

COMP 150-AVS

Fall 2018

OCaml and Functional Programming

Dialects of ML

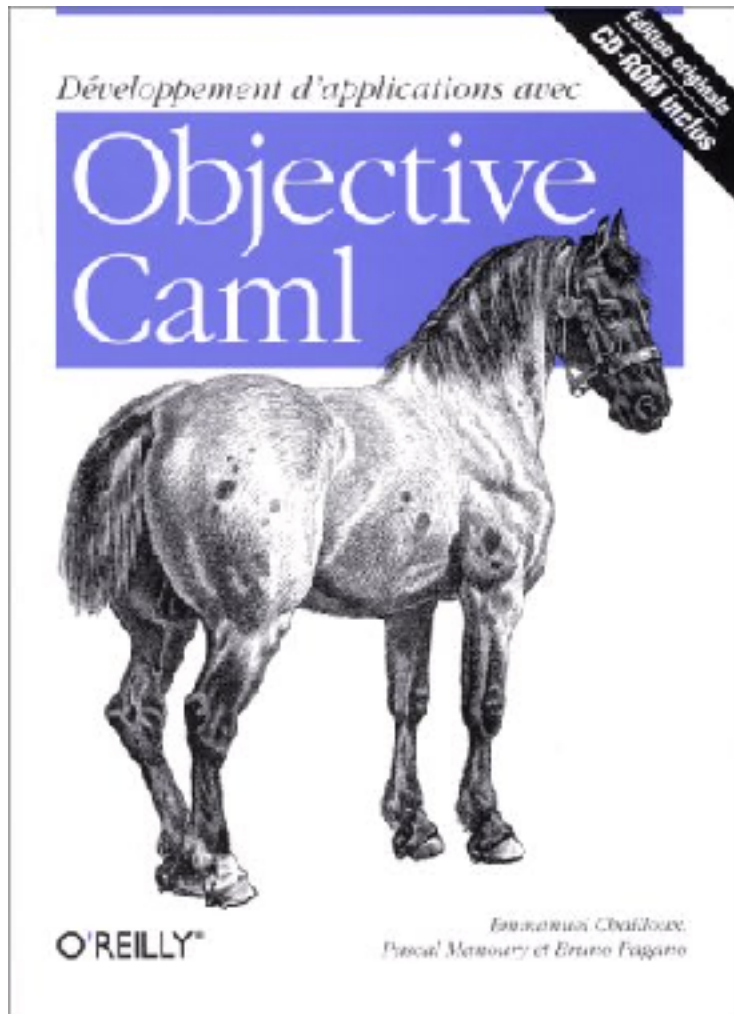
- ▶ ML (Meta Language)
 - Univ. of Edinburgh, 1973
 - Part of theorem-proving system LCF (Logic of Computable Functions)
- ▶ SML/NJ (Standard ML of New Jersey)
 - Bell Labs and Princeton, 1990
 - Now Yale, AT&T Research, Univ. of Chicago, etc...
- ▶ OCaml (Objective CAML)
 - INRIA, 1996
 - French Nat'l Institute for Research in Automation and Computer Science

Dialects of ML (cont.)

- ▶ Other dialects
 - MoscowML, ML Kit, Concurrent ML, etc...
 - SML/NJ and OCaml are most popular

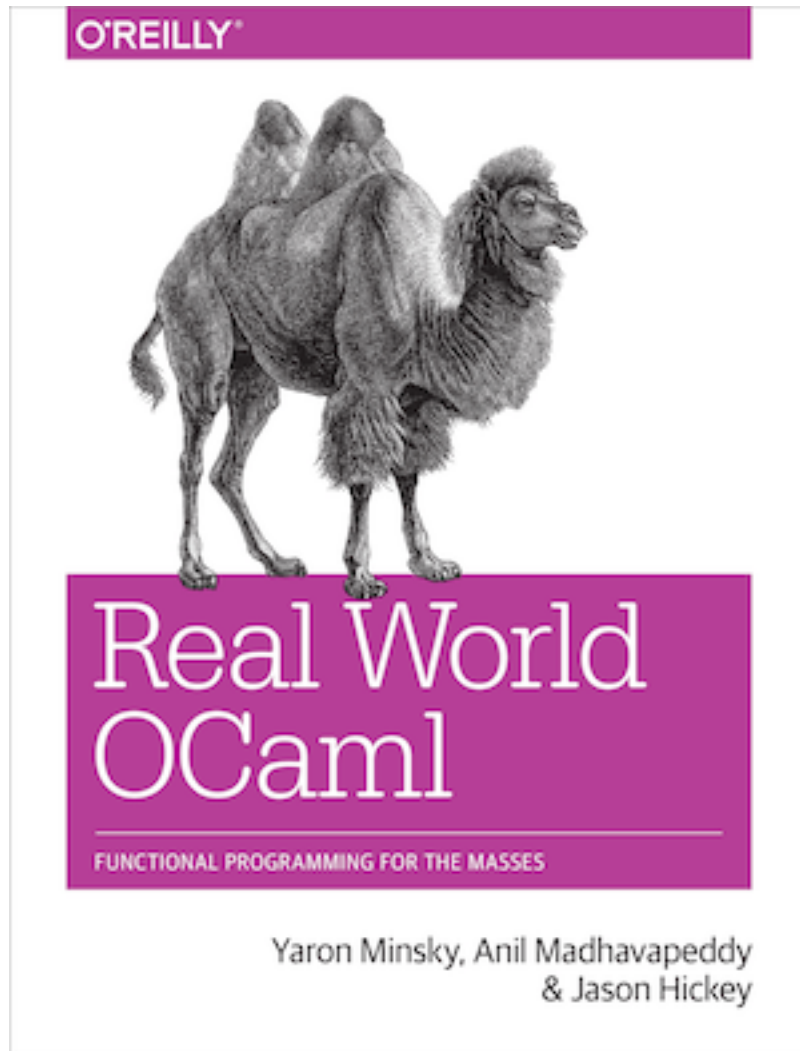
- ▶ Languages all have the same core ideas
 - But small and annoying syntactic differences
 - So you should not buy a book with ML in the title
 - Because it probably won't cover OCaml

Useful Information on OCaml language



- Translation available
 - *Developing Applications with Objective Caml*

More Information on OCaml



- Book designed to introduce **and advance** understanding of OCaml
 - Authors use OCaml in the real world
 - Introduces new libraries, tools
- Free HTML online
 - realworldocaml.org

Features of ML

- ▶ “Mostly functional”
 - Some assignments
- ▶ Higher-order functions
 - Functions can be parameters and return values
- ▶ Type inference
 - No need to write types in the source language
 - But the language is statically typed
 - Supports **parametric polymorphism**
 - *Generics* in Java, *templates* in C++

Features of ML (cont.)

- ▶ Data types and pattern matching
 - Convenient for certain kinds of data structures
- ▶ Exceptions
- ▶ Garbage collection

Functional Languages in the Real World

- **Java 8** 
- **F#, C# 3.0, LINQ**  Microsoft
- **Scala**   **Linked in** 
- **Haskell**    at&t
- **Erlang**    T-Mobile
- **OCaml**  **Bloomberg**  **CITRIX**
<https://ocaml.org/learn/companies.html>  Jane Street

Installing OCaml

- ▶ We will use version 4.07
- ▶ Recommend using opam
 - ▶ <https://opam.ocaml.org>
 - ▶ You might install ocaml using system package manager
- ▶ For project 1, also install **ounit** package

A Small OCaml Program – Things to Notice

Use `let`
to bind
variables

Use `(* *)` for comments (may nest)

No type declarations

Need to use
correct print
function (OCaml
also has `printf`)

```
(* Small OCaml program *)  
let x = 37;;  
let y = x + 5;;  
print_int y;;  
print_string  
  "\n";;
```

Line breaks, spacing
ignored (like C, C++,
Java, not like Ruby)

`::` ends a
top-level
expression

OCaml Interpreter

Expressions can be typed and evaluated at the top-level

```
# 3 + 4;;  
- : int = 7  
  
# let x = 37;;  
val x : int = 37  
  
# x;;  
- : int = 37  
  
# let y = 5;;  
val y : int = 5  
  
# let z = 5 + x;;  
val z : int = 42  
  
# print_int z;;  
42- : unit = ()  
  
# print_string "Colorless green ideas sleep furiously";;  
Colorless green ideas sleep furiously- : unit = ()  
  
# print_int "Colorless green ideas sleep furiously";;  
This expression has type string but is here used with type int
```

gives type and value of each expr

“-” = “the expression you just typed”

unit = “no interesting value” (like void)

OCaml Interpreter (cont.)

