

COMP 181

Lecture 5 Parsing

September 19, 2006



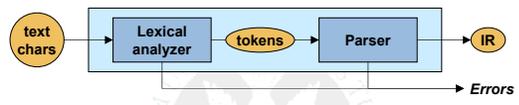

Prelude




- Microprocessor news:
 - Semiconductor with lasers
 - So what?
- Chip-to-chip communication is costly
 - **On chip**: registers, L1 and L2 cache – 1 to 8 cycles
 - **Off chip**: main memory – up to 150 cycles
- What's so great about optical communication?
 - Speed of light
 - No grounding, crosstalk, resistance, capacitance, etc.
 - Wave division multiplexing
 - 2.6 terabits/sec – equivalent to 30 million phone calls

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Where are we?

- Lexical analyzer
 - Reads characters one at a time
 - Produces a stream of tokens
 <kind, value>
- Automatically generated...

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Building a lexer

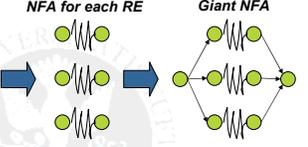


Specification

```

"if"
"while"
[a-zA-Z][a-zA-Z0-9]*
[0-9][0-9]*
(
)
...

```



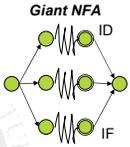
- Language: `if | while | [a-zA-Z][a-zA-Z0-9]* | [0-9][0-9]* ...`
- **Problem**:
 - Giant NFA either accepts or rejects a one token
 - We need to **partition** a string, and indicate the kind

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Partitioning



- **Input**: stream of characters
 $x_0, x_1, x_2, x_3, \dots, x_n$



- Annotate the NFA
 - Remember the accepting state of each RE
 - Annotate with the kind of token
- Does giant NFA accept some substring $x_0 \dots x_i$?
 - Return substring and kind of token
 - Restart the NFA at x_{i+1}

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Partitioning problems



- Matching is ambiguous
 - **Example**: `"εoo+3"`
 - We want `<foo>, <+>, <3>`
 - But: `<f>, <oo>, <+>, <3>` also works with our NFA
 - Can end the identifier anywhere
 - Note: "foo+" does not satisfy NFA
- Solution: **"maximal munch"**
 - Choose the longest substring that is accepted
 - Must look at the next character to decide -- **lookahead**
 - Keep munching until no transition on lookahead

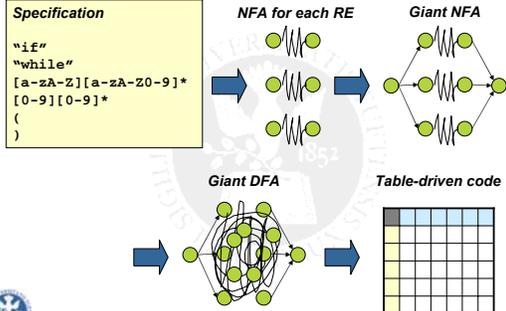
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More problems

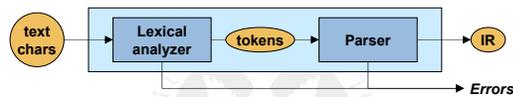
- Some strings satisfy multiple REs
 - Example:** "new foo"
 - <new> could be an identifier or a keyword
- Solution:** rank the REs
 - First, use maximal munch
 - Second, if substring satisfies two REs, choose the one with higher rank
 - Order is important in the specification
 - Put keywords first!



Building a lexer



Next step



- Parsing:** Organize tokens into "sentences"
 - Do tokens conform to language *syntax*?
 - Good news:** token types are just numbers
 - Bad news:** language syntax is fundamentally more complex than lexical specification
 - Good news:** we can still do it in linear time in most cases



Parsing introduction

- Is the following sentence grammatically correct:

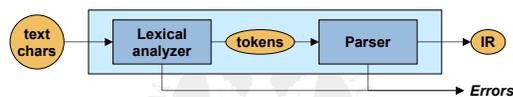
The horse ran past the barn fell

- Why?
 - We can use run as a transitive verb
 - I ran the horse past the barn
 - The horse that was ran past the barn
 - Structure
 - Subject: the horse ran past the barn
 - Verb: fell

Hopefully, parsing programming languages won't be this hard!



