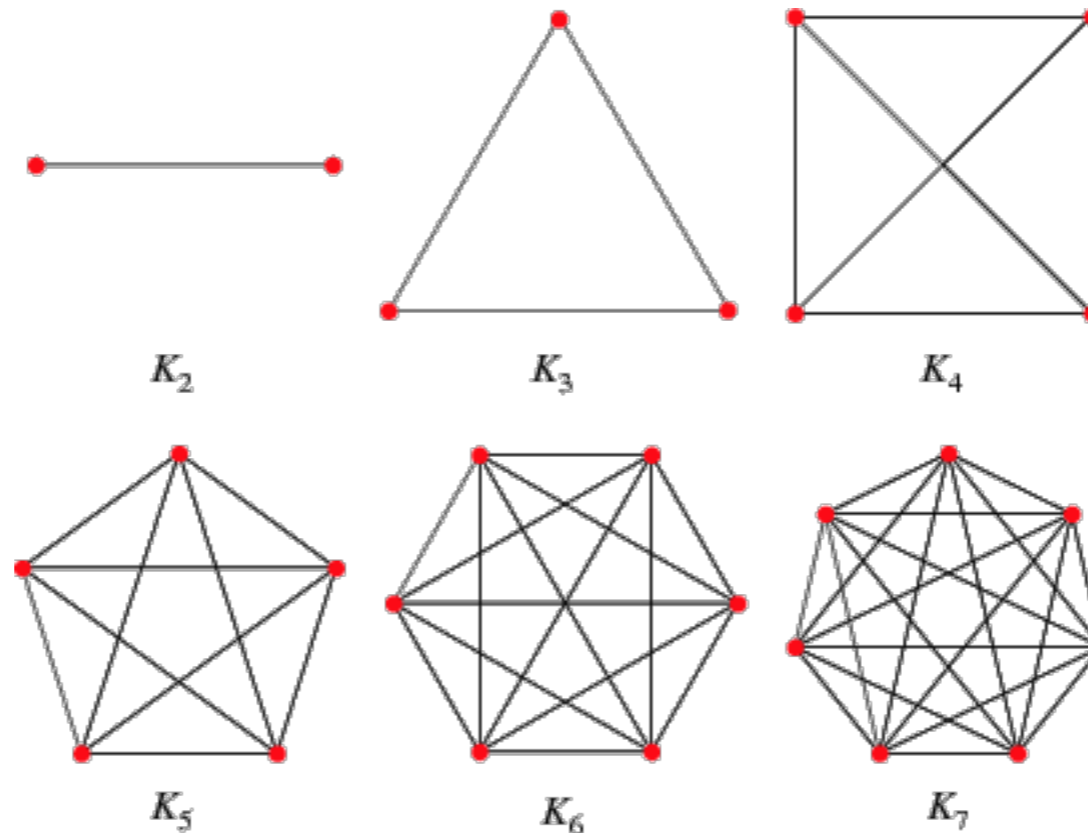
Key Distribution

- Secure key distribution without asymmetric cryptography is difficult
- Simple approach: send key through an out-of-band channel



Key Distribution

- Pairwise key distribution requires $\binom{N}{2}$ plastic cups



Key Distribution and Key Agreement

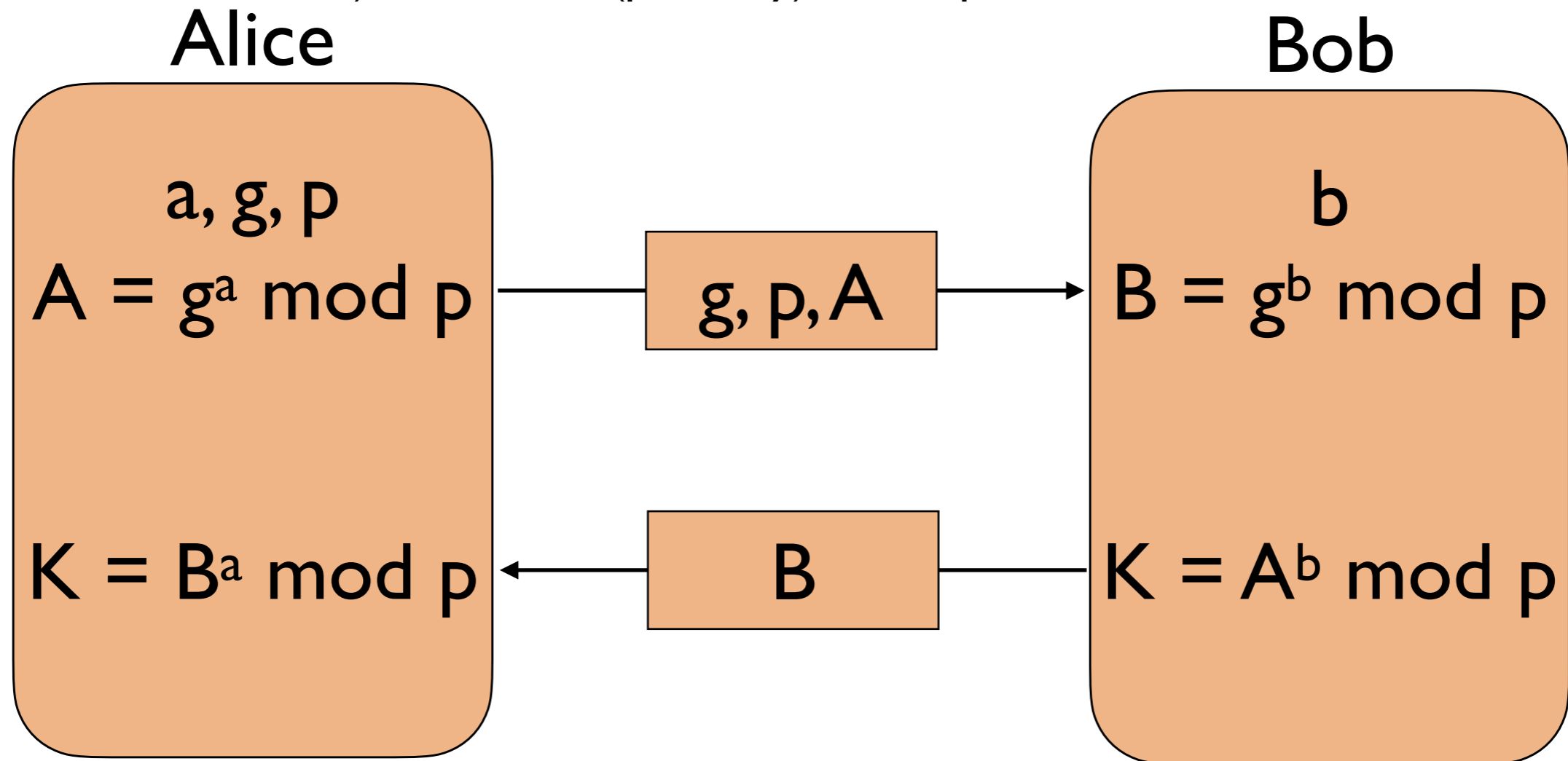
- **Key Distribution** is the process where we assign and transfer keys to a participant
- **Key Agreement** is the process whereby two or more parties negotiate a key

Diffie-Hellman (DH) Key Agreement

- The DH paper started the modern age of cryptography, and indirectly the security community
 - Negotiate a secret over an insecure media
 - E.g., “in the clear” (seems impossible)
 - Idea: participants exchange intractable puzzles that can be solved easily with additional information
- Mathematics are very deep
 - Use the hardness of computing discrete logarithms in finite field to make secure

Diffie-Hellman (DH) Key Agreement

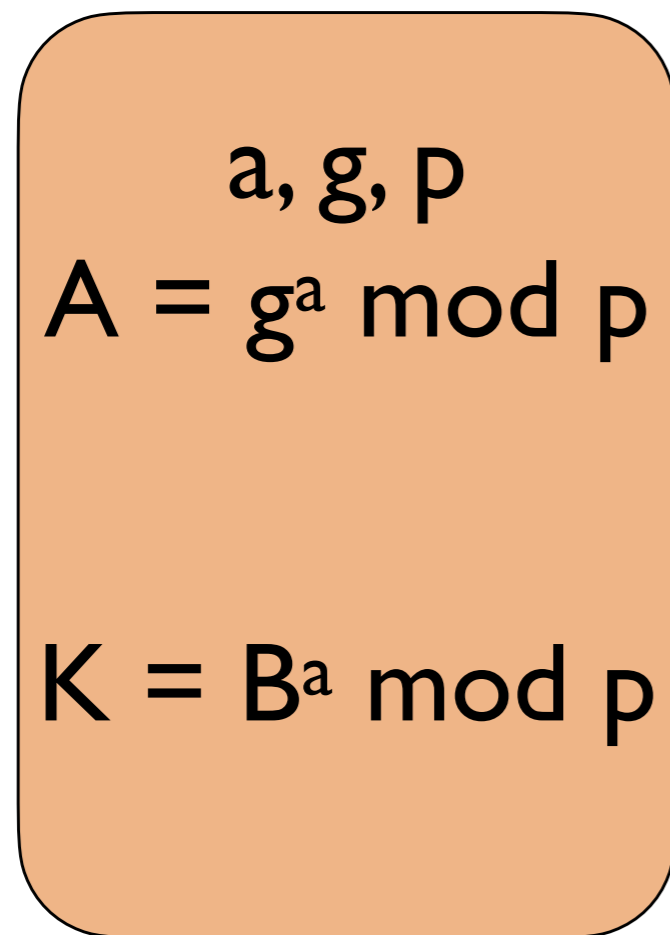
- Proposed by Whitfield Diffie and Martin Hellman in 1976
- g =base, p =prime, a =Alice's secret, b =Bob's secret
- Eve cannot compute K without knowing either a or b (neither of which is transmitted), even if she (passively) intercepts all communication!