► Files can be loaded at top level

```
% ocaml
```

```
Objective Caml version 4.07.0
```

```
# #use "ocaml1.ml";;
```

```
val x : int = 37
```

```
val y : int = 42
```

```
42- : unit = ()
```

```
- : unit = ()
```

```
# x;;
```

```
- : int = 37
```

```
ocaml1.ml
```

```
(* Small OCaml program *)  
let x = 37;;  
let y = x + 5;;  
print_int y;;  
print_string "\n";;
```

 #use loads in a file one line at a time

OCaml Compiler

- OCaml programs can be compiled using `ocamlc`
 - Produces `.cmo` (“compiled object”) and `.cmi` (“compiled interface”) files
 - We’ll talk about interface files later
 - By default, also links to produce executable `a.out`
 - Use `-o` to set output file name
 - Use `-c` to compile only to `.cmo/.cmi` and not to link
- Can also compile with `ocamlopt`
 - Produces `.cmx` files, which contain native code
 - Faster, but not platform-independent (or as easily debugged)

OCaml Compiler

- Compiling and running the following small program:

hello.ml:

```
(* A small OCaml program *)  
print_string "Hello world!\n";;
```

```
% ocamlc hello.ml
```

```
% ./a.out
```

```
Hello world!
```

```
%
```

OCaml Compiler: Multiple Files

main.ml:

```
let main () =  
  print_int (Util.add 10 20);  
  print_string "\n"  
  
let () = main ()
```

util.ml:

```
let add x y = x+y
```

- Compile both together (produces a.out)
 `ocamlc util.ml main.ml`
- Or compile separately
 `ocamlc -c util.ml`
 `ocamlc util.cmo main.ml`
- To execute
 `./a.out`

OCamlbuild

- Use `ocamlbuild` to compile larger projects and automatically find dependencies
- Build a native or bytecode executable out of `main.ml` and its local dependencies

```
ocamlbuild main.byte
```

- The executable `main.byte` is in `_build` folder. To execute:

```
./main.byte
```


Basic Types in OCaml

- ▶ Read `e : t` as “expression `e` has type `t`”

`42 : int`

`true : bool`

`"hello" : string`

`'c' : char`

`3.14 : float`

`() : unit (* don't care value *)`

- ▶ OCaml has **static** types to help you avoid errors

- Note: Sometimes the messages are a bit confusing

```
# 1 + true;;
```

This expression has type `bool` but is here used with
type `int`

- Watch for the underline as a hint to what went wrong
- But not always reliable

The Let Construct

- ▶ **let** is often used for defining local variables
 - **let** $x = e1$ **in** $e2$ **means**
 - Evaluate $e1$
 - Then evaluate $e2$, with x bound to result of evaluating $e1$
 - x is *not* visible outside of $e2$

```
let pi = 3.14 in pi *. 3.0 *. 3.0;;  
pi;;
```

error

bind pi in
body of let

floating point
multiplication

The Let Construct (cont.)

- ▶ Compare to similar usage in Java/C

```
let pi = 3.14 in
  pi *. 3.0 *. 3.0;;
pi;;
```

```
{
  float pi = 3.14;
  pi * 3.0 * 3.0;
}
pi;
```

- ▶ In the top-level, omitting `in` means “from now on”
let pi = 3.14;;
(* pi is now bound in the rest of the top-level scope *)

::; versus ;

- ▶ ::; ends an expression in the top-level of OCaml
 - Use it to say: “Give me the value of this expression”
 - Not used in the body of a function
 - Not needed after each function definition
 - Though for now it won't hurt if used there
- ▶ e1; e2 evaluates e1 and then e2, and returns e2

```
let p (s,t) = print_int s; print_int t; "Done!"
```

- Notice no ; at end
- ; is a **separator**, not a **terminator**
- Invoking
 - Prints `p (1,2)`
 - Returns `"1 2"`
 - Returns `"Done!"`

Examples – Semicolon

▶ Definition

- $e1 ; e2$ (* evaluate $e1$, evaluate $e2$, return $e2$)

▶ $1 ; 2 ; ;$

- (* 2 – value of 2nd expression is returned *)

▶ $(1 + 2) ; 4 ; ;$

- (* 4 – value of 2nd expression is returned *)

▶ $1 + (2 ; 4) ; ;$

- (* 5 – value of 2nd expression is returned to $1 +$ *)

▶ $1 + 2 ; 4 ; ;$

- (* 4 – because $+$ has higher precedence than $;$ *)

Nested Let

- Uses of `let` can be nested

```
let pi = 3.14 in
let r = 3.0 in
    pi *. r *. r;;
(* pi, r no longer in scope *)
```

```
{
    float pi = 3.14;
    {
        float r = 3.0;
        pi * r * r;
    }
}
/* pi, r not in scope */
```

Defining Functions

Use `let` to
define
functions

List parameters
after function name

```
let next x = x + 1;;  
next 3;;  
let plus (x, y) = x + y;;  
plus (3, 4);;
```

No parentheses
on function calls

No return
statement

Local Variables

- ▶ You can use `let` inside of functions for locals

```
let area r =  
  let pi = 3.14 in  
  pi *. r *. r
```

- ▶ And you can use as many `lets` as you want

```
let area d =  
  let pi = 3.14 in  
  let r = d /. 2.0 in  
  pi *. r *. r
```


Lists in OCaml

- ▶ The basic data structure in OCaml is the **list**
 - Lists are written as `[e1; e2; ...; en]`
 - # `[1;2;3]`
 - : `int list = [1;2;3]`
 - Notice type of list is `int list`
 - Lists must be homogeneous

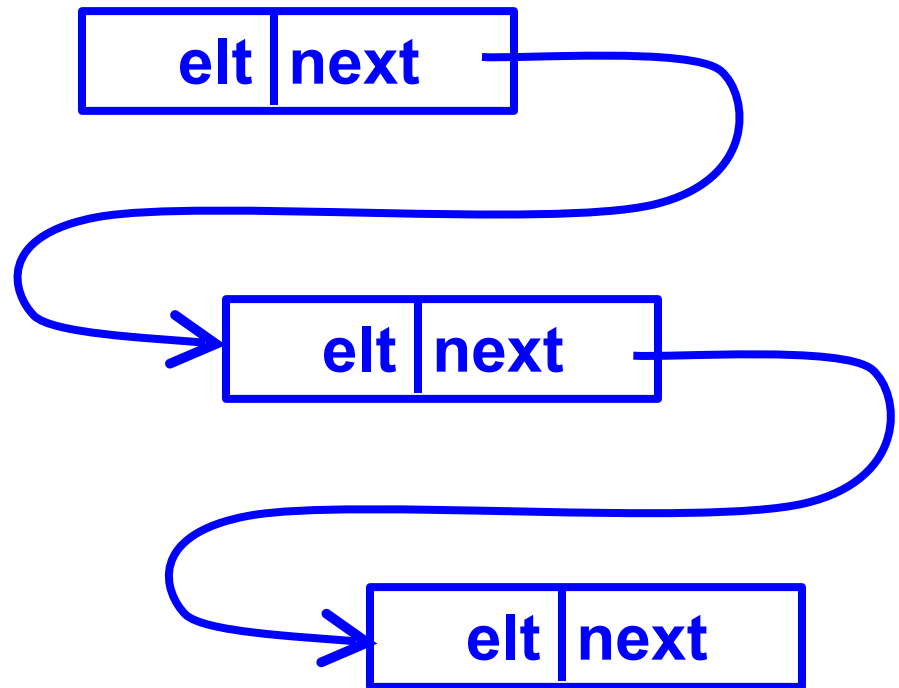
Lists in OCaml (cont.)

► More on OCaml lists

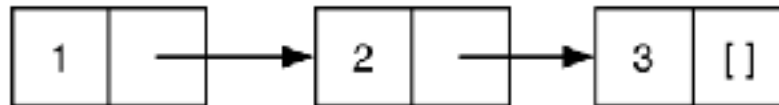
- The empty list is `[]`
 - # `[]`
 - : `'a list`
- The `'a` means “a list containing anything”
 - We'll find out more about this later
- List elements are separated using semicolons
- Warning: Don't use a comma instead of a semicolon
 - Means something different (we'll see in a bit)

Consider a Linked List in C

```
struct list {  
    int elt;  
    struct list *next;  
};  
...  
struct list *l;  
...  
i = 0;  
while (l != NULL) {  
    i++;  
    l = l->next;  
}
```

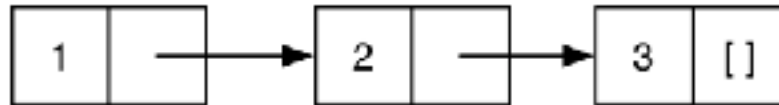


Lists in OCaml are Linked



- ▶ `[1;2;3]` is represented above
 - A nonempty list is a pair (element, rest of list)
 - The element is the **head** of the list
 - The pointer is the **tail** or **rest** of the list
 - ...which is itself a list!
- ▶ Thus in math a list is either
 - The empty list `[]`
 - Or a pair consisting of an element and a list
 - This recursive structure will come in handy shortly

Lists are Linked (cont.)