Parsing



- Parser**
 - Reads tokens from the scanner
 - Checks organization of tokens against a *grammar*
 - Constructs a *derivation*
 - Derivation drives construction of IR



Study of parsing

- Discovering the derivation of a sentence
 - "Diagramming a sentence" in grade school
 - Formalization:
 - Mathematical model of syntax – a grammar G
 - Algorithm for testing membership in L(G)
- Roadmap:
 - Context-free grammars
 - Top-down parsers
 - Ad hoc, often hand-coded, recursive decent parsers*
 - Bottom-up parsers
 - Automatically generated LR parsers*



Specifying syntax with a grammar

- Limitations of regular expressions
 - Later in lecture, and in homework (*yes, homework*)
 - Need something more powerful
 - Still want formal specification (*for automation*)
- Context-free grammar
 - Set of rules for generating sentences
 - Expressed in Backus-Naur form (BNF)



Context-free grammar

- Example:

#	Production rule
1	sheepnoise \rightarrow sheepnoise baa
2	baa

“produces” or “generates”

Alternative (shorthand)
- Formally: **context-free grammar** is
 - $G = (s, N, T, P)$
 - T : set of terminals (*provided by scanner*)
 - N : set of non-terminals (*represent structure*)
 - $s \in N$: start or goal symbol
 - $P : N \rightarrow (N \cup T)^*$: set of production rules



Language L(G)

- Language L(G)

$L(G)$ is all sentences generated from start symbol
- Generating sentences
 - Use productions as **rewrite rules**
 - Start with goal (or start) symbol – a non-terminal
 - Choose a non-terminal and “expand” it to the right-hand side of one of its productions
 - Only terminal symbols left \rightarrow sentence in L(G)
 - Intermediate results known as **sentential forms**



Examples

- Grammar:

#	Production rule
1	sheepnoise \rightarrow sheepnoise baa
2	baa
- | Rule | Sentential form |
|------|-----------------|
| - | sheepnoise |
| 2 | baa |

Rule	Sentential form
-	sheepnoise
1	sheepnoise baa
1	sheepnoise baa baa
2	baa baa baa
- | Rule | Sentential form |
|------|-----------------|
| - | sheepnoise |
| 1 | sheepnoise baa |
| 2 | baa baa |

Sheep noises aren't that interesting for compilers...



Better example

- Language of expressions
 - Numbers and identifiers
 - Allow different binary operators
 - Arbitrary nesting of expressions

#	Production rule
1	expr \rightarrow expr op expr
2	number
3	identifier
4	op \rightarrow +
5	-
6	*
7	/

Expressions can consist of other expressions connected by operators

Numbers and identifiers can fill in any of the positions in the overall expression



Language of expressions

- What's in this language?

#	Production rule	Rule	Sentential form
1	expr \rightarrow expr op expr	-	expr
2	number	1	expr op expr
3	identifier	3	<id,x> op expr
4	op \rightarrow +	5	<id,x> - expr
5	-	1	<id,x> - expr op expr
6	*	2	<id,x> - <num,2> op expr
7	/	6	<id,x> - <num,2> * expr
		3	<id,x> - <num,2> * <id,y>

\rightarrow We can build the string “x - 2 * y”
This string is in the language



Derivations

- Using grammars
 - A sequence of rewrites is called a *derivation*
 - Discovering a derivation for a string is *parsing*
- Different derivations are possible
 - At each step we can choose any non-terminal
 - Rightmost derivation:** always choose right NT
 - Leftmost derivation:** always choose left NT
 - (Other "random" derivations – not of interest)



Left vs right derivations

- Two derivations of " $x - 2 * y$ "

Rule	Sentential form
-	<i>expr</i>
1	<i>expr op expr</i>
3	<i><id, x> op expr</i>
5	<i><id, x> - expr</i>
1	<i><id, x> - expr op expr</i>
2	<i><id, x> - <num, 2> op expr</i>
6	<i><id, x> - <num, 2> * expr</i>
3	<i><id, x> - <num, 2> * <id, y></i>

Left-most derivation

Rule	Sentential form
-	<i>expr</i>
1	<i>expr op expr</i>
3	<i>expr op <id, y></i>
6	<i>expr * <id, y></i>
1	<i>expr op expr * <id, y></i>
2	<i>expr op <num, 2> * <id, y></i>
5	<i>expr - <num, 2> * <id, y></i>
3	<i><id, x> - <num, 2> * <id, y></i>