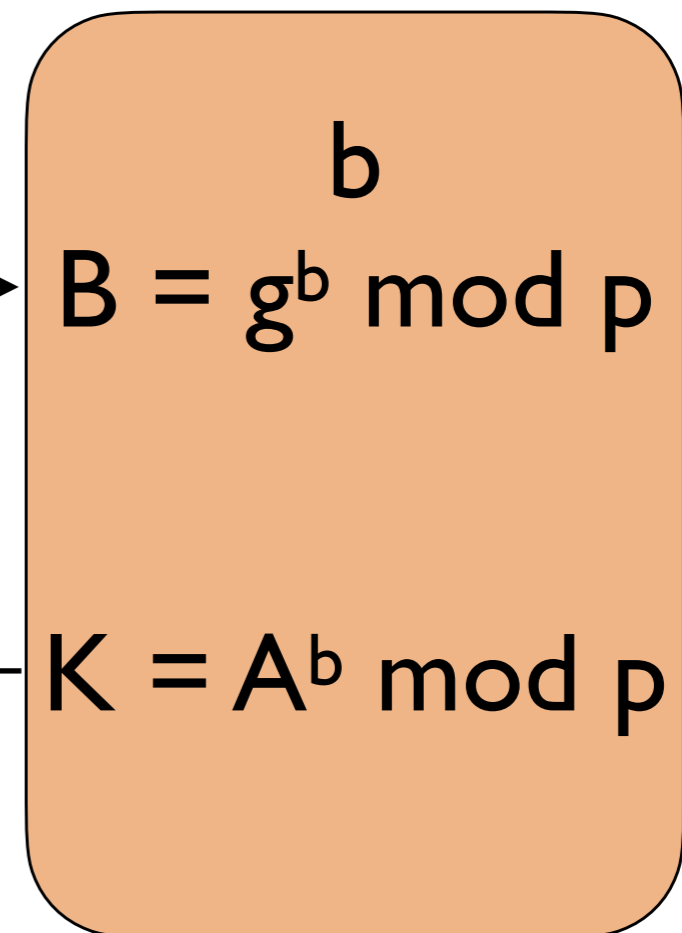
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Alice



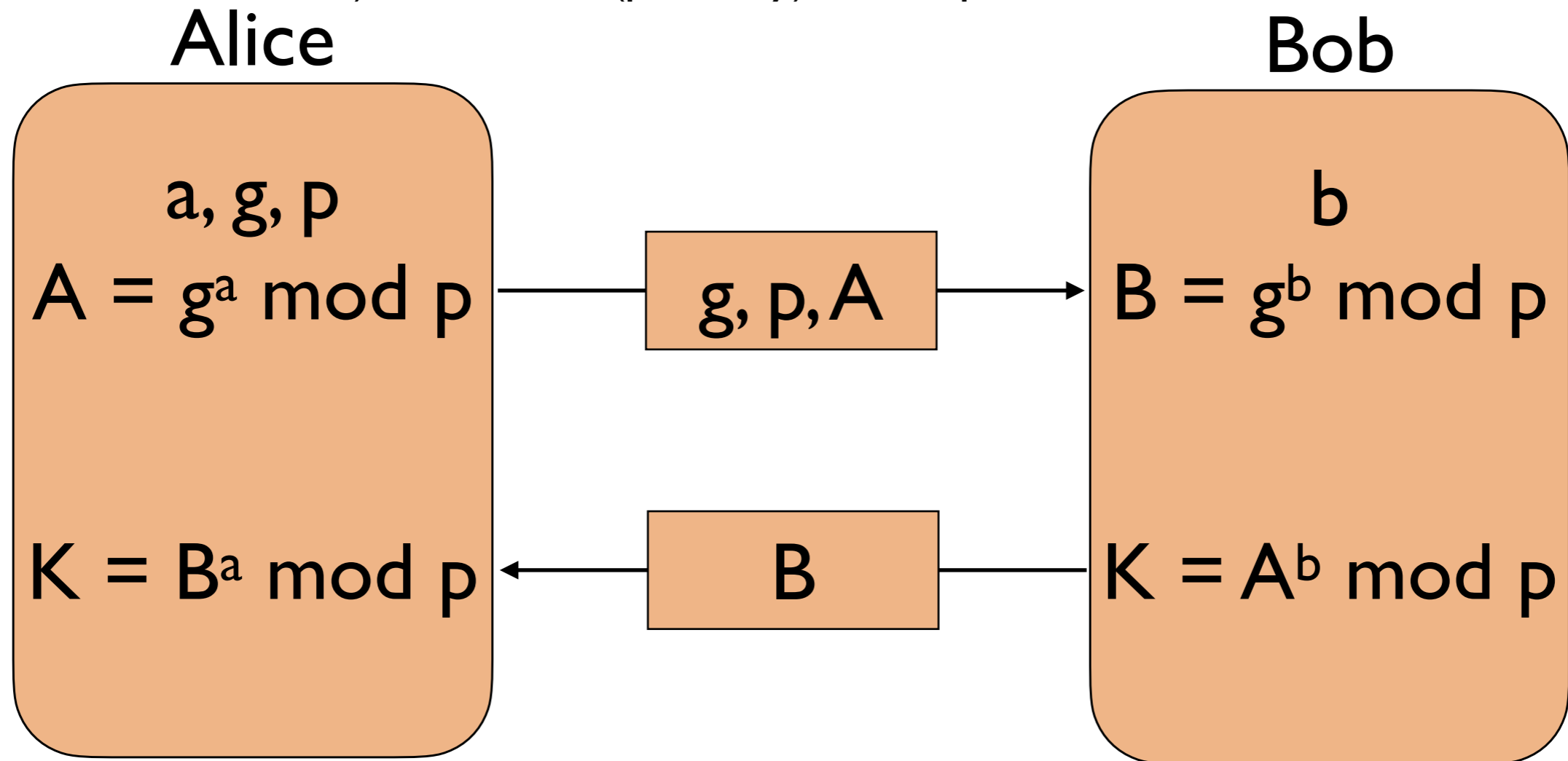
Bob



$$K = B^a \text{ mod } p$$

Diffie-Hellman (DH) Key Agreement

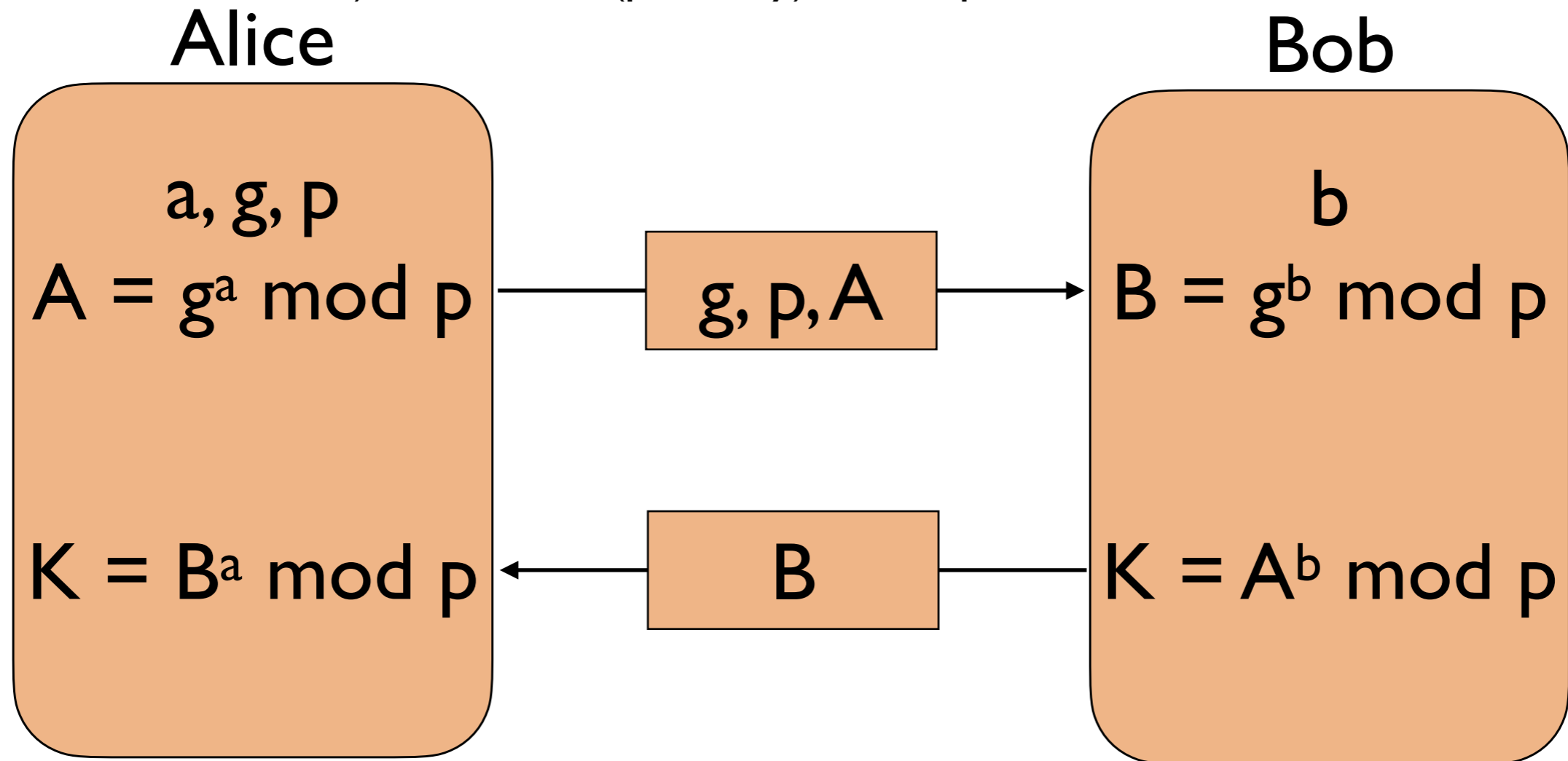
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$$K = B^a \text{ mod } p = (g^b \text{ mod } p)^a \text{ mod } p$$

