

HW 6: due Tues, November 15

- Find the maximum weight matching in a complete bipartite graph with the following adjacency matrix (rows represent vertices in X, columns vertices in Y), using the primal/dual algorithm to output both the matching and a proof that it is max weight.

$$\begin{vmatrix} 7 & 8 & 9 & 1 & 6 \\ 8 & 2 & 1 & 5 & 7 \\ 9 & 1 & 0 & 3 & 2 \\ 4 & 5 & 9 & 5 & 8 \\ 6 & 5 & 2 & 8 & 4 \end{vmatrix}$$

- The *bottleneck matching problem* is the following: given a graph $G = (V, E)$, and a *weight* $w : E \rightarrow \mathbb{Z}^+$, find a perfect matching M such that $\max_{e \in M} w(e)$ is as small as possible. Give a polynomial time algorithm for bottleneck matching.
- The *bin packing* problem is the following: We are given n objects of size $\{c_1, \dots, c_n\}$ and another integer B – the *bin capacity* and we are asked to find an assignment of these objects to bins such that the sum of all the sizes of the objects in each bin does not exceed B , and there are *as few bins as possible*. Show that in the special case that the sizes ALL satisfy $c_j > B/3$, then bin-packing can be reformulated as a matching problem. Then solve it in a much easier way.