- ▶ `::` prepends an element to a list
 - `h::t` is the list with `h` as the element at the beginning and `t` as the “rest”
 - `::` is called a **constructor**, because it builds a list
 - Although not emphasized, `::` does allocate memory

▶ Examples

```
3::[ ]           (* The list [3] *)  
2::(3::[ ])     (* The list [2; 3] *)  
1::(2::(3::[ ])) (* The list [1; 2; 3] *)
```

More Examples

```
# let y = [1;2;3] ;;
val y : int list = [1; 2; 3]
# let x = 4::y ;;
val x : int list = [4; 1; 2; 3]
# let z = 5::y ;;
val z : int list = [5; 1; 2; 3]
```

➤ not modifying existing lists, just creating new lists

```
# let w = [1;2]::y ;;
```

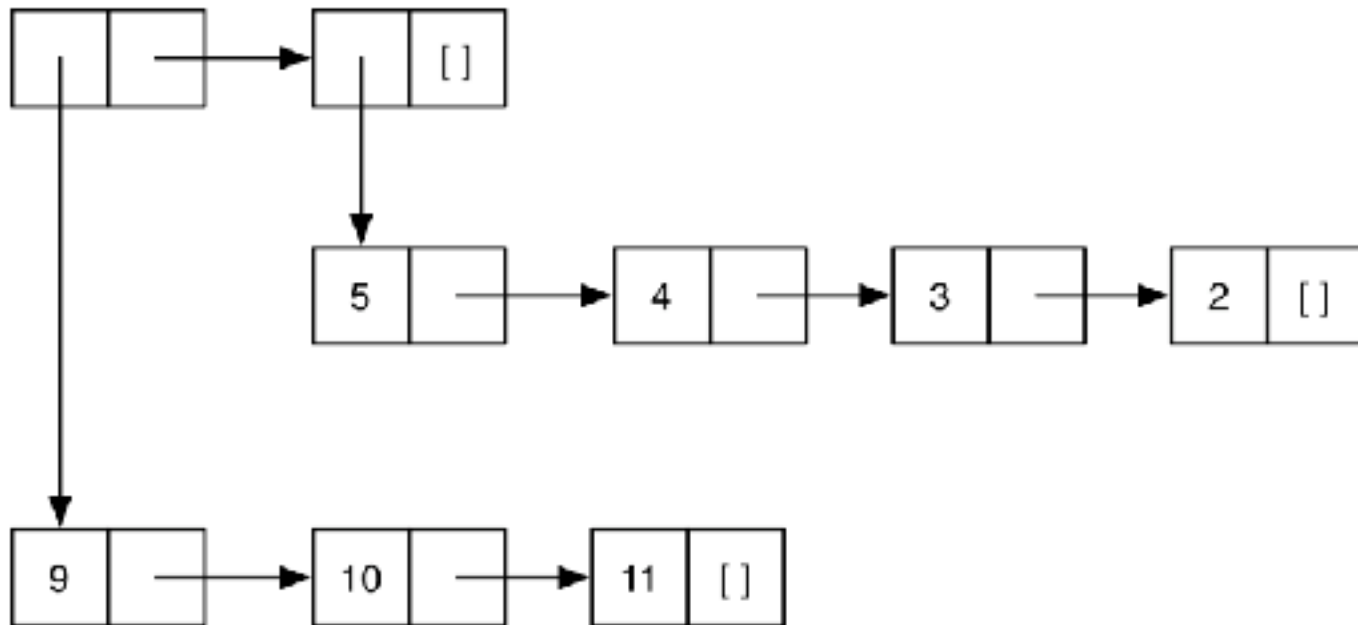
This expression has type **int list** but is here used with type **int list list**

- The left argument of `::` is an element
- Can you construct a list `y` such that `[1;2]::y` makes sense?

Lists of Lists

► Lists can be nested arbitrarily

- Example: `[[9; 10; 11]; [5; 4; 3; 2]]`
 - > Type = int list list



Practice

► What is the type of

- [1;2;3]

`int list`

- [[[]; []; [1.3;2.4]]]

`float list list list`

- let func x = x::(0::[])

`int -> int list`

Pattern Matching

- ▶ To pull lists apart, use the `match` construct
`match e with p1 -> e1 | ... | pn -> en`
- ▶ `p1...pn` are **patterns** made up of
 - `[]`, `::`, and **pattern variables**
- ▶ `match` finds the first `pk` that matches shape of `e`
 - Then `ek` is evaluated and returned
 - During evaluation of `pk`, pattern variables in `pk` are bound to the corresponding parts of `e`

Pattern Matching Example

► Match syntax

- `match e with p1 -> e1 | ... | pn -> en`

► Code 1

- `let is_empty l = match l with
 [] -> true
 | (h::t) -> false`

► Outputs

- `is_empty [] (* evaluates to true *)`
- `is_empty [1] (* evaluates to false *)`
- `is_empty [1;2] (* evaluates to false *)`

Pattern Matching Example (cont.)

▶ Code 2

- `let hd l = match l with (h::t) -> h`

▶ Outputs

- `hd [1;2;3] (* evaluates to 1 *)`
- `hd [1;2] (* evaluates to 1 *)`
- `hd [1] (* evaluates to 1 *)`
- `hd [] (* Exception: Match failure *)`

Pattern Matching Example (cont.)

▶ Code 3

- `let t1 l = match l with (h::t) -> t`

▶ Outputs

- `t1 [1;2;3] (* evaluates to [2;3] *)`
- `t1 [1;2] (* evaluates to [2] *)`
- `t1 [1] (* evaluates to [] *)`
- `t1 [] (* Exception: Match failure *)`

Pattern Matching – Wildcards

- ▶ An underscore `_` is a wildcard pattern
 - Matches anything
 - Doesn't add any bindings
 - Useful when you want to know something matches
 - But don't care what its value is

- ▶ In previous examples
 - Many values of `h` or `t` ignored
 - Can replace with wildcard `_`
 - Code behavior is identical

Pattern Matching – Wildcards (cont.)

▶ Code using `_`

- `let is_empty l = match l with
 [] -> true | (_ :: _) -> false`
- `let hd l = match l with (h :: _) -> h`
- `let tl l = match l with (_ :: t) -> t`

▶ Outputs

- `is_empty [1] (* evaluates to false *)`
- `is_empty [] (* evaluates to true *)`
- `hd [1;2;3] (* evaluates to 1 *)`
- `tl [1;2;3] (* evaluates to [2;3] *)`
- `hd [1] (* evaluates to 1 *)`
- `tl [1] (* evaluates to [] *)`

Pattern Matching – Missing Cases

- ▶ When pattern is defined
 - OCaml will warn you about non-exhaustive matches
- ▶ When pattern is used
 - Exceptions for inputs that don't match any pattern

▶ Example

```
# let hd l = match l with (h::_) -> h;;
```

```
Warning: this pattern-matching is not exhaustive.
```

```
Here is an example of a value that is not matched:
```

```
[]
```

```
# hd [];;
```

```
Exception: Match_failure ("", 1, 11).
```


Pattern Matching – An Abbreviation

- ▶ `let f p = e`, where `p` is a pattern
 - is shorthand for `let f x = match x with p -> e`
- ▶ Examples
 - `let hd (h::_) = h`
 - `let tl (_::t) = t`
 - `let f (x::y::_) = x + y`
 - `let g [x; y] = x + y`
- ▶ Useful if there's only one acceptable input

Pattern Matching – Lists of Lists

- ▶ Can pattern match on lists of lists as well
- ▶ Examples
 - `let addFirsts`
 $((x::_) :: (y::_) :: _) = x + y$
`addFirsts [[1;2];[4;5];[7;8;9]] = 5`
 - `let addFirstSecond`
 $(x::_) :: (_::y::_) :: _ = x + y$
`addFirstSecond [[1;2];[4;5];[7;8;9]] = 6`
- ▶ Note – you probably won't do this much or at all
 - You'll mostly write recursive functions over lists instead

OCaml Functions Take One Argument

- ▶ Recall this example

```
let plus (x, y) = x + y;;  
plus (3, 4);;
```

- It looks like you're passing in two arguments
- ▶ Actually, you're passing in a **tuple** instead

```
let plus t = match t with  
    (x, y) -> x + y;;  
plus (3, 4);;
```

- And using pattern matching to extract its contents

Tuples

- ▶ **Constructed** using `(e1, ..., en)`
- ▶ **Deconstructed** using pattern matching
- ▶ Tuples are like C structs
 - But without field labels
 - Allocated on the heap
- ▶ Tuples can be heterogenous
 - Unlike lists, which must be homogenous
 - `(1, ["string1"; "string2"])` is a valid tuple

Tuples – Examples

- ▶ `let plusThree (x, y, z) = x+y+z`
`let addOne (x, y, z) = (x+1, y+1, z+1)`
 - `plusThree (addOne (3,4,5)) = 15`
- ▶ `let sum ((a, b), c) = (a+c, b+c)`
 - `sum ((1, 2), 3) = (4,5)`
- ▶ `let plusFirstTwo (x::y::_ , a) = (x+a, y+a)`
 - `plusFirstTwo ([1; 2; 3], 4) = (5,6)`

Tuples – More Examples

- ▶ `let t1s (_::xs, _::ys) = (xs, ys)`
 - `t1s ([1;2;3], [4;5;6;7]) = ([2;3],[5;6;7])`
- ▶ Remember
 - Semicolon for lists
 - Comma for tuples
- ▶ Example
 - `[1, 2] = [(1, 2)]` = a list of size one
 - `(1; 2)` = a syntax error

Another Tuple Example

▶ Given

- `let f l = match l with x :: (_ :: y) -> (x, y)`

▶ What is the value of

- `f [1;2;3;4]`

List and Tuple Types

▶ Tuple types use `*` to separate components

▶ Examples

- `(1,2)` : `int * int`
- `(1,"string",3.5)` : `int * string * float`
- `(1,["a";"b"],'c')` : `int * string list * char`
- `[(1,2)]` : `(int * int) list`
- `[(1,2);(3,4)]` : `(int * int) list`
- `[(1,2);(1,2,3)]` : `error`

Polymorphic Functions

- ▶ Some functions require specific list types
 - `let plusFirstTwo (x::y::_, a) =
 (x + a, y + a)`
 - `plusFirstTwo :
 int list * int -> (int * int)`
- ▶ But other functions work for a list of any type
 - `let hd (h::_) = h`
 - `hd [1; 2; 3] (* returns 1 *)`
 - `hd ["a"; "b"; "c"] (* returns "a" *)`
- ▶ These functions are **polymorphic**

Polymorphic Types

► OCaml gives such functions **polymorphic** types

- `hd : 'a list -> 'a`

- Read as

- Function takes a list of any element type 'a
- And returns something of that type

► Example

- `let tl (_::t) = t`

- `tl : 'a list -> 'a list`

Polymorphic Types (cont.)