Diffie-Hellman (DH) Key Agreement

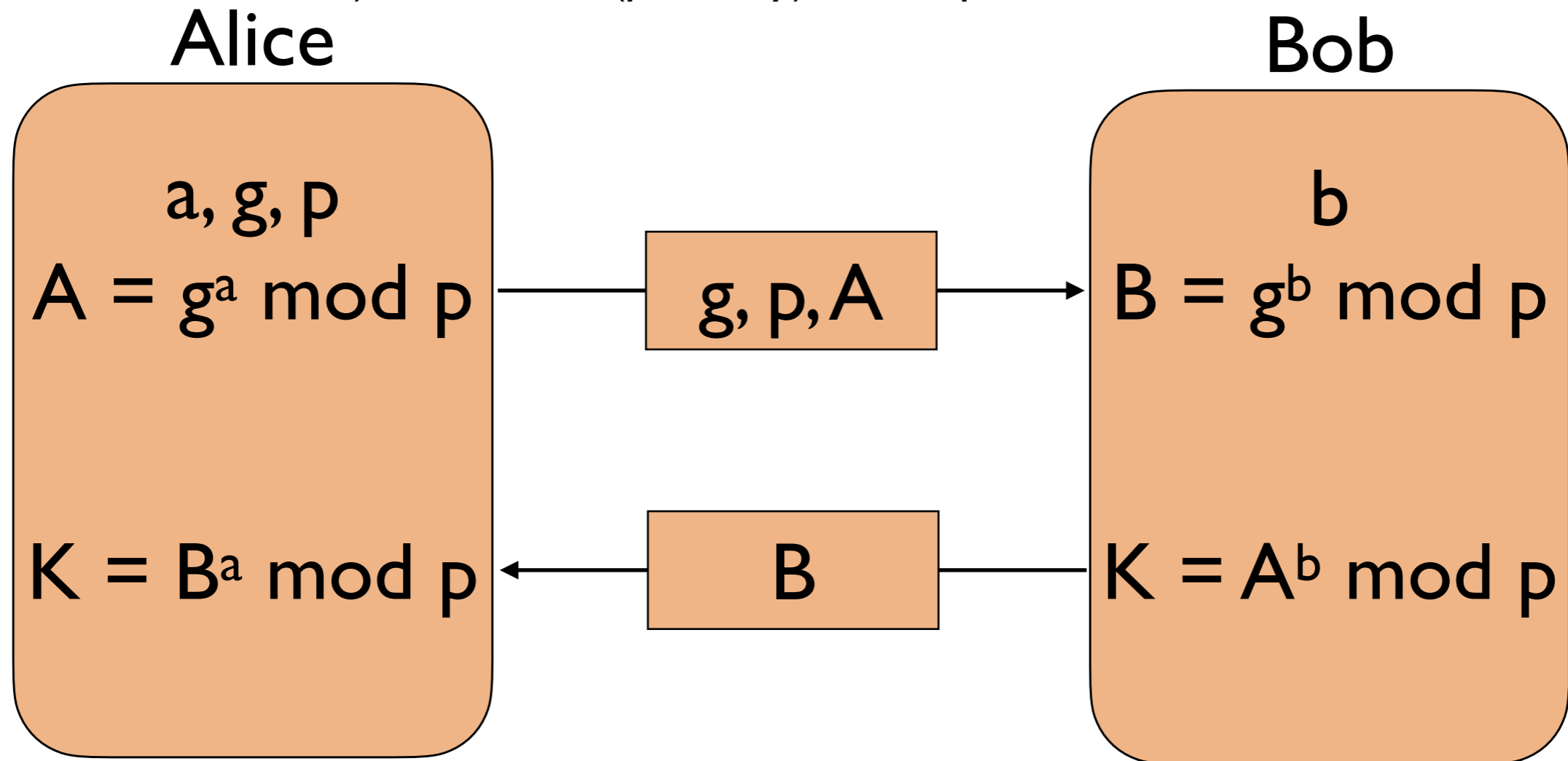
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$$K = B^a \text{ mod } p = (g^b \text{ mod } p)^a \text{ mod } p = g^{ab} \text{ mod } p$$

Diffie-Hellman (DH) Key Agreement

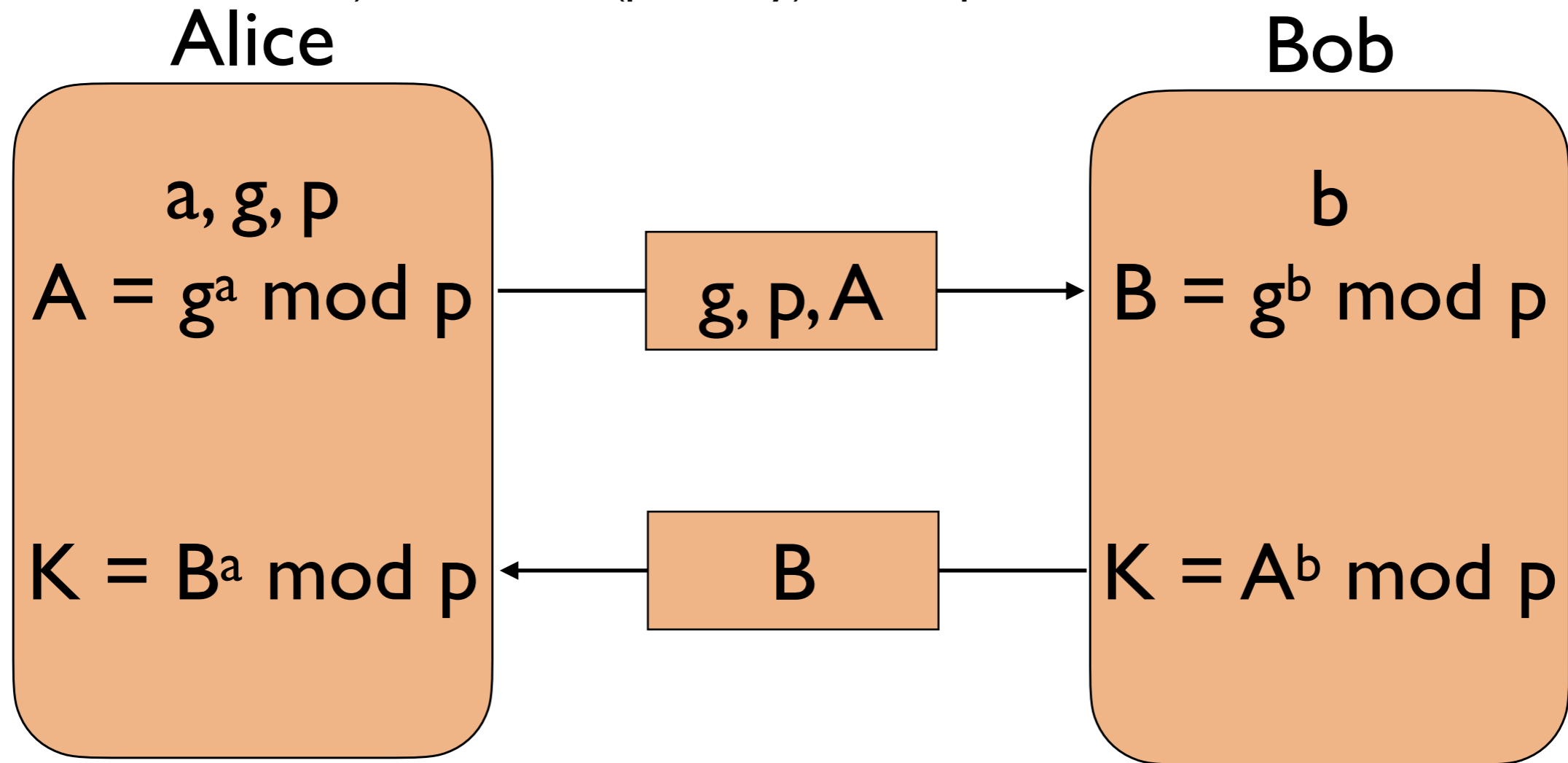
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Diffie-Hellman (DH) Key Agreement