Right-most derivation



Derivations and parse trees

- Two different derivations
 - Both are correct
 - Do we care which one we use?
 - Represent derivation as a *parse tree*
 - Leaves are terminal symbols
 - Inner nodes are non-terminals
 - To depict production $\alpha \rightarrow \beta \gamma \delta$ show nodes β, γ, δ as children of α
- ➡ Tree is used to build internal representation

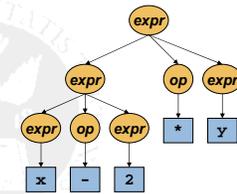


Example (I)

Right-most derivation

Rule	Sentential form
-	<i>expr</i>
1	<i>expr op expr</i>
3	<i>expr op <id, y></i>
6	<i>expr * <id, y></i>
1	<i>expr op expr * <id, y></i>
2	<i>expr op <num, 2> * <id, y></i>
5	<i>expr - <num, 2> * <id, y></i>
3	<i><id, x> - <num, 2> * <id, y></i>

Parse tree



- Problem:** evaluates as $(x - 2) * y$

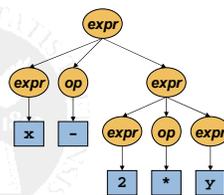


Example (I)

Left-most derivation

Rule	Sentential form
-	<i>expr</i>
1	<i>expr op expr</i>
3	<i><id, x> op expr</i>
5	<i><id, x> - expr</i>
1	<i><id, x> - expr op expr</i>
2	<i><id, x> - <num, 2> op expr</i>
6	<i><id, x> - <num, 2> * expr</i>
3	<i><id, x> - <num, 2> * <id, y></i>

Parse tree



- Solution:** evaluates as $x - (2 * y)$



Derivations and precedence

- Problem:**
 - Two different valid derivations
 - Shape of tree implies its meaning
 - One captures semantics we want – *precedence*
- Can we express precedence in grammar?
 - Notice: operations deeper in tree evaluated first
 - Idea:** add an intermediate production
 - New production isolates different levels of precedence
 - Force higher precedence "deeper" in the grammar



Adding precedence

- Two levels:

Level 1: lower precedence – higher in the tree

Level 2: higher precedence – deeper in the tree

- Observations:

- Larger: requires more rewriting to reach terminals
- Produces same parse tree under both left and right derivations

#	Production rule
1	$expr \rightarrow expr + term$
2	$ expr - term$
3	$ term$
4	$term \rightarrow term * factor$
5	$ term / factor$
6	$ factor$
7	$factor \rightarrow \underline{number}$
8	$ \underline{identifier}$

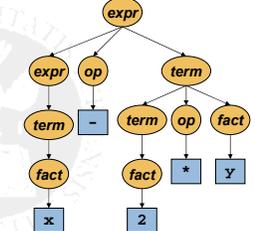


Expression example

Right-most derivation

Parse tree

Rule	Sentential form
-	$expr$
2	$expr - term$
4	$expr - term * factor$
8	$expr - term * <id,y>$
6	$expr - factor * <id,y>$
7	$expr - <num,2> * <id,y>$
3	$term - <num,2> * <id,y>$
6	$factor - <num,2> * <id,y>$
8	$<id,x> - <num,2> * <id,y>$



Now right derivation yields $x - (2 * y)$



Typical patterns

- One or more:

#	Production rule
1	$list \rightarrow element list$
2	$ element$

- Zero or more:

#	Production rule
1	$list \rightarrow element list$
2	$ $

- Comma separated list:

#	Production rule
1	$list \rightarrow element , list$
2	$ element$



C expressions

```
primary.expression: /* P */ /* 6.3.1 EXTENDED */
| constant
| string.literal.list
| '(' expression ')'
;

postfix.expression: /* P */ /* 6.3.2 CLARIFICATION */
| primary.expression
| postfix.expression '[' expression ']'
| postfix.expression '(' ')'
| postfix.expression '(' argument.expression.list ')'
| postfix.expression '.' identifier
| postfix.expression ctokARROW identifier
| postfix.expression ctokICR
| postfix.expression ctokDECR
;
```



C expressions

```
argument.expression.list: /* P */ /* 6.3.2 */
| assignment.expression
| argument.expression.list ',' assignment.expression
;

unary.expression: /* P */ /* 6.3.3 */
| postfix.expression
| ctokICR unary.expression
| ctokDECR unary.expression
| unary.operator cast.expression
| ctokSIZEOF unary.expression
| ctoksizeof '(' type.name ')'
;

unary.operator: /* P */ /* 6.3.3 */
| '&' | '*' | '+' | '-' | '~' | '-' | '!'
;
```



