



Linear vs. Logistic Regression for Classification Purposes

| Linear Regression  | Logistic Regression  |
|--|--|
| A value $x \in \mathbb{R}$                                     | A value $0 \le x \le 1$                                      |
| A hard boundary between<br>classes on either side of a<br>line | Probability of belonging to a certain class                  |
| Tries to find line that<br>best <b>fits</b> to the data        | Tries to find separator that best <b>divides</b> the classes |

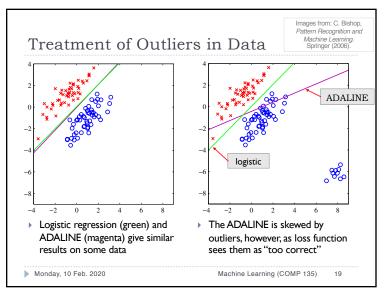
Monday, 10 Feb. 2020

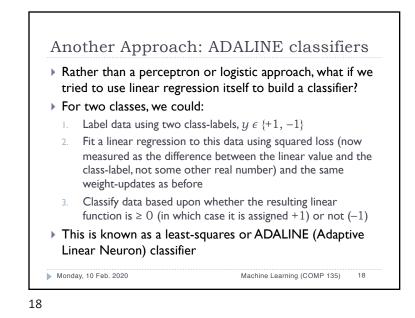
16

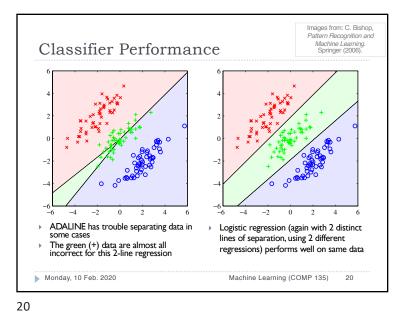
Machine Learning (COMP 135) 16

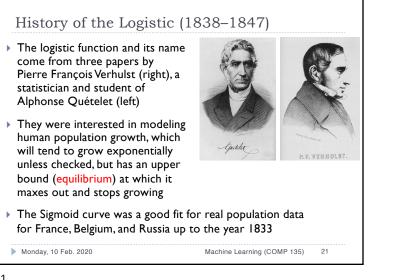
| Linear                 |   |
|------------------------|---|
| Lincal                 |   |
| Loss function          | $Loss(\mathbf{w}) = \sum_{j=1}^{N} (y_j - h_{\mathbf{w}}(\mathbf{x}_j))^2$  |
| Weight-update equation | $w_i \leftarrow w_i + \alpha \sum_j x_{j,i} \left( y_j - h_{\mathbf{w}}(\mathbf{x}_j) \right)$  |
| Logistic               |   |
| Loss function          | $-\frac{1}{N}\sum_{j=1}^{N}\left[y_{j}\log h_{\mathbf{w}}(\mathbf{x}_{j})+(1-y_{j})\log(1-h_{\mathbf{w}}(\mathbf{x}_{j}))\right]$                         |
| Weight-update equation | $w_j \leftarrow w_j + \alpha(y_j - h_{\mathbf{w}}(\mathbf{x}_j)) \\ \times h_{\mathbf{w}}(\mathbf{x}_j)(1 - h_{\mathbf{w}}(\mathbf{x}_j)) \times x_{i,j}$ |











## This Week Logistic regression; decision trees Readings: Book excerpts (online texts) Linked from class schedule Assignment 02: due Wednesday, 12 Feb. (9:00 AM) Office Hours: 237 Halligan Monday, 10:30 AM – Noon Tuesday, 9:00 AM – 10:30 AM

## History of the Logistic (20th C.) The logistic was re-discovered by Raymond Pearl (left) and Lowell Reed (right) in the 1920's > They later discovered Verhulst's earlier work, and credited him, but his logistic terminology didn't really catch on until the work of others, after WWII Pearl and collaborators went on to apply the logistic curve to models of human and fruit fly populations, as well as to the growth of cantaloupes In the 40's and 50's, statisticians working to model bioassay (effects of medicines and other substances on living tissues) popularized the use of the logistic and its name Due to computational conveniences, this became more popular than other models ► Monday, 10 Feb. 2020 Machine Learning (COMP 135) 22

22

6