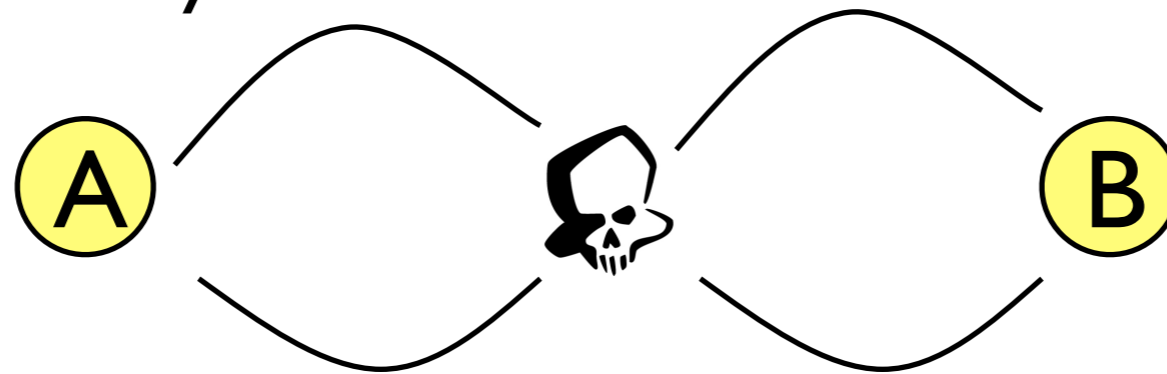
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$$K = B^a \text{ mod } p = (g^b \text{ mod } p)^a \text{ mod } p = g^{ab} \text{ mod } p = (g^a \text{ mod } p)^b \text{ mod } p = A^b \text{ mod } p$$

Attacks on Diffie-Hellman

- Subject to **Man-in-the-Middle** (MitM) attack
- You really don't know anything about who you have exchanged keys with

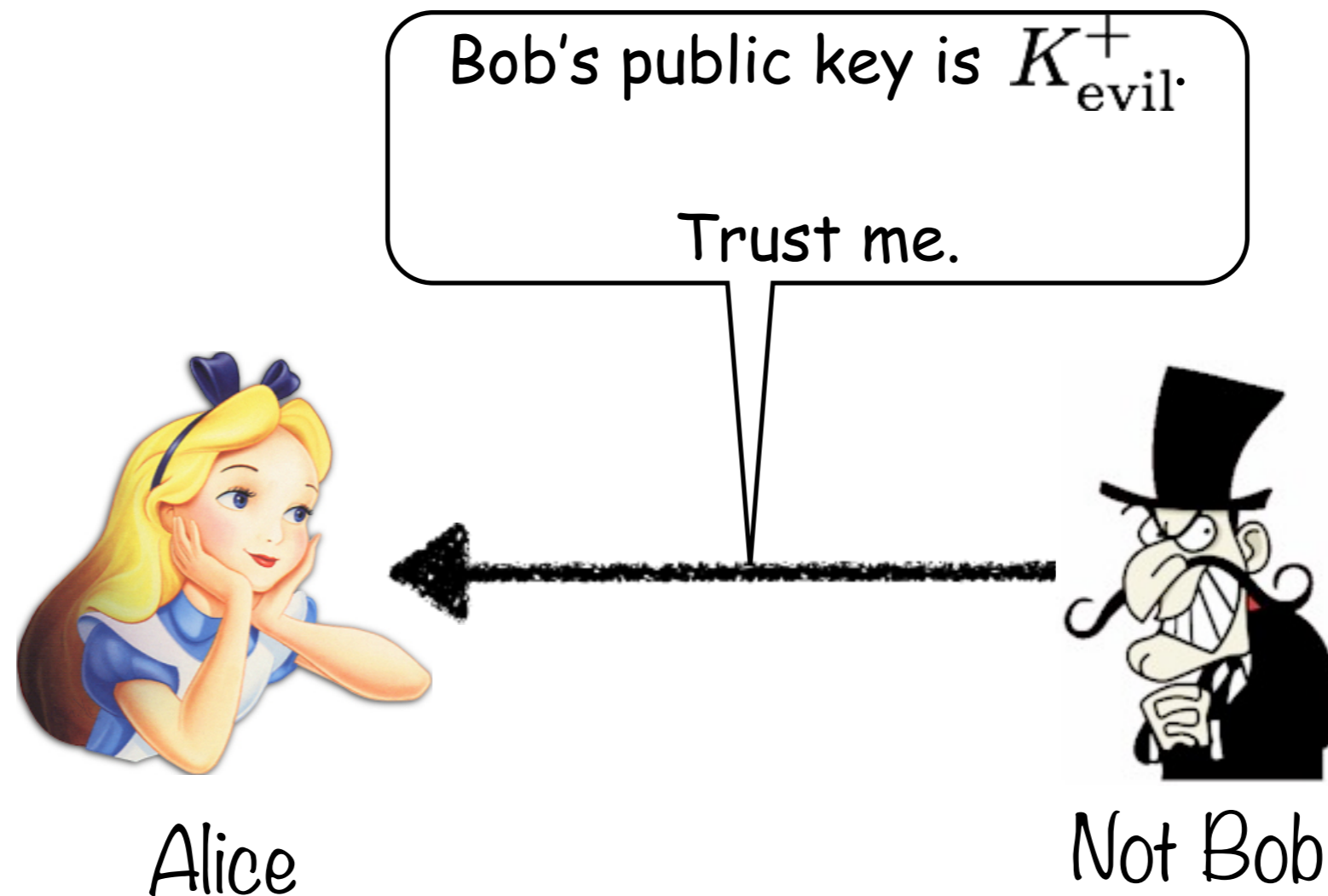


- Alice and Bob think they are talking directly to each other, but Mallory is actually performing two separate exchanges
- Fix: Authenticated DH exchange
 - The parties sign the exchanges (more or less)
 - Requires pre-shared knowledge or trusted third party

Key Agreement, Part II: Public Key Distribution



How do we *verify* we're using the correct public key?

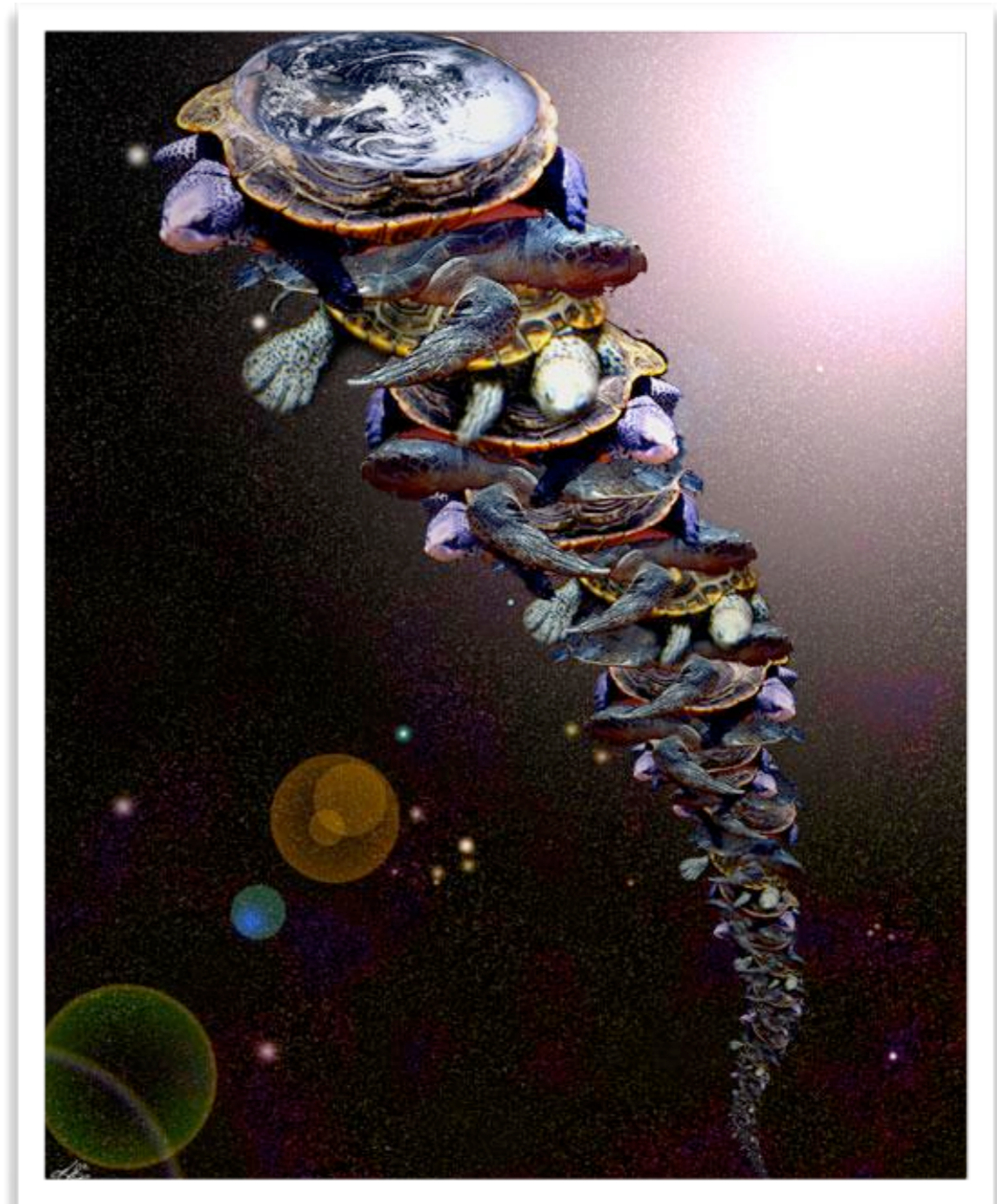


Why not just use a database?