► More Examples

- `let swap (x, y) = (y, x)`
`swap : 'a * 'b -> 'b * 'a`

- `let tls (_::xs, _::ys) = (xs, ys)`
`tls : 'a list * 'b list ->`
`'a list * 'b list`

Tuples Are a Fixed Size

▶ This OCaml definition

- `# let foo x = match x with`
 `(a, b) -> a + b`
 | (a, b, c) -> a + b + c;;

▶ Would yield this error message

- This pattern matches values of type 'a * 'b * 'c
 but is here used to match values of type 'd * 'e

▶ Tuples of different size have different types

- Thus never more than one match case with tuples

Pattern matching is *AWESOME*

1. You can't forget a case
 - Compiler issues inexhaustive pattern-match warning
2. You can't duplicate a case
 - Compiler issues unused match case warning
3. You can't get an exception
 - Can't do something like `List.hd []`
4. Pattern matching leads to elegant, concise, beautiful code

OCaml Data

- ▶ So far, we've seen the following kinds of data
 - Basic types (int, float, char, string)
 - Lists
 - One kind of data structure
 - A list is either `[]` or `h::t`, deconstructed with pattern matching
 - Tuples
 - Let you collect data together in fixed-size pieces
 - Functions
- ▶ How can we build other data structures?
 - Building everything from lists and tuples is awkward

User Defined Types

- ▶ `type` can be used to create new names for types
 - Useful for combinations of lists and tuples
- ▶ Examples
 - `type my_type = int * (int list)`
`(3, [1; 2]) : my_type`
 - `type my_type2 = int * char * (int * float)`
`(3, 'a', (5, 3.0)) : my_type2`

Data Types

- ▶ **type** can also be used to create **variant types**
 - Equivalent to C-style unions

```
type shape =  
  Rect of float * float (* width * length *)  
  | Circle of float      (* radius *)
```

- ▶ **Rect** and **Circle** are **value constructors**
 - Here a **shape** is either a **Rect** or a **Circle**

Data Types (cont.)

```
let area s =  
  match s with  
    | Rect (w, l) -> w *. l  
    | Circle r -> r *. r *. 3.14  
  
area (Rect (3.0, 4.0))  
area (Circle 3.0)
```

- ▶ Use pattern matching to **deconstruct** values
 - **s** is a **shape**
 - Do different things for **s** depending on its constructor

Data Types (cont.)

```
type shape =  
  Rect of float * float (* width * length *)  
  | Circle of float      (* radius *)  
  
let l = [Rect (3.0, 4.0) ; Circle 3.0]
```

▶ What's the type of `l`?

shape list

▶ What's the type of `l`'s first element?

shape

Data Types Constructor

- ▶ Constructors must begin with uppercase letter
- ▶ The **arity** of a constructor
 - Is the number of arguments it takes
 - A constructor with no arguments is **nullary**

```
type optional_int =  
  None  
  | Some of int
```

- ▶ Example
 - Arity of **None** = 0
 - Arity of **Some** = 1

Polymorphic Data Types

```
type optional_int =
  None
  | Some of int
let add_with_default a = function
  None -> a + 42
  | Some n -> a + n
add_with_default 3 None           (* 45 *)
add_with_default 3 (Some 4)      (* 7  *)
```

- ▶ This option type can work with any kind of data
 - In fact, this option type is built into OCaml

Recursive Data Types

- ▶ We can build up lists this way

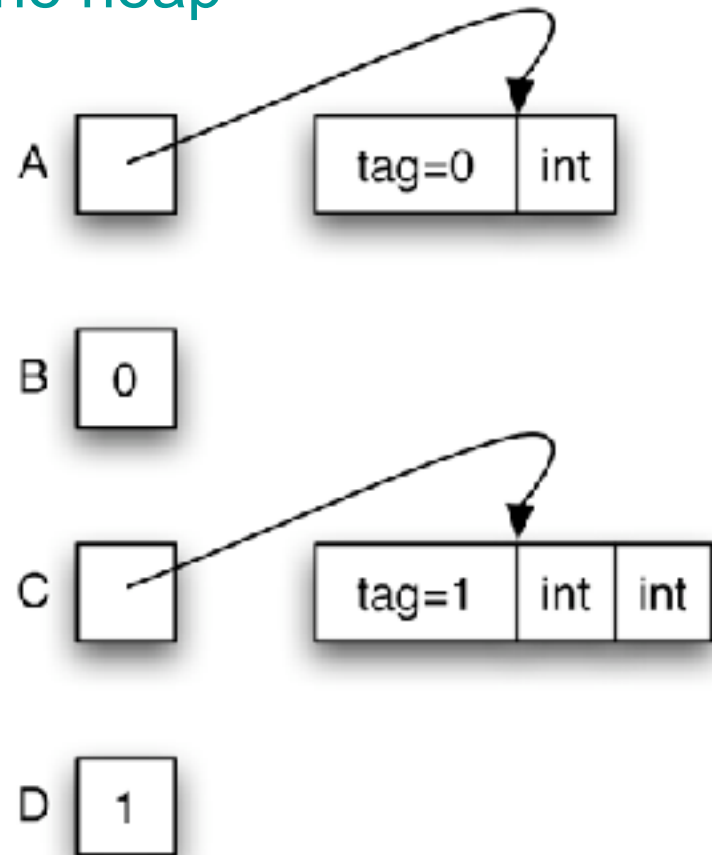
```
type 'a list =  
  Nil  
  | Cons of 'a * 'a list  
  
let rec len = function  
  Nil -> 0  
  | Cons (_, t) -> 1 + (len t)  
  
len (Cons (10, Cons (20, Cons (30, Nil))))
```

- Won't have nice `[1; 2; 3]` syntax for this kind of list

Data Type Representations

- ▶ Values in a data type are stored
 1. Directly as integers
 2. As pointers to blocks in the heap

```
type t =  
  A of int  
| B  
| C of int * int  
| D
```



Type Annotations

- ▶ The syntax `(e : t)` asserts that “`e` has type `t`”
 - This can be added anywhere you like

```
let (x : int) = 3
let z = (x : int) + 5
```
- ▶ Use to give functions parameter and return types

```
let fn (x:int):float = (float_of_int x) *. 3.14
```

 - Note special position for return type
 - Thus `let g x:int = ...` means `g` returns `int`
- ▶ Not needed for this course
- ▶ But can be useful for debugging
 - Especially for more complicated types

Conditionals

- ▶ Use `if...then...else` just like C/Java
 - No parentheses and no end

```
if grade >= 90 then
    print_string "You got an A"
else if grade >= 80 then
    print_string "You got a B"
else if grade >= 70 then
    print_string "You got a C"
else
    print_string "You're not doing so well"
```


Conditionals (cont.)

► In OCaml, conditionals return a result

- The value of whichever branch is true/false
- Like `?:` in C, C++, and Java

```
# if 7 > 42 then "hello" else "goodbye";;
```

```
- : string = "goodbye"
```

```
# let x = if true then 3 else 4;;
```

```
x : int = 3
```

```
# if false then 3 else 3.0;;
```

```
This expression has type float but is  
here used with type int
```

The Factorial Function

- ▶ Using conditionals & functions
 - Can you write `fact`, the factorial function?

```
let rec fact n =  
  if n = 0 then  
    1  
  else  
    n * fact (n-1) ;;
```

- ▶ Notice no return statements
 - This is pretty much how it needs to be written

Let Rec

- ▶ The **rec** part means “define a recursive function”
- ▶ Let vs. let rec
 - `let x = e1 in e2` `x` in scope within `e2`
 - `let rec x = e1 in e2` `x` in scope within `e2` and `e1`
- ▶ Why use let rec?
 - If you used let instead of let rec to define fact

```
let fact n =  
  if n = 0 then 1  
  else n * fact (n-1) in e2
```

 Fact is not bound here!

Examples – Let

- ▶ $x;;$
 - (* Unbound value x *)

- ▶ $\text{let } x = 1 \text{ in } x + 1;;$
 - (* 2 *)

- ▶ $\text{let } x = x \text{ in } x + 1;;$
 - (* Unbound value x *)

Examples – Let

- ▶ `let x = 1 in (x + 1 ; x) ;;`
• (* 1 – ; has higher precedence than let ... in *)

- ▶ `(let x = 1 in x + 1) ; x;;`
• (* Unbound value x *)

- ▶ `let x = 4 in (let x = x + 1 in x);;`
• (* 5 *)

Let – More Examples

▶ `let f n = 10;;`
`let f n = if n = 0 then 1 else n * f (n - 1);;`




- `f 0;;`
- `f 1;;`

▶ `let f x = ... f ... in ... f ...`
• (* Unbound value f *)



▶ `let rec f x = ... f ... in ... f ...`
• (* Bound value f *)



Recursion = Looping

- ▶ Recursion is essentially the only way to iterate
 - The only way we're going to talk about, anyway
 - Feature of functional programming languages

- ▶ Another example

```
let rec print_up_to (n, m) =  
  print_int n; print_string "\n";  
  if n < m then print_up_to (n + 1, m)
```

Lists and Recursion

► Lists have a recursive structure

- And so most functions over lists will be recursive

```
let rec length l = match l with  
  [] -> 0  
  | (_::t) -> 1 + (length t)
```

- This is just like an inductive definition
 - *The length of the empty list is zero*
 - *The length of a nonempty list is 1 plus the length of the tail*
- Type of length?