C expressions

```
cast.expression: /* P */ /* 6.3.4 */
| '(' type.name ')' cast.expression
;

multiplicative.expression: /* P */ /* 6.3.5 */
| cast.expression
| multiplicative.expression '*' cast.expression
| multiplicative.expression '/' cast.expression
| multiplicative.expression '%' cast.expression
;

additive.expression: /* P */ /* 6.3.6 */
| multiplicative.expression
| additive.expression '+' multiplicative.expression
| additive.expression '-' multiplicative.expression
;
```



C expressions

```

shift.expression: /* P */ /* 6.3.7 */
  additive.expression
  | shift.expression ctokLS additive.expression
  | shift.expression ctokRS additive.expression
  ;

relational.expression: /* P */ /* 6.3.8 */
  shift.expression
  | relational.expression '<' shift.expression
  | relational.expression '>' shift.expression
  | relational.expression ctokLE shift.expression
  | relational.expression ctokGE shift.expression
  ;

equality.expression: /* P */ /* 6.3.9 */
  relational.expression
  | equality.expression ctokEQ relational.expression
  | equality.expression ctokNE relational.expression
  ;

```



C expressions

```

AND.expression: /* P */ /* 6.3.10 */
  equality.expression
  | AND.expression '&' equality.expression
  ;

inclusive.OR.expression: /* P */ /* 6.3.12 */
  exclusive.OR.expression
  | inclusive.OR.expression '|' exclusive.OR.expression
  ;

logical.AND.expression: /* P */ /* 6.3.13 */
  inclusive.OR.expression
  | logical.AND.expression ctokANDAND inclusive.OR.expression
  ;

logical.OR.expression: /* P */ /* 6.3.14 */
  logical.AND.expression
  | logical.OR.expression ctokOROR logical.AND.expression
  ;

```



C expressions

```

conditional.expression: /* P */ /* 6.3.15 */
  logical.OR.expression
  | logical.OR.expression '?' expression ':' conditional.expression
  ;

assignment.expression: /* P */ /* 6.3.16 */
  conditional.expression
  | unary.expression assignment.operator assignment.expression
  ;

expression: /* P */ /* 6.3.17 */
  assignment.expression
  | expression ',' assignment.expression
  ;

```



Error productions

- How to provide useful error information?
- Idea:** add productions for common errors

#	Production rule
1	$expr \rightarrow expr\ op\ expr$
2	<u>number</u>
3	<u>identifier</u>
4	$expr\ op\ error$

- Special "error" token – used in yacc/bison
- Emit message:
 - "binary operation missing operand"



Ambiguity

- Original example has another problem:

#	Production rule	Rule	Sentential form
1	$expr \rightarrow expr\ op\ expr$	-	$expr$
2	<u>number</u>	1	$expr\ op\ expr$
3	<u>identifier</u>	1	$expr\ op\ expr\ op\ expr$
4	$op \rightarrow +$	3	$\langle id, x \rangle\ op\ expr\ op\ expr$
5	-	5	$\langle id, x \rangle\ -\ expr\ op\ expr$
6	*	2	$\langle id, x \rangle\ -\ \langle num, 2 \rangle\ op\ expr$
7	/	6	$\langle id, x \rangle\ -\ \langle num, 2 \rangle\ *\ expr$
		3	$\langle id, x \rangle\ -\ \langle num, 2 \rangle\ *\ \langle id, y \rangle$

- Multiple leftmost derivations – hard to automate
- Such a grammar is called **ambiguous**



Ambiguous grammars

- A grammar is ambiguous *iff*:
 - There are multiple leftmost or multiple rightmost derivations for a single sentential form
 - Note:** leftmost and rightmost derivations may differ, even in an unambiguous grammar
 - Intuitively:**
 - We can choose different non-terminals to expand
 - But each non-terminal should lead to a unique set of terminal symbols
- Classic example: if-then-else ambiguity



If-then-else

- Grammar:

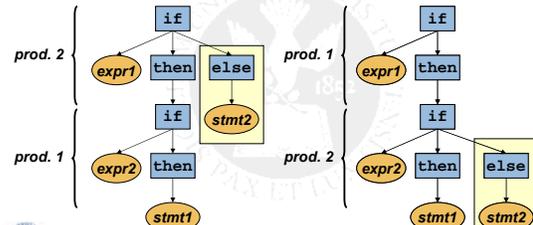
#	Production rule
1	$stmt \rightarrow \underline{if} \ expr \ \underline{then} \ stmt$
2	$\quad \quad \quad \ \underline{if} \ expr \ \underline{then} \ stmt \ \underline{else} \ stmt$
3	$\quad \quad \quad \ \dots other \ statements \dots$

- Problem:** nested if-then-else statements
 - Each one may or may not have `else`
 - How to match each `else` with `if`



If-then-else ambiguity

- Sentential form with two derivations:
 $if \ expr1 \ then \ if \ expr2 \ then \ stmt1 \ else \ stmt2$



Removing ambiguity

- Restrict the grammar
 - Choose a rule: "else" matches innermost "if"
 - Codify with new productions

#	Production rule
1	$stmt \rightarrow \underline{if} \ expr \ \underline{then} \ stmt$
2	$\quad \quad \quad \ \underline{if} \ expr \ \underline{then} \ \underline{withelse} \ \underline{else} \ stmt$
3	$\quad \quad \quad \ \dots other \ statements \dots$
4	$\underline{withelse} \rightarrow \underline{if} \ expr \ \underline{then} \ \underline{withelse} \ \underline{else} \ \underline{withelse}$
5	$\quad \quad \quad \ \dots other \ statements \dots$

- Intuition:** when we have an "else", all preceding nested conditions must have an "else"



Ambiguity

- Ambiguity can take different forms
 - Grammatical ambiguity (*if-then-else problem*)
 - Contextual ambiguity
 - In C: `x * y;` could follow `typedef int x;`
 - In Fortran: `x = f(y);` `f` could be function or array
- Cannot be solved directly in grammar
 - Issues of **type** (later in course)
- Deeper question:
How much can the parser do?



Scanning vs parsing

- Consider the language of just matching parentheses:

<code>()</code>	legal
<code>(())</code>	legal
<code>(((</code>	illegal
<code>()(())(())</code>	legal

- Can this language be expressed as a regular expression?
 - Answer: no
 - Intuitively: regular languages only expand "at the end"
 - Formally: use **pumping lemma**



Regular vs context-free

- Using a context-free grammar

#	Production rule
1	$\underline{parens} \rightarrow \underline{parens} \ (\ \underline{parens} \)$
2	$\quad \quad \quad \ \epsilon$

- Difference in power:
 - Context-free grammars solve problem
Intuitively: allow expansion "in the middle"
 - Regular grammars: less powerful
 Only allow productions of the form $\alpha \rightarrow \underline{x} \beta$



Regular languages

- Still good for scanning
 - Efficiency (overhead, not asymptotic)
 - Comments, white space

#	Production rule
1	$expr \rightarrow comm\ expr\ op\ comm\ expr$
2	$ \underline{number}\ comm$
3	$ \underline{identifier}\ comm$
...
8	$comm \rightarrow /*\ text\ */$
9	$ $

- Yuck! And hard to get right



Beyond context-free?

- Is there a context-free grammar for:

$$a^n b^n c^n$$
 - Must have same number of a's, b's, and c's

- No

Intuitively: need to expand in two places

- Slightly surprising:

$$a^n b^m c^{m+n}$$

is a context-free language

#	Production rule
1	$S \rightarrow aS\underline{c}$
2	$ B$
3	$B \rightarrow \underline{b}B\underline{c}$
4	$ \epsilon$



Big picture

- Scanners
 - Based on regular expressions
 - Efficient for recognizing token types
 - Remove comments, white space
 - Cannot handle complex structure
- Parsers
 - Based on context-free grammars
 - More powerful than REs, but still have limitations
 - Less efficient
- Type and semantic analysis
 - Based on attribute grammars and type systems
 - Handles "context-sensitive" constructs



Roadmap

- So far...
 - Context-free grammars, precedence, ambiguity
 - Derivation of strings
- Parsing:
 - Start with string, discover the derivation
 - Two major approaches
 - Top-down – start at the top, work towards terminals
 - Bottom-up – start at terminals, assemble into tree



Next time...

- Today: homework on lexers
 - Posted on the web-page
 - Due September 26 (one week)
- Top-down parsers