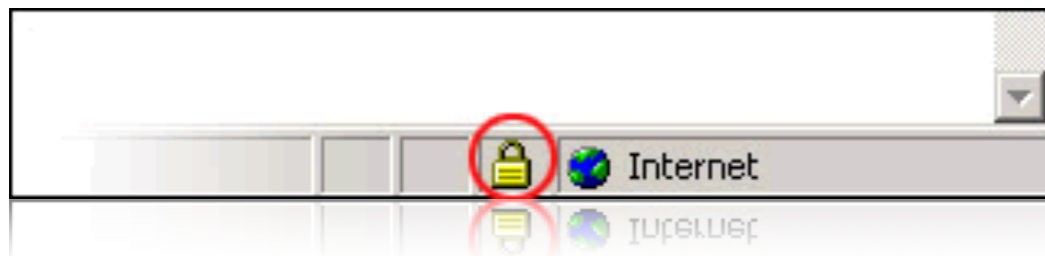
- Every user has his/her own public key and private key.
- Public keys are all published in a database.
- Alice gets Bob's public key from the database
- Alice encrypts the message and sends it to Bob using Bob's public key.
- Bob decrypts it using his private key.
- **What's the problem with this approach?**

Solving the Turtles Problem


- We need a **trust anchor**
 - there must be someone with authority
 - requires *a priori* trust
- Solution: form a trust hierarchy
 - “I believe **X** because...”
 - “**Y** vouches for **X** and...”
 - “**Z** vouches for **Y** and...”
 - “I implicitly trust **Z**.”



Browser Certificate



Class 3 Public Primary Certification Authority
↳ VeriSign Class 3 Public Primary Certification Authority - G5
↳ VeriSign Class 3 International Server CA - G3
↳ www.chase.com

 **www.chase.com**
Issued by: VeriSign Class 3 International Server CA - G3
Expires: Thursday, August 16, 2012 7:59:59 PM ET
✔ This certificate is valid

▼ **Details**

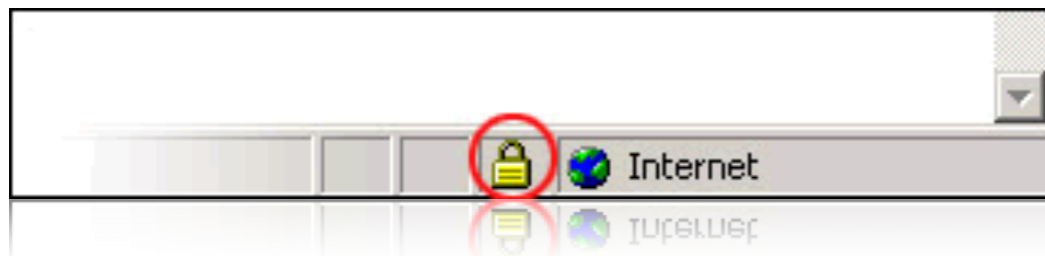
Subject Name	
Country	US
State/Province	New Jersey
Locality	Jersey City
Organization	JPMorgan Chase
Organizational Unit	CIG
Common Name	www.chase.com
Issuer Name	
Country	US
Organization	VeriSign, Inc.
Organizational Unit	VeriSign Trust Network
Organizational Unit	Terms of use at https://www.verisign.com/rpa (c)10
Common Name	VeriSign Class 3 International Server CA - G3
Serial Number	61 5C 33 29 65 09 08 60 A4 E6 82 50 00 F6 22 F0
Version	3
Signature Algorithm	SHA-1 with RSA Encryption (1 2 840 113549 1 1 5)
Parameters	none
Not Valid Before	Tuesday, August 16, 2011 8:00:00 PM ET
Not Valid After	Thursday, August 16, 2012 7:59:59 PM ET

OK

What's a certificate?

- A certificate ...
 - ... makes an association between an identity and a private key
 - ... contains public key information $\{e,n\}$
 - ... has a validity period
 - ... is signed by some *certificate authority* (CA)
 - ... identity may have been vetted by a *registration authority* (RA)
- People trust CA (e.g., Verisign) to vet identity

Browser Certificate

A screenshot of a browser's certificate details dialog box. The dialog box is titled "Class 3 Public Primary Certification Authority" and shows the following information:

Class 3 Public Primary Certification Authority
↳ VeriSign Class 3 Public Primary Certification Authority - G5
↳ VeriSign Class 3 International Server CA - G3
↳ www.chase.com

www.chase.com
Issued by: VeriSign Class 3 International Server CA - G3
Expires: Thursday, August 16, 2012 7:59:59 PM ET
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Details

Subject Name	
Country	US
State/Province	New Jersey
Locality	Jersey City
Organization	JPMorgan Chase
Organizational Unit	CIG
Common Name	www.chase.com

Issuer Name

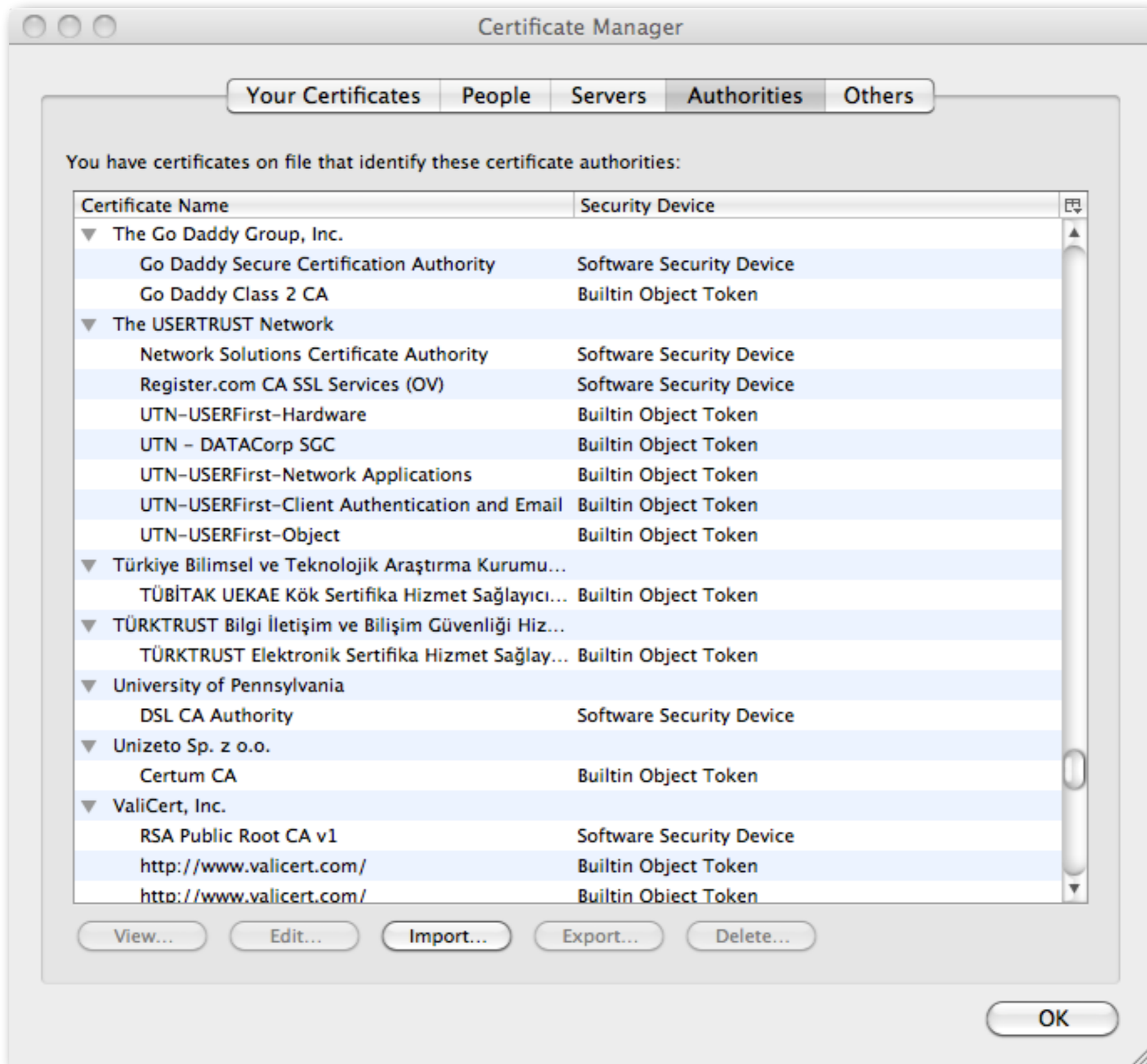
Country	US
Organization	VeriSign, Inc.
Organizational Unit	VeriSign Trust Network
Organizational Unit	Terms of use at https://www.verisign.com/rpa (c)10
Common Name	VeriSign Class 3 International Server CA - G3

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OK

Why do I trust the certificate?