Examples – Recursive Functions

- ▶ `sum l (* sum of elts in l *)`
`let rec sum l = match l with`
 `[] -> 0`
 `| (x::xs) -> x + (sum xs)`

- ▶ `negate l (* negate elements in list *)`
`let rec negate l = match l with`
 `[] -> []`
 `| (x::xs) -> (-x) :: (negate xs)`

Examples – Recursive Functions

► `last l` (* last element of l *)

```
let rec last l = match l with
  [x] -> x
  | _::xs -> last xs
```

► `append (l, m)`

(* list containing all elements in list l followed by all elements in list m *)

```
let rec append (l, m) = match l with
  [] -> m
  | (x::xs) -> x::(append (xs, m))
```

Examples – Recursive Functions

- ▶ `rev l` (* reverse list; hint: use append *)
let rec rev l = match l with
 [] -> []
 | (x::xs) -> append ((rev xs), [x])
- `rev` takes $O(n^2)$ time. Can you do better?

A Clever Version of Reverse

```
let rec rev_helper (l, a) = match l with
  [] -> a
  | (x::xs) -> rev_helper (xs, (x::a))
let rev l = rev_helper (l, [])
```

► Let's give it a try

```
rev [1; 2; 3] →
rev_helper ([1;2;3], []) →
rev_helper ([2;3], [1]) →
rev_helper ([3], [2;1]) →
rev_helper ([], [3;2;1]) →
[3;2;1]
```

Examples – Recursive Functions

- ▶ `flattenPairs l (* ('a * 'a) list -> 'a list *)`
let rec flattenPairs l = match l with
 [] -> []
 | ((a, b)::t) -> a :: b :: (flattenPairs t)
- ▶ `take (n, l) (* return first n elements of l *)`
let rec take (n, l) =
 if n = 0 then []
 else match l with
 [] -> []
 | (x::xs) -> x :: (take (n-1, xs))

Higher-Order Functions

- ▶ In OCaml you can pass functions as arguments, and return functions as results

```
let plus_three x = x + 3
let twice (f, z) = f (f z)
twice (plus_three, 5)
// twice : ('a->'a) * 'a -> 'a
```

```
let plus_four x = x + 4
let pick_fn n =
  if n > 0 then plus_three else plus_four
(pick_fn 5) 0
// pick_fn : int -> (int->int)
```

The map Function

► Let's write the `map` function

- Takes a function and a list, applies the function to each element of the list, and returns a list of the results

```
let rec map (f, l) = match l with
  [] -> []
  | (h::t) -> (f h) :: (map (f, t))
```

```
let add_one x = x + 1
```

```
let negate x = -x
```

```
map (add_one, [1; 2; 3])
```

```
map (negate, [9; -5; 0])
```

The map Function (cont.)

- ▶ What is the type of the map function?

```
let rec map (f, l) = match l with
  [] -> []
  | (h::t) -> (f h) :: (map (f, t))
```

$('a \rightarrow 'b) * 'a \text{ list} \rightarrow 'b \text{ list}$


f l

Anonymous Functions

- ▶ Passing functions around is very common
 - So often we don't want to bother to give them names
- ▶ Use `fun` to make a function with no name

Parameter

Body



```
fun x -> x + 3
```

```
twice ((fun x -> x + 3), 5)
```

```
map ((fun x -> x+1), [1; 2; 3])
```

Pattern Matching with fun

- ▶ `match` can be used within `fun`

```
map ((fun l -> match l with (h::_) -> h),  
     [ [1; 2; 3]; [4; 5; 6; 7]; [8;  
     9] ])
```

- ▶ But use named functions for complicated matches
- ▶ May use standard pattern matching abbreviations

```
map ((fun (x, y) -> x+y), [(1,2); (3,4)])
```

All Functions Are Anonymous

- ▶ Functions are first-class, so you can bind them to other names as you like

```
let f x = x + 3
let g = f
g 5
```

- ▶ In fact, `let` for functions is just shorthand

```
let f x = body
```

```
      ↓      stands for
let f = fun x -> body
```

Examples – Anonymous Functions

▶ `let next x = x + 1`

- Short for `let next = fun x -> x + 1`

▶ `let plus (x, y) = x + y`

- Short for `let plus = fun (x, y) -> x + y`

- Which is short for

```
let plus = fun z ->
```

```
  (match z with (x, y) -> x + y)
```

Examples – Anonymous Functions

- ▶ `let rec fact n =`
 - `if n = 0 then 1 else n * fact (n-1)`
 - Short for `let rec fact = fun n ->`
 - `(if n = 0 then 1 else n * fact (n-1))`

The fold Function

▶ Common pattern

- Iterate through list and apply function to each element, keeping track of partial results computed so far

```
let rec fold (f, a, l) = match l with
  [] -> a
  | (h::t) -> fold (f, f (a, h), t)
```

- **a** = “accumulator”
- Usually called **fold left** to remind us that **f** takes the accumulator as its first argument

▶ What's the type of **fold**?

= ('a * 'b -> 'a) * 'a * 'b list -> 'a

Example

```
let rec fold (f, a, l) = match l with
  [] -> a
  | (h::t) -> fold (f, f (a, h), t)
```

```
let add (a, x) = a + x
fold (add, 0, [1; 2; 3; 4]) →
fold (add, 1, [2; 3; 4]) →
fold (add, 3, [3; 4]) →
fold (add, 6, [4]) →
fold (add, 10, []) →
10
```

We just built the `sum` function!

Another Example

```
let rec fold (f, a, l) = match l with
  [] -> a
  | (h::t) -> fold (f, f (a, h), t)
```

```
let next (a, _) = a + 1
fold (next, 0, [2; 3; 4; 5]) →
fold (next, 1, [3; 4; 5]) →
fold (next, 2, [4; 5]) →
fold (next, 3, [5]) →
fold (next, 4, []) →
4
```

We just built the `length` function!

Using fold to Build rev

```
let rec fold (f, a, l) = match l with
  [] -> a
  | (h::t) -> fold (f, f (a, h), t)
```

- ▶ Can you build the **reverse** function with **fold**?

```
let prepend (a, x) = x::a
fold (prepend, [], [1; 2; 3; 4]) →
fold (prepend, [1], [2; 3; 4]) →
fold (prepend, [2; 1], [3; 4]) →
fold (prepend, [3; 2; 1], [4]) →
fold (prepend, [4; 3; 2; 1], []) →
[4; 3; 2; 1]
```

The Call Stack in C/Java/etc.

```
void f(void) {  
  int x;  
  x = g(3);  
}
```

```
int g(int x) {  
  int y;  
  y = h(x);  
  return y;  
}
```

```
int h (int z) {  
  return z + 1;  
}
```

```
int main(){  
  f();  
  return 0;  
}
```

x	4	f
x	3	g
y	4	
z	3	h

Nested Functions

- ▶ In OCaml, you can define functions anywhere
 - Even inside of other functions

```
let sum l =  
  fold ((fun (a, x) -> a + x), 0, l)
```

```
let pick_one n =  
  if n > 0 then (fun x -> x + 1)  
  else (fun x -> x - 1)  
(pick_one -5) 6    (* returns 5 *)
```

Nested Functions (cont.)

- ▶ You can also use **let** to define functions inside of other functions

```
let sum l =  
  let add (a, x) = a + x in  
  fold (add, 0, l)
```

```
let pick_one n =  
  let add_one x = x + 1 in  
  let sub_one x = x - 1 in  
  if n > 0 then add_one else sub_one
```

How About This?

```
let addN (n, l) =  
  let add x = n + x in  
  map (add, l)
```

- (Equivalent to...)

Accessing variable
from outer scope



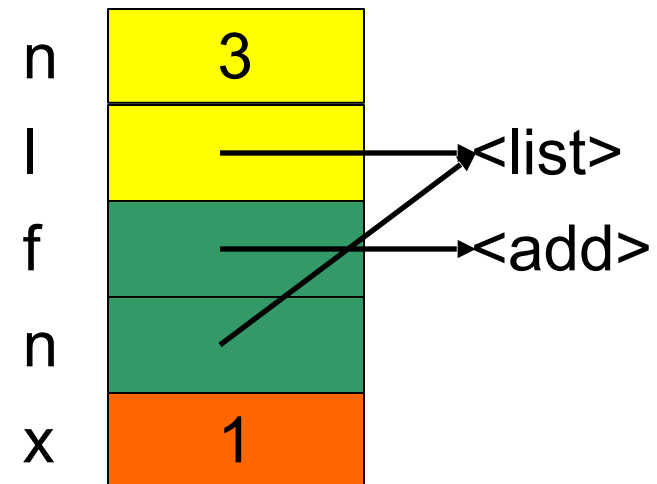
```
let addN (n, l) =  
  map ((fun x -> n + x), l)
```

Consider the Call Stack Again

```
let map (f, n) = match n with
  [] -> []
| (h::t) -> (f h)::(map (f, t))
```

```
let addN (n, l) =
  let add x = n + x in
  map (add, l)
```

```
addN (3, [1; 2; 3])
```



- ▶ Uh oh...how does `add` know the value of `n`?
 - **Dynamic scoping**: it reads it off the stack
 - The language could do this, but can be confusing (see above)
 - OCaml uses **static scoping** like C, C++, Java, and Ruby

Static Scoping

- ▶ In **static** or **lexical scoping**, (nonlocal) names refer to their nearest binding in the program text
 - Going from inner to outer scope
 - In our example, **add** refers to **addN**'s **n**
 - C example:

Refers to the **x** at file scope – that's the nearest **x** going from inner scope to outer scope in the source code

```
int x;
void f() { x = 3; }
void g() { char *x = "hello"; f(); }
```

Returned Functions

- ▶ As we saw, in OCaml a function can return another function as a result
 - So consider the following example

```
let addN n = (fun x -> x + n)
(addN 3) 4 (* returns 7 *)
```