- A collection of “root” CA certificates
 - ... baked into your browser
 - ... vetted by the browser manufacturer
 - ... supposedly closely guarded
- Root certificates used to validate certificate
 - Vouches for certificate’s authenticity



Public Key Infrastructure

Public Key Infrastructure

- Hierarchy of keys used to authenticate certificates
- Requires a **root of trust** (i.e., a **trust anchor**)

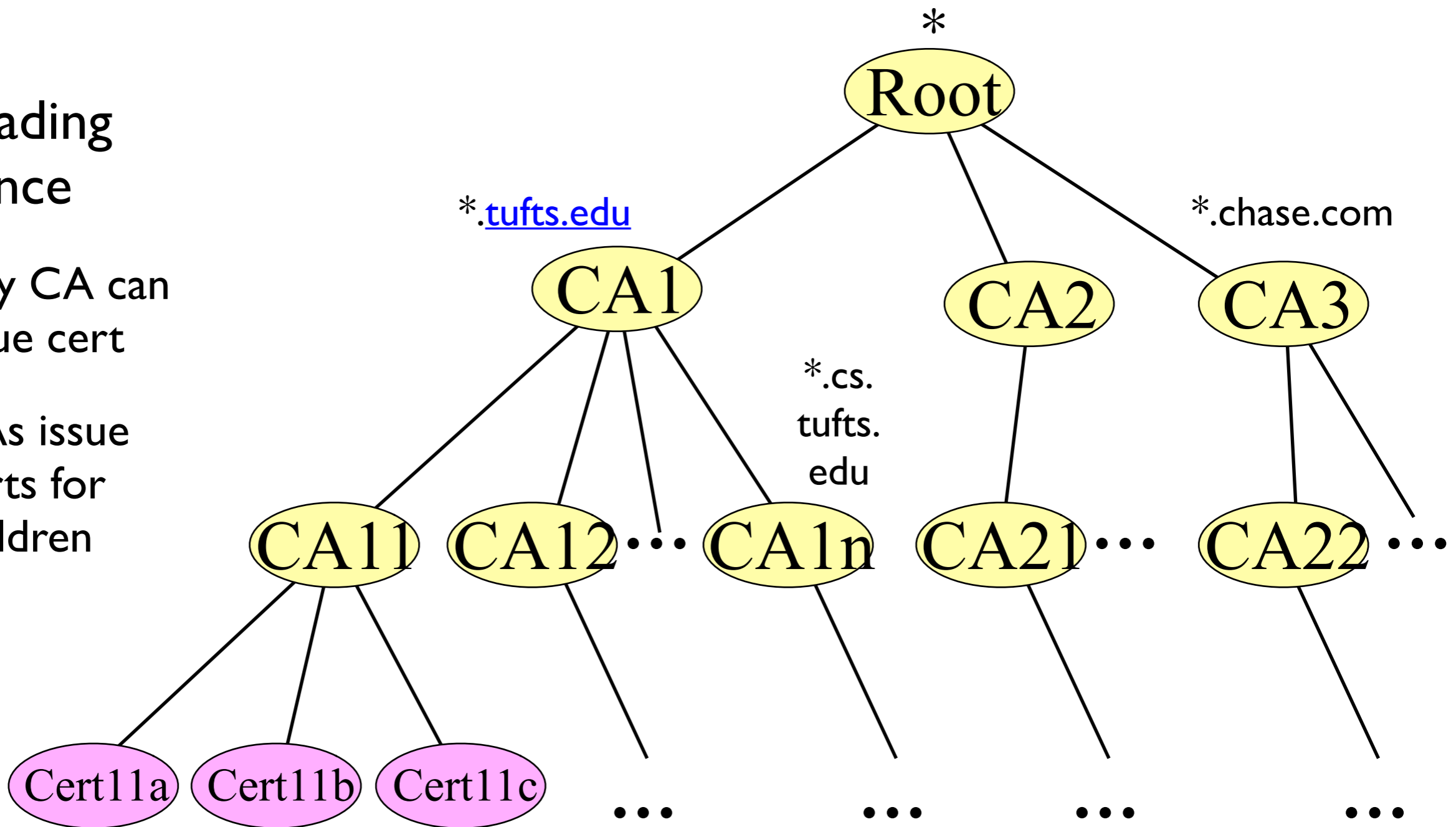
What is a PKI?