- When the anonymous function is called, `n` isn't even on the stack any more!
 - We need some way to keep `n` around after `addN` returns

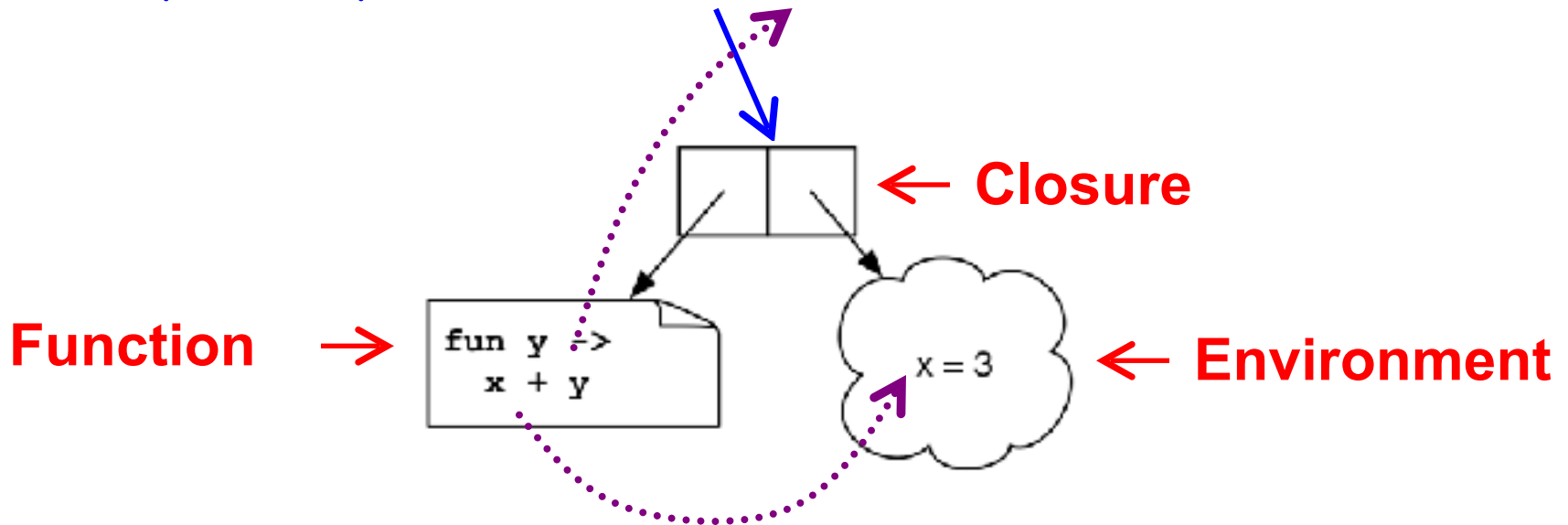
Environments and Closures

- ▶ An **environment** is a mapping from variable names to values
 - Just like a stack frame
- ▶ A **closure** is a pair (f, e) consisting of function code f and an environment e
- ▶ When you invoke a closure, f is evaluated using e to look up variable bindings

Example – Closure 1

```
let add x = (fun y -> x + y)
```

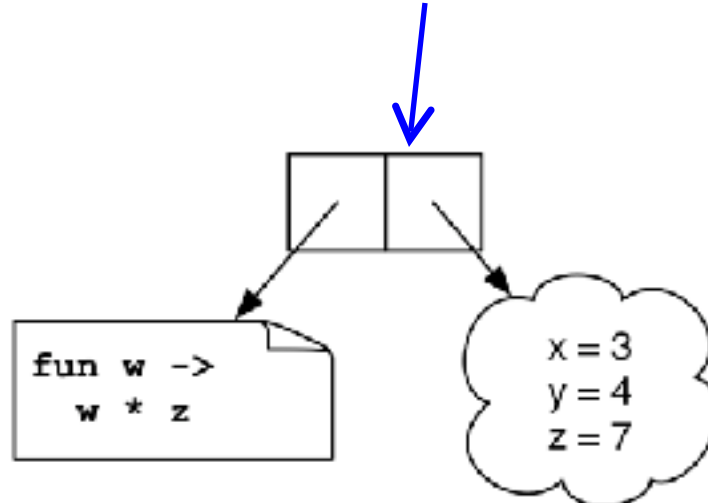
(add 3) 4 → <cl> 4 → 3 + 4 → 7



Example – Closure 2

```
let mult_sum (x, y) =  
  let z = x + y in  
  fun w -> w * z
```

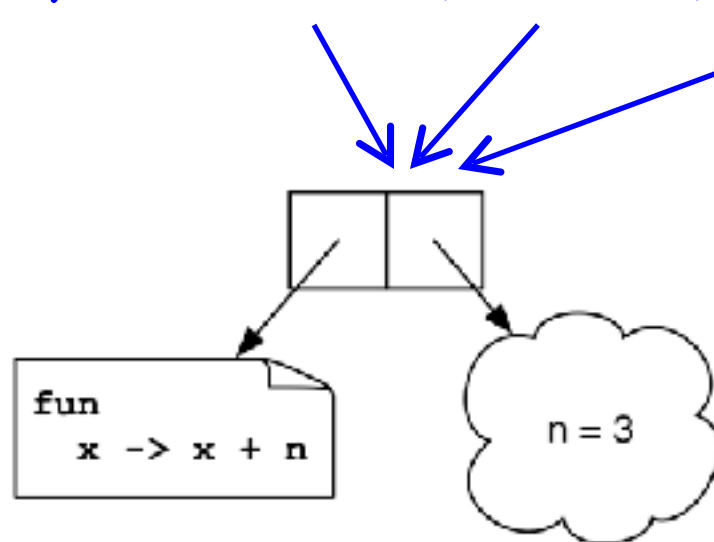
`(mult_sum (3, 4)) 5` → `<cl> 5` → `5 * 7` → `35`



Example – Closure 3

```
let twice (n, y) =  
  let f x = x + n in  
  f (f y)
```

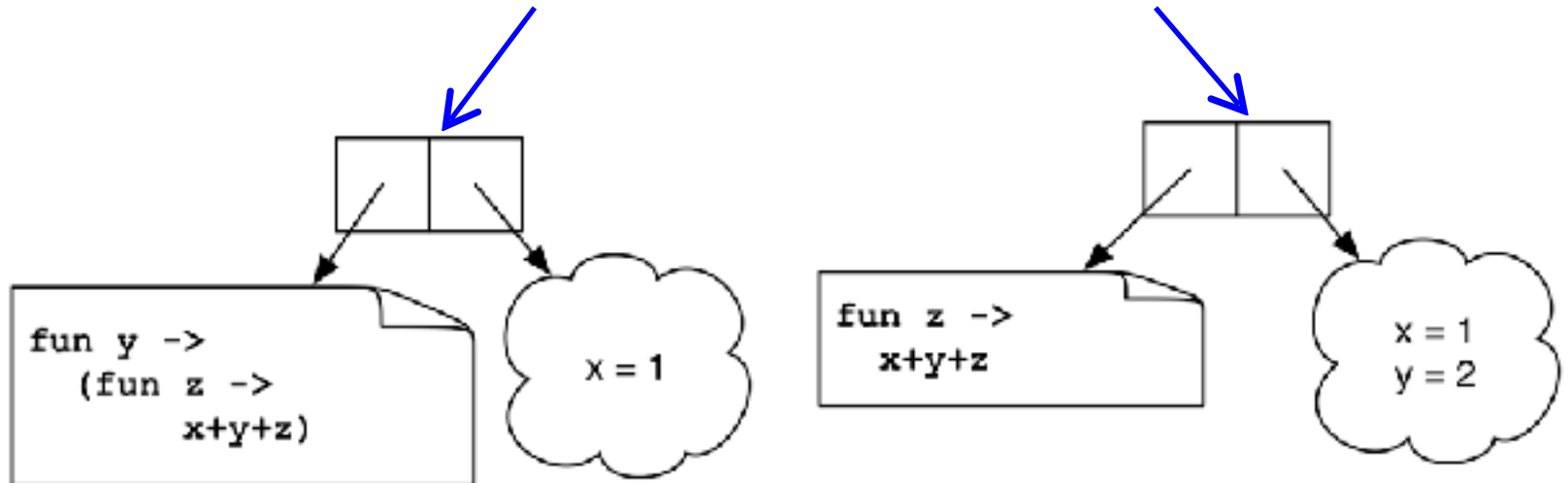
`twice (3, 4) → <cl> (<cl> 4) → <cl> 7 → 10`



Example – Closure 4

```
let add x = (fun y -> (fun z -> x + y + z))
```

`((add 1) 2) 3` → `(<c1> 2) 3` → `<c1> 3` → `1+2+3`



Currying

- ▶ We just saw another way for a function to take multiple arguments
 - The function consumes one argument at a time, creating closures until all the arguments are available
- ▶ This is called **currying** the function
 - Named after the logician Haskell B. Curry
 - But Schönfinkel and Frege discovered it
 - So it should probably be called Schönfinkelizing or Fregging

Curried Functions in OCaml

- ▶ OCaml has a really simple syntax for currying

```
let add x y = x + y
```

- This is identical to all of the following

```
let add = (fun x -> (fun y -> x + y))  
let add = (fun x y -> x + y)  
let add x = (fun y -> x+y)
```

Curried Functions in OCaml (cont.)

- ▶ What is the type of add?

```
let add x y = x + y
```

- ▶ Answer

- add has type `int -> (int -> int)`
- add 3 has type `int -> int`
 - add 3 is a function that adds 3 to its argument
- `(add 3) 4 = 7`

- ▶ This works for any number of arguments

Curried Functions in OCaml (cont.)