- Rooted tree of CAs

- Cascading issuance

- Any CA can issue cert

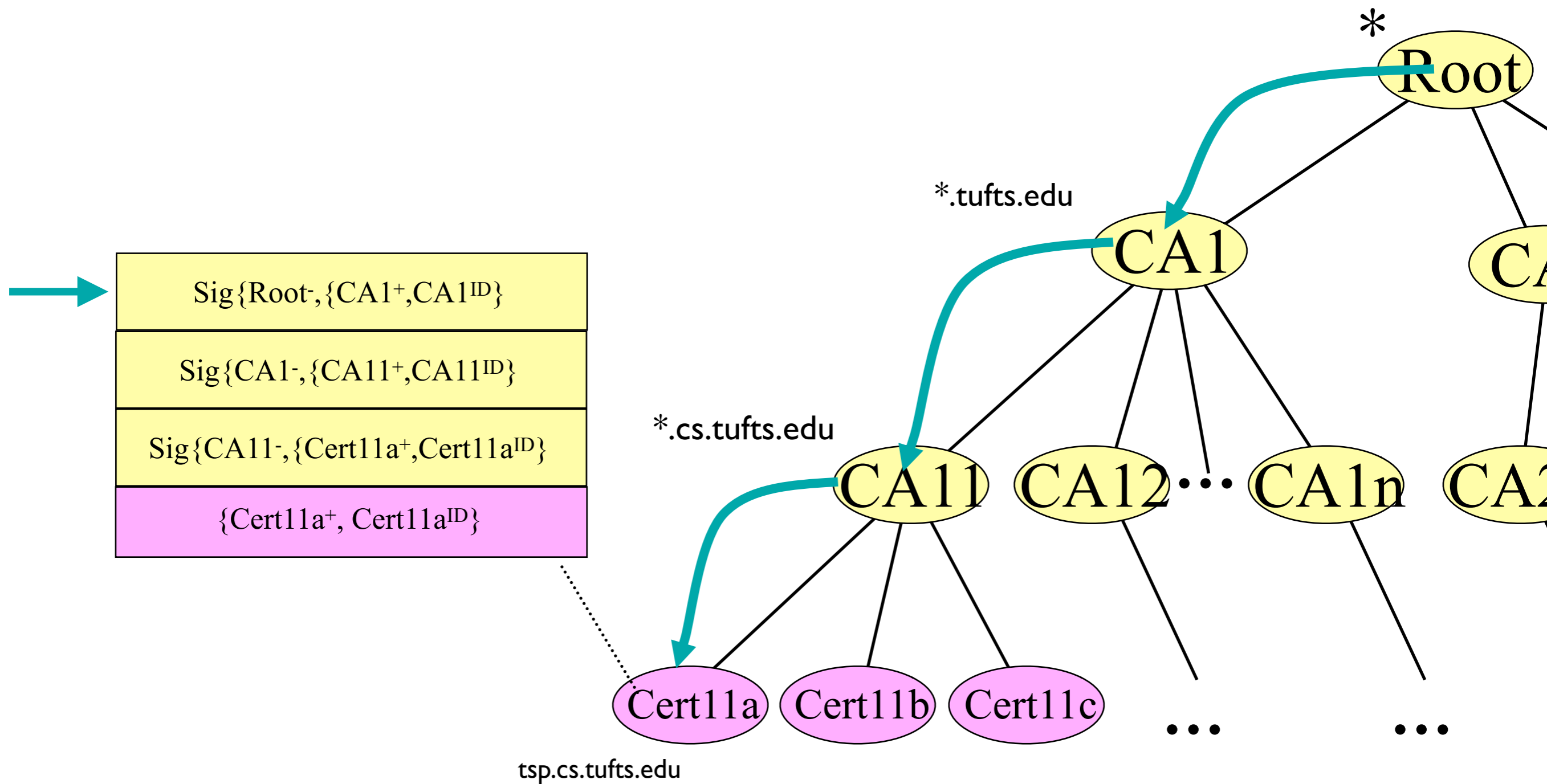
- CAs issue certs for children



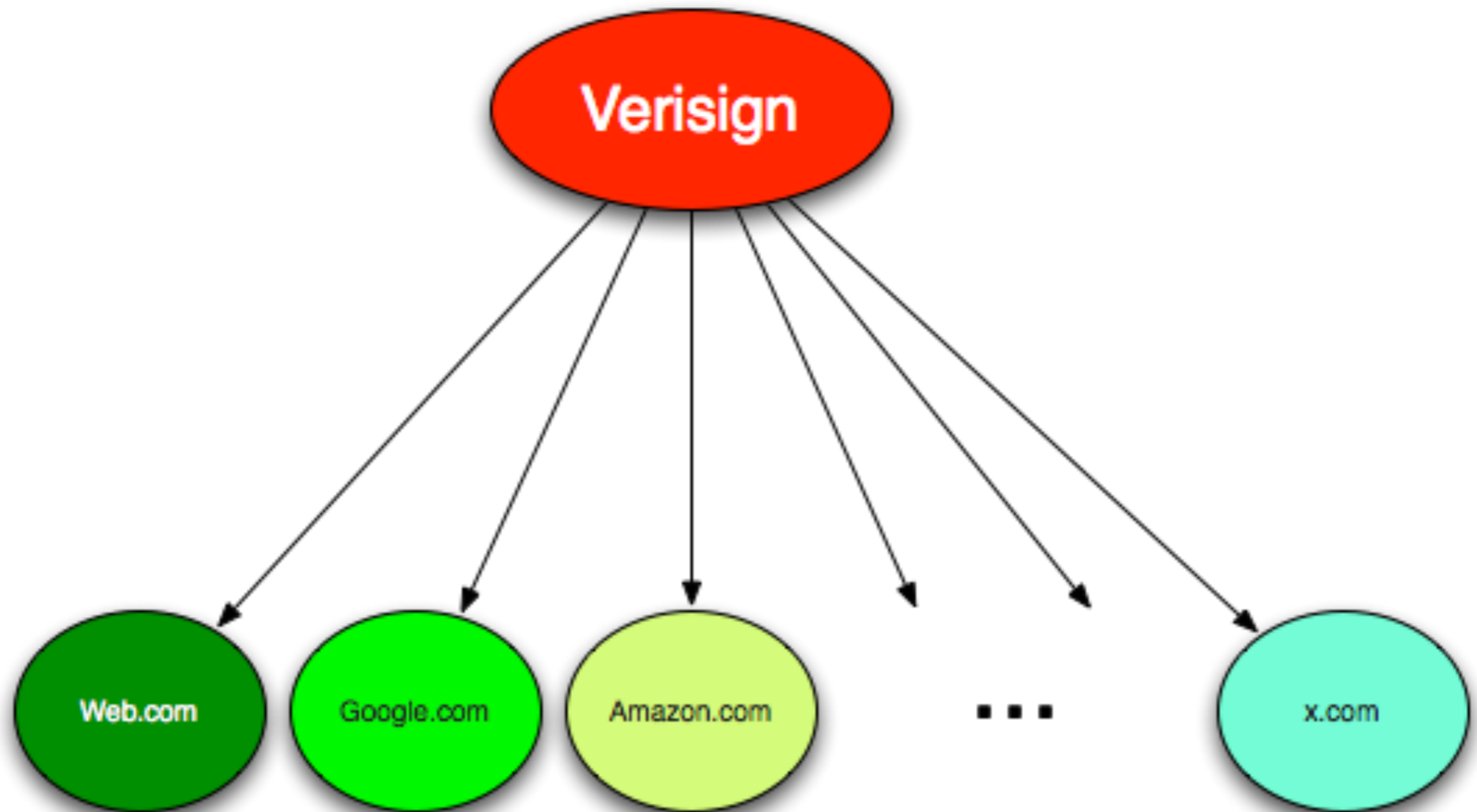
Obtaining a Certificate

1. Alice has some identity document A^{ID} and generates a keypair (A^-, A^+)
2. $A \rightarrow CA : \{A^+, A^{ID}\}, \text{Sig}(A^-, \{A^+, A^{ID}\})$
 - CA verifies signature -- proves Alice has A^-
 - CA may (and should!) also verify A^{ID} offline
3. CA signs $\{A^+, A^{ID}\}$ with its private key (CA^-)
 - CA attests to binding between A^+ and A^{ID}
4. $CA \rightarrow A : \{A^+, A^{ID}\}, \text{Sig}(CA^-, \{A^+, A^{ID}\})$
 - this is the certificate; Alice can freely publish it
 - anyone who knows CA^+ (and can therefore validate the CA's signature) knows that CA "attested to" $\{A^+, A^{ID}\}$
 - note that CA never learns A^-