- ▶ Currying is so common, OCaml uses the following conventions
 - `->` associates to the right
 - `int -> int -> int` is the same as `int -> (int -> int)`
 - Function application `()` associates to the left
 - `add 3 4` is the same as `(add 3) 4`

Another Example of Currying

- ▶ A curried add function with three arguments

```
let add_th x y z = x + y + z
```

is the same as

```
let add_th x = (fun y -> (fun z -> x+y+z))
```

- ▶ Then...

- `add_th` has type `int -> (int -> (int -> int))`
- `add_th 4` has type `int -> (int -> int)`
- `add_th 4 5` has type `int -> int`
- `add_th 4 5 6` is `15`

Recall Functions `map` & `fold`

► Map

```
let rec map (f, l) = match l with  
  [] -> []  
  | (h::t) -> (f h) :: (map (f, t))
```

- Type = ('a -> 'b) * 'a list -> 'b list

► Fold

```
let rec fold (f, a, l) = match l with  
  [] -> a  
  | (h::t) -> fold (f, f (a, h), t)
```

- Type = ('a * 'b -> 'a) * 'a * 'b list -> 'a

Currying and the `map` Function

► New Map

```
let rec map f l = match l with
  [] -> []
| (h::t) -> (f h) :: (map f t)
```

► Examples

```
let negate x = -x
```

```
map negate [1; 2; 3] (* [-1; -2; -3 ] *)
```

```
let negate_list = map negate
```

```
negate_list [-1; -2; -3] (* [1; 2; 3 ] *)
```

```
let sum_pair_l = map (fun (a, b) -> a + b)
```

```
sum_pair_l [(1, 2); (3, 4)] (* [3; 7] *)
```

► What is the type of this form of map?

```
('a -> 'b) -> 'a list -> 'b list
```

Currying and the **fold** Function

► New Fold

```
let rec fold f a l = match l with
| [] -> a
| (h::t) -> fold f (f a h) t
```

► Examples

```
let add x y = x + y
```

```
fold add 0 [1; 2; 3] (* 6 *)
```

```
let sum = fold add 0
```

```
sum [1; 2; 3] (* 6 *)
```

```
let next n _ = n + 1
```

```
let len = fold next 0 (* len not polymorphic! *)
```

```
len [4; 5; 6; 7; 8] (* 5 *)
```

► What is the type of this form of fold?

```
('a -> 'b -> 'a) -> 'a -> 'b list -> 'a
```

Another Convention

- ▶ Since functions are curried, **function** can often be used instead of **match**
 - **function** declares anonymous function w/ one argument
 - Instead of

```
let rec sum l = match l with  
  [] -> 0  
| (h::t) -> h + (sum t)
```

- It could
 be written

```
let rec sum = function  
  [] -> 0  
| (h::t) -> h + (sum t)
```

Another Convention (cont.)

- Instead of

```
let rec map f l = match l with
  [] -> []
| (h::t) -> (f h) :: (map f t)
```

- It could be written

```
let rec map f = function
  [] -> []
| (h::t) -> (f h) :: (map f t)
```

Currying is Standard in OCaml

- ▶ Pretty much all functions are curried
 - Like the standard library `map`, `fold`, etc.
 - See `/usr/local/lib/ocaml`
 - In particular, look at the file `list.ml` for standard list functions
 - Access these functions using `List.<fn name>`
 - E.g., `List.hd`, `List.length`, `List.map`
- ▶ OCaml plays a lot of tricks to avoid creating closures and to avoid allocating on the heap
 - It's unnecessary much of the time, since functions are usually called with all arguments

OCaml Exceptions

```
exception My_exception of int
let f n =
  if n > 0 then
    raise (My_exception n)
  else
    raise (Failure "foo")
let bar n =
  try
    f n
  with My_exception n ->
    Printf.printf "Caught %d\n" n
  | Failure s ->
    Printf.printf "Caught %s\n" s
```

OCaml Exceptions (cont.)

- ▶ Exceptions are declared with **exception**
 - They may appear in the signature as well
- ▶ Exceptions may take arguments
 - Just like type constructors
 - May also be nullary
- ▶ Catch exceptions with **try...with...**
 - Pattern-matching can be used in **with**
 - If an exception is uncaught
 - Current function exits immediately
 - Control transfers up the call chain
 - Until the exception is caught, or reaches the top level

OCaml Exceptions (cont.)

- ▶ Exceptions may be thrown by I/O statements
 - Common way to detect end of file
 - Need to decide how to handle exception
- ▶ Example

```
try
  (input_char stdin)      (* reads 1 char *)
with End_of_file -> 0    (* return 0?      *)

try
  read_line ()           (* reads 1 line *)
with End_of_file -> ""  (* return ""?     *)
```

Modules

- ▶ So far, most everything we've defined
 - Has been at the “top-level” of OCaml
 - This is not good software engineering practice
- ▶ A better idea
 - Use **modules** to group together associated
 - Types, functions, and data
 - Avoid polluting the top-level with unnecessary stuff
- ▶ For lots of sample modules
 - See the OCaml standard library

Modularity and Abstraction

- ▶ Another reason for creating a module
 - So we can **hide** details
 - Example
 - Build a binary tree module
 - Hide exact representation of binary trees
 - This is also good software engineering practice
 - Prevents clients from relying on details that may change
 - Hides unimportant information
 - Promotes local understanding (clients can't inject arbitrary data structures, only ones our functions create)

Modularity

▶ Definition

- Extent to which a computer program is composed of **separate** parts
- Higher degree of modularity is better

▶ Modular programming

- Programming techniques that increase modularity
 - Interface vs. implementation

▶ Modular programming languages

- Explicit support for modules
- ML, Modula-2, **OCaml**

Creating a Module in OCaml

```
module Shapes =
  struct
    type shape =
      Rect of float * float (* wid*len *)
      | Circle of float      (* radius  *)

    let area = function
      Rect (w, l) -> w *. l
      | Circle r -> r *. r *. 3.14

    let unit_circle = Circle 1.0
  end;;
```

Creating a Module in OCaml (cont.)

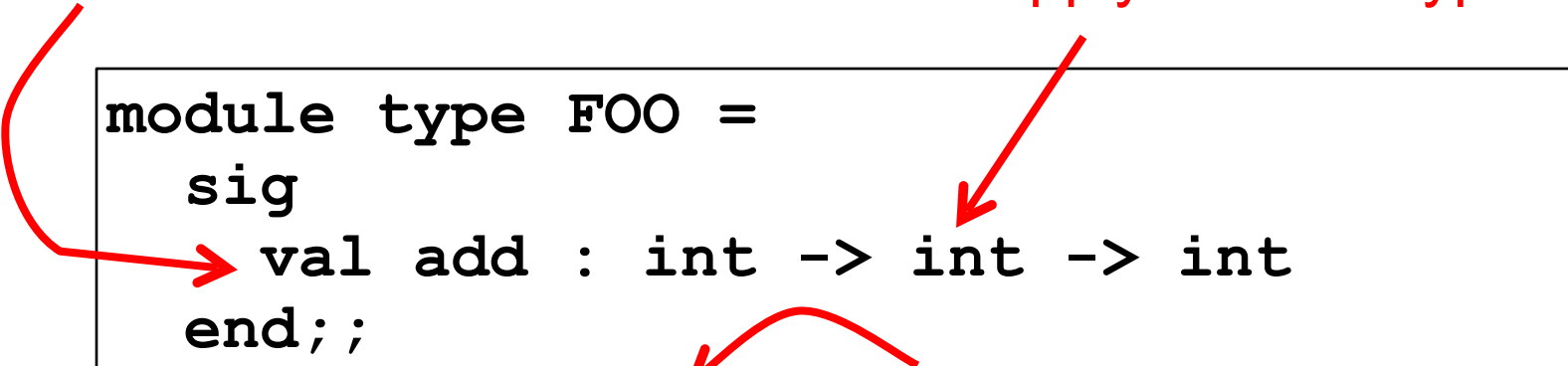
```
module Shapes =
  struct
    type shape = ...
    let area = ...
    let unit_circle = ...
  end;;
unit_circle;;      (* not defined *)
Shapes.unit_circle;;
Shapes.area (Shapes.Rect (3.0, 4.0));;
open Shapes;;     (* import names
                   into curr scope *)
unit_circle;;     (* now defined *)
```


Module Signatures

Entry in signature

Supply function types

```
module type FOO =  
  sig  
    val add : int -> int -> int  
  end;;  
module Foo : FOO =  
  struct  
    let add x y = x + y  
    let mult x y = x * y  
  end;;  
Foo.add 3 4;;      (* OK *)  
Foo.mult 3 4;;    (* not accessible *)
```



Module Signatures (cont.)

▶ Convention

- Signature names are **all capital letters**
- This isn't a strict requirement, though

▶ Items can be omitted from a module signature

- This provides the ability to hide values

▶ The default signature for a module hides nothing

- You'll notice this is what OCaml gives you if you just type in a module with no signature at the top-level

Abstract Types in Signatures

```
module type SHAPES =
  sig
    type shape
    val area : shape -> float
    val unit_circle : shape
    val make_circle : float -> shape
    val make_rect : float -> float -> shape
  end;;

module Shapes : SHAPES =
  struct
    ...
    let make_circle r = Circle r
    let make_rect x y = Rect (x, y)
  end
```

- ▶ Now definition of **shape** is hidden

Abstract Types in Signatures

```
# Shapes.unit_circle
- : Shapes.shape = <abstr> (* OCaml won't show impl *)
# Shapes.Circle 1.0
Unbound Constructor Shapes.Circle
# Shapes.area (Shapes.make_circle 3.0)
- : float = 29.5788
# open Shapes;;
# (* doesn't make anything abstract accessible *)
```

- ▶ How does this compare to modularity in...
 - C?
 - C++?
 - Java?