Certificate Validation

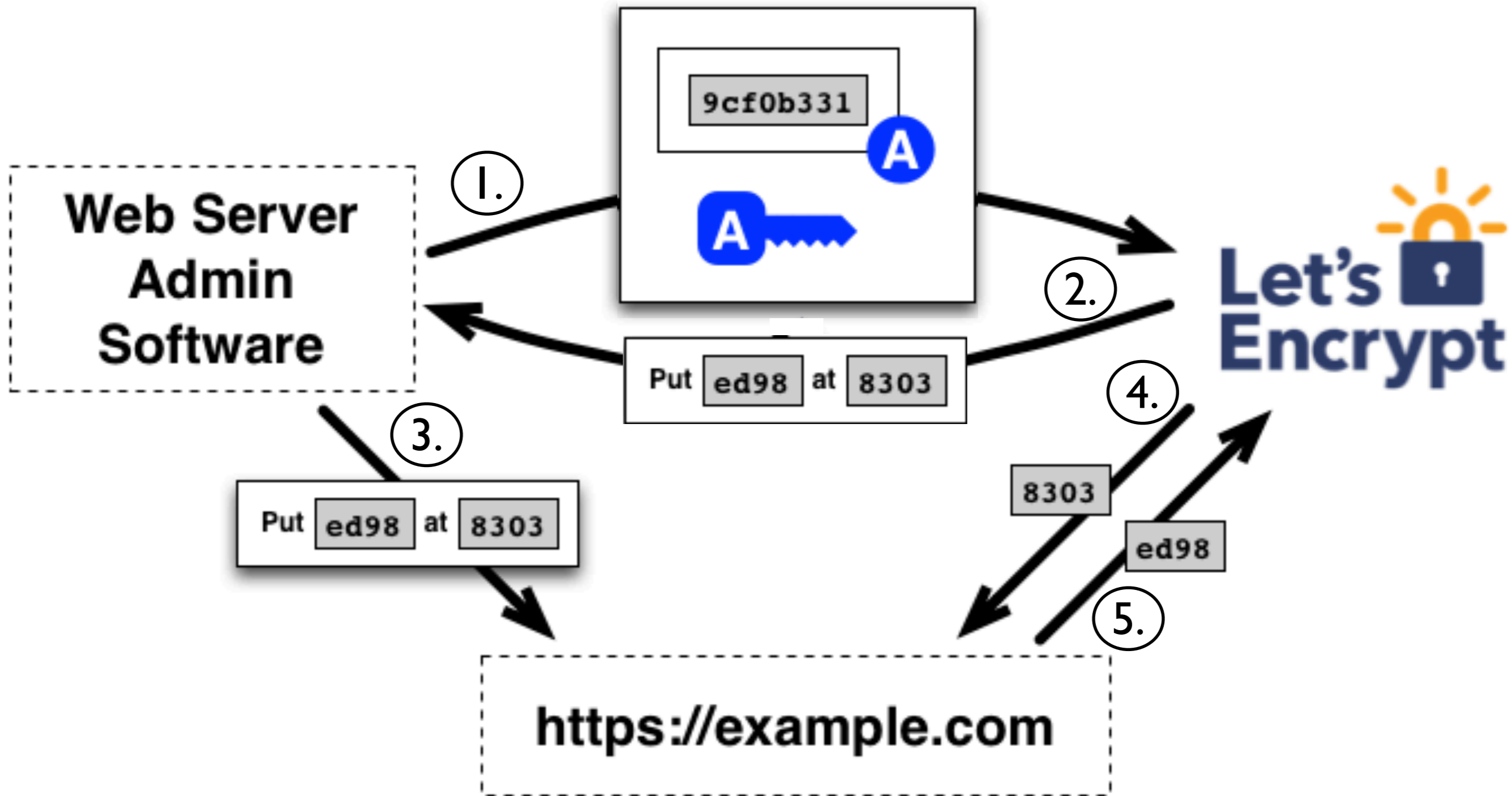


PKIs in Reality





**Let's
Encrypt**

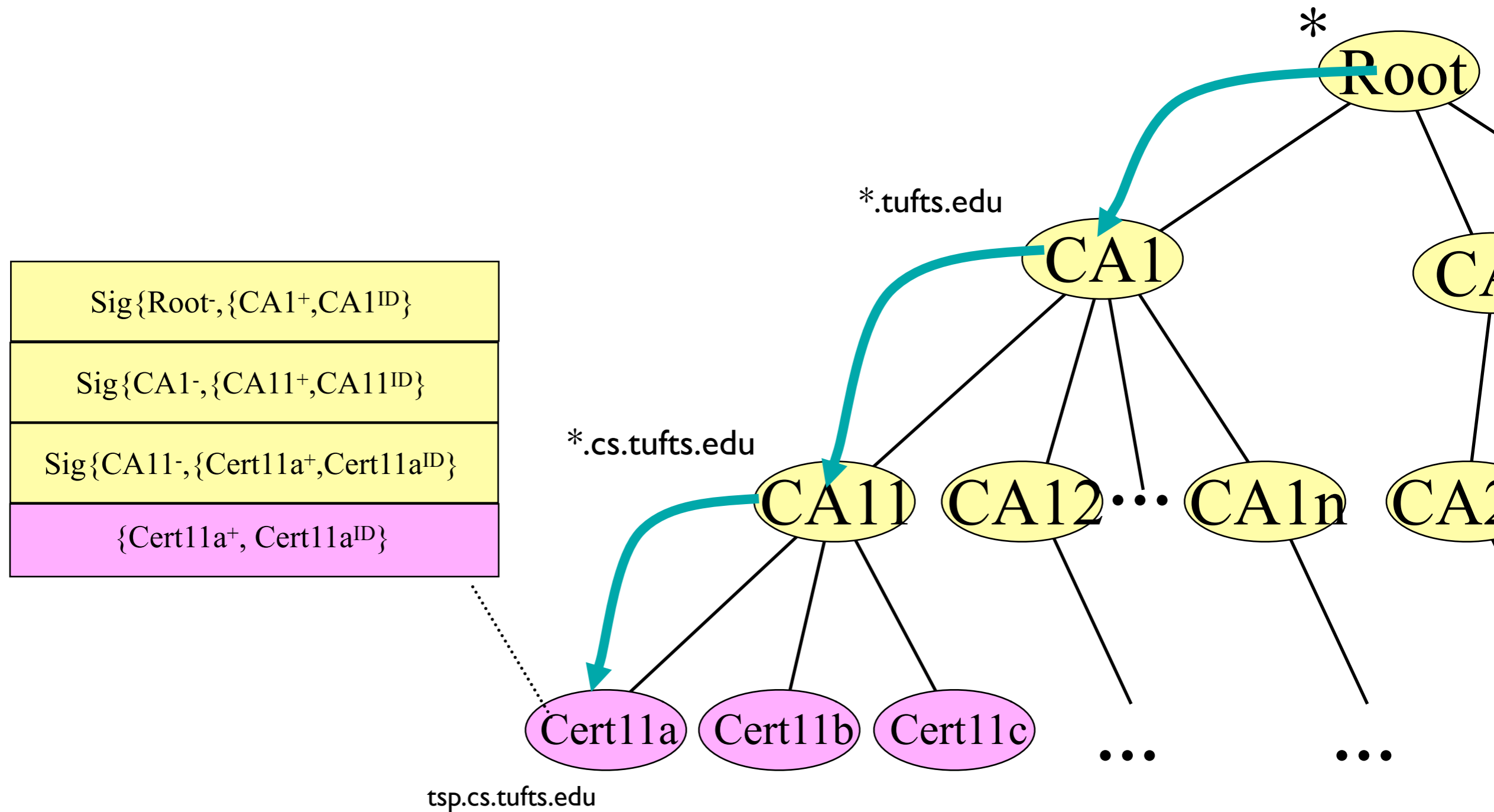


When PKI Goes Wrong!

PKI and Revocation

- Certificate may be revoked before expiration
 - Lost private key
 - Compromised
 - Owner no longer authorized
- Revocation is hard ...
 - Verifiers need to check revocation state
 - Loses the advantage of off-line verification
 - Revocation state must be authenticated

Certificate Validation



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60% not revoked

20% 2yr+ TTL

"Analysis of SSL Certificate Reissues and Revocations in the Wake of Heartbleed", Zhang et. al., IMC '14

- Any CA may sign any certificate
- Browser weighs all root CAs equally
- *Q: Is this problematic?*

The DigiNotar Incident

The screenshot shows the DigiNotar website homepage. The browser address bar displays 'www.diginotar.com'. The website header includes the DigiNotar logo (A VASCO COMPANY) and a navigation menu with links for HOME, ANNOUNCEMENTS, PRODUCTS, BRANCH SOLUTIONS, ABOUT DIGINOTAR, PARTNERS, and PROJECTS. A search bar is located in the top right of the header. The main banner features a woman looking at a laptop with the text: 'Know for sure with whom you have an agreement. How do you check the identity of someone who's doing business online?'. Below the banner is a navigation bar with links for EV SSL, Contact, and FAQ. The main content area is divided into three columns: 'Go to ...' with links for Managed PKI, SSL Certificates, SIM-ID, Signing Service, and DocProof; 'DigiNotar®, Internet Trust Provider' with a description of their services and a 'More information >>' link; and 'Announcements' with three recent news items: 'Publication report Fox-IT', 'Cooperation Dutch government', and 'DigiNotar reports security incident'. At the bottom, there is a 'GO EV SSL BUY NOW' graphic and the VASCO logo (A VASCO COMPANY).

DigiNotar Incident

DigiNotar is a CA based in the Netherlands that is (well, was) trusted by most OSes and browsers

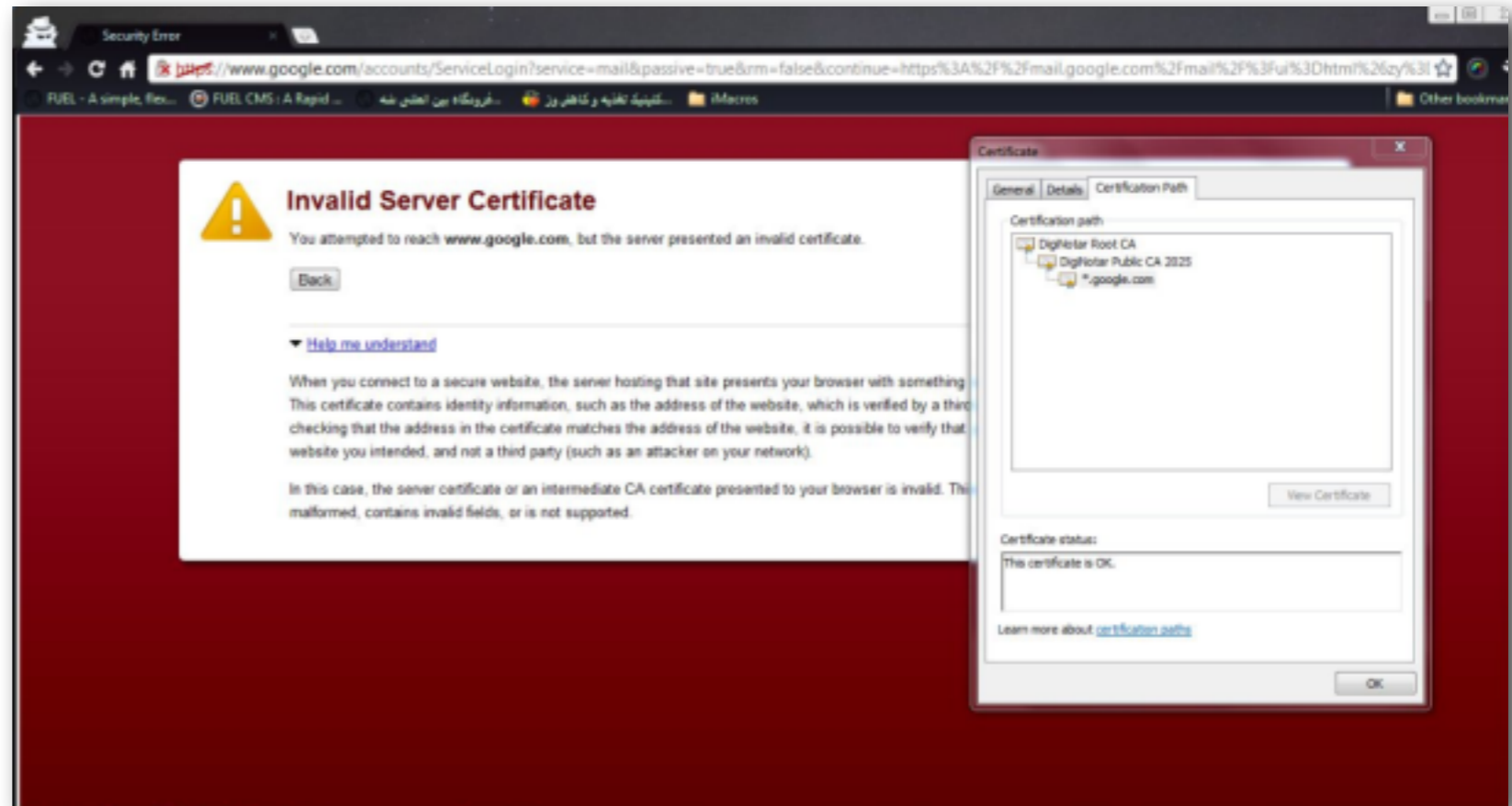
July 2011: Issued fake certificate for gmail.com to site in Iran that ran MitM attack...

... this fooled most browsers, but...



DigiNotar Incident

- As added security measure, Google Chrome hardcodes fingerprint of Google's certificate
- Since DigiNotar didn't issue Google's true certificate, this caused an error message in Chrome



Meta-Issue:
How much should we trust CAs?

(Because right now, we trust them a lot.)

Key Management Summary

- Key management is HARD
- PKI is not a panacea
- Devil is in the details