.ml and .mli files

- ▶ Put the signature in a `foo.mli` file, the struct in a `foo.ml` file
 - Use the same names
 - Omit the `sig...end` and `struct...end` parts
 - The OCaml compiler will make a `Foo` module from these

Example – OCaml Module Signatures

shapes.mli

```
type shape
val area : shape -> float
val unit_circle : shape
val make_circle : float -> shape
val make_rect : float -> float -> shape
```

shapes.ml

```
type shape =
  Rect of ...
...
let make_circle r = Circle r
let make_rect x y = Rect (x, y)
```

```
% ocamlc shapes.mli      # produces shapes.cmi
% ocamlc shapes.ml      # produces shapes.cmo
ocaml
# #load "shapes.cmo"    (* load Shapes module *)
```

Functors

- ▶ Modules can take other modules as arguments
 - Such a module is called a **functor**
 - You're mostly on your own if you want to use these
- ▶ Example: **Set** in standard library

```
module type OrderedType = sig
  type t
  val compare : t -> t -> int
end

module Make(Ord: OrderedType) =
  struct ... end

module StringSet = Set.Make(String);;
(* works because String has type t,
  implements compare *)
```

So Far, Only Functional Programming

- ▶ We haven't given you **any** way so far to change something in memory
 - All you can do is create new values from old
- ▶ This actually makes programming **easier** !
 - Don't care whether data is shared in memory
 - Aliasing is irrelevant
 - Provides strong support for compositional reasoning and abstraction
 - Example: Calling a function f with argument x always produces the same result
 - But could take (much) more memory & time to execute

Imperative OCaml

► There are three basic operations on memory

1) `ref` : `'a -> 'a ref`

➤ Allocate an updatable reference

2) `!` : `'a ref -> 'a`

➤ Read the value stored in reference

3) `:=` : `'a ref -> 'a -> unit`

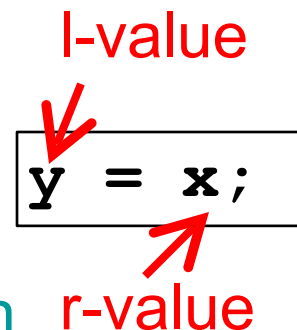
➤ Write to a reference

```
let x = ref 3    (* x : int ref *)
let y = !x
x := 4
```

Comparison to L- and R-values

- ▶ Recall that in C/C++/Java, there's a strong distinction between l- and r-values

- An r-value refers to just a value, like an integer
- An l-value refers to a location that can be written



- ▶ A variable's meaning depends on where it appears
 - On the right-hand side, it's an r-value, and it refers to the contents of the variable
 - On the left-hand side of an assignment, it's an l-value, and it refers to the location the variable is stored in

L-Values and R-Values in C (cont.)

Store 3 in
location x

```
int x;  
int y;  
x = 3;
```

Read contents
of x and store
in location y

```
y = x;
```

Makes no
sense

```
3 = x;
```

- ▶ Notice that x, y, 3 all have the **same** type: **int**

Comparison to OCaml

```
int x; C  
Int y;  
  
x = 3;  
  
y = x;  
  
3 = x;
```

```
let x = ref 0;; OCaml  
let y = ref 0;;  
  
x := 3;; (* x : int ref *)  
  
y := (!x) ; ;  
  
3 := x;; (* 3 : int; error *)
```

- ▶ In OCaml, an updatable location and the contents of the location have **different** types
 - The location has a **ref** type

Capturing a **ref** in a Closure

- ▶ We can use **refs** to make things like counters that produce a fresh number “everywhere”

```
let next =
  let count = ref 0 in
  function () ->
    let temp = !count in
      count := (!count) + 1;
      temp;;
# next ();;
- : int = 0
# next ();;
- : int = 1
```

Semicolon Revisited; Side Effects

- ▶ Now that we can update memory, we have a real use for `;` and `() : unit`
 - `e1; e2` means evaluate `e1`, throw away the result, and then evaluate `e2`, and return the value of `e2`
 - `()` means “no interesting result here”
 - It’s only interesting to throw away values or use `()`
 - If computation does something besides return a result
- ▶ A **side effect** is a visible state change
 - Modifying memory
 - Printing to output
 - Writing to disk

Grouping with begin...end

- ▶ If you're not sure about the scoping rules, use `begin...end` to group together statements with semicolons

```
let x = ref 0

let f () =
  begin
    print_string "hello";
    x := (!x) + 1
  end
```

The Trade-Off of Side Effects

- ▶ Side effects are absolutely necessary
 - That's usually why we run software!
 - We want something to happen that we can observe

- ▶ But...they also make reasoning harder
 - Order of evaluation now matters
 - Calling the same function in different places may produce different results
 - Aliasing is an issue
 - If we call a function with refs $r1$ and $r2$, it might do strange things if $r1$ and $r2$ are aliased

Records

- Labeled tuples of values

```
# type course = {title:string; num:int};;
type course = { title : string; num : int; }
# let x = {title="Program Analysis"; num=150};;
val x : course = {title = "Program Analysis"; num = 150}
```

- Fields are referenced with the dot notation

```
# x.title;;
- : string = "Program Analysis"
# x.number;;
- : int = 150
```

- All record types are named, and must be complete in any instance

```
# let y = {title="Program Analysis"};;
Error: Some record field labels are undefined: num
```

Records (cont'd)

- Record patterns can include partial matches

```
# let nextNum {num=x} = x;;  
val nextNum : course -> int = <fun>
```

- The `with` construct can be used to modify just part of a record

```
# {x with num=151};;  
- : course = {title = "Program Analysis"; num = 151}
```

Records (cont'd)

- Record fields may be **mutable**

```
# type course = {title:string; mutable num:int};;
type course = { title : string; mutable num : int; }
# let x = {num=150; title="Program Analysis"};;
val x : course = {title = "Program Analysis"; num = 150}
# x.num <- 151;;
- : unit = ()
# x;;
- : course = {title = "Program Analysis"; num = 151}
```

- In fact, this is what updatable refs translate to

```
# let y = ref 42;;
val y : int ref = {contents = 42}
```

Arrays and strings

- OCaml arrays are mutable and bounds-checked

```
# let x = [|1;2;3|];;
val x : int array = [|1; 2; 3|]
# x.(0) <- 4;;
- : unit = ()
# x;;
- : int array = [|4; 2; 3|]
# x.(4);;
Exception: Invalid_argument "index out of bounds".
# x.(-1);;
Exception: Invalid_argument "index out of bounds".
```

- OCaml strings are also mutable (this will change!)

```
# let x = "Hello";;
val x : string = "Hello"
# x.[0] <- 'J';;
- : unit = ()
# x;;
- : string = "Jello"
```

Labeled arguments

- OCaml allows arguments to be labeled

```
# let f ~x ~y = x-y;;  
val f : x:int -> y:int -> int = <fun>  
# f 4 3;;  
- : int = 1  
# f ~y:4 ~x:3;;  
- : int = -1
```

- Functions with labeled args can be partially applied

```
# let g = f ~y:4;;  
val g : x:int -> int = <fun>  
# g 3;;  
- : int = -1  
# g ~x:3;;  
- : int = -1
```

Optional arguments

- Labeled arguments may be optional

```
# let bump ?(step = 1) x = x + step;;  
val bump : ?step:int -> int -> int = <fun>  
# bump 2;;  
- : int = 3  
# bump ~step:3 2;;  
- : int = 5
```

- One nit: type inference with partial applications of functions with labeled arguments may not always work

While and for

```
# while true do Printf.printf "Hello\n";;  
Hello  
Hello  
Hello  
...  
# for i = 1 to 10 do Printf.printf "%d\n" i done;;  
1  
2  
...  
10
```

- Can you encode **while** and **for** only using functions and recursion?

Variants

- Recall OCaml data types (also called *variants*)

```
type shape =  
| Circle of float  
| Rect of float * float
```

- Each constructor name refers to a unique type
 - E.g., `Circle` always makes a shape
- Some downsides
 - Have to define all such types in advance of uses
 - Can't accept data coming from two different variants

Polymorphic variants

- Like variants, but permit an unbounded number of constructors, created anywhere
 - Type inference takes care of matching up various uses

```
# [\On; \Off];;  
- : [> \Off | \On ] list = [\On; \Off]  
# \Number 1;  
- : [> \Number of int ] = \Number 1  
# let f = function \On -> 1 | \Off -> 0 | \Number n -> n;;  
val f : [< \Number of int | \Off | \On ] -> int = <fun>  
# List.map f [\On; \Off];;  
- : int list = [1; 0]
```

- “`<`”—allow fewer tags “`>`”—allow more tags
- Can remove this ability by creating a named type

```
# type 'a vlist = [\Nil | \Cons of 'a * 'a vlist];;  
type 'a vlist = [ \Cons of 'a * 'a vlist | \Nil ]
```

Regular vs. polymorphic variants

- Benefits of polymorphic variants:
 - More flexible
 - If used well, can improve modularity, maintainability
- Benefits of regular variants:
 - More type checking permitted
 - Only declared constructors used
 - Check for complete pattern matching
 - Enforce type constraints on parameters
 - Better error messages
 - Sometimes type inference with polymorphic variants subtle
 - Compiler can create slightly more optimized code
 - More is known at compile time