

# PILOT: An Interactive Tool for Learning and Grading\*

Stina Bridgeman  
Brown Univ.  
ssb@cs.brown.edu

Michael T. Goodrich  
Johns Hopkins Univ.  
goodrich@jhu.edu

Stephen G. Kobourov  
Johns Hopkins Univ.  
kobourov@cs.jhu.edu

Roberto Tamassia  
Brown Univ.  
rt@cs.brown.edu

## Abstract

We describe a Web-based interactive system, called PILOT, for testing computer science concepts. The strengths of PILOT are its universal access and platform independence, its use as an algorithm visualization tool, its ability to test algorithmic concepts, its support for graph generation and layout, its automated grading mechanism, and its ability to award partial credit to proposed solutions.

## 1 Introduction

Interactive World Wide Web (WWW)-based learning tools have become the focus of research for a large number of computer science educators [7, 8]. Interaction and animation in and out of the classroom offer the chance to actively engage students in the learning process. Several interactive educational tools have been developed over the last few years. Many of these, however, quickly become obsolete as hardware/software platforms and operating systems change. With the advent of platform-independent applications, there are far greater possibilities for creating more useful educational tools. While many computer science courses offer online access to handouts, syllabi, homework assignments solutions and other static documents, only a few have begun to exploit the full potential of the new technology available to us.

Online testing systems can be useful in distance learn-

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ing, virtual universities, and online classes, and several systems that allow for online testing have been developed in the last decade (e.g., see [10]). Such systems tend to support multiple-choice questions, which provide a natural class of questions that can be automatically graded online. While such questions can be used to provide useful measures of student learning, we believe there are significant additional learning and testing opportunities available that have yet to be fully exploited. In particular, because of the ability to formally define input and output specifications, there are other more complex questions that should also allow for automatic online grading, at least in theory. Some of the immediate advantages of online grading for richer sets of questions are the ability to test students' answer *creation* abilities rather than simply their answer *choosing* abilities. In addition, online grading also provides fast and consistent grading, provably correct solutions, and pointers to information relevant to the question. Moreover, online grading also allows the assignment of different questions to the students, thus reducing issues of cheating and plagiarism.

We are therefore interested in interactive online automated grading tools that aid student learning and test answer creation abilities, not just answer choosing skills. In addition, we are interested in the visualization of questions, errors, and answers.

### 1.1 Previous Work

Several previous software systems have been designed with online testing in mind [13, 14]. Blackboard.com [5] provides automatic grading for quizzes with multiple choice and true/false questions. Systems such as QUIZIT [17], WebCT [18], and ASSYST [12] have been designed to perform online testing of answers whose correct syntax can be specified as regular expressions. Previous systems that allow for richer types of answers have needed assistance from the course graders and the instructor to perform the actual answer checking. In addition to the difficulty of dealing with sophisticated forms of answers, another area where these previous systems have trouble is in their lack of ability to provide partial credit to answers that are "almost" correct.

Intelligent tutoring systems have been an area of research in artificial intelligence for several decades. The primary application of these systems is providing feedback and tutoring the student rather than grading responses. Many systems, such as the LISP Tutor [2] and the Geometry Tutor [1], focus on abstract problem-solving skills and thus are more complicated than our aims here.

Since our notion of answer specification and checking involves a strong visualization component, it is also related to previous work on the visualization of algorithms and data structures. There is a rich literature that describes the benefits of concept visualization in education settings. Algorithm animation has been successfully used for visualizing graph algorithms, sorting, and searching, to name a few examples [16]. Similarly, program code animation also helps in the learning of new programming languages. Finally, concept animation has also been successful in communicating difficult concepts such as finite state automata [7]. Tools for creating animations of data structures and algorithms have also been developed [15]. Interactive tutorials have been designed and their positive impact on student learning evaluated [4]. Electronic books have been proposed and developed, in which hypertext, interactive animations, audio and video parts are integrated in a web-based standalone educational resource [6].

## 1.2 Our Results

We have designed a Platform-Independent Learning Online Tool, PILOT, with several goals in mind. First, we would like to offer an interactive tool that can be used in class to aid in exposition. Furthermore, there are numerous problems that students learn best by example, and we would like a tool that can generate random instances of a problem and allow the student to create the solution online. Finally, we would like to allow for automated grading so that the student can receive immediate feedback on her work. Thus, PILOT allows for:

- WWW access and platform independence
- generation of interesting random instances of a problem
- user interaction to specify a solution
- online submission of solutions for evaluation
- evaluation of solutions, providing a score and comments
- generation of correct solutions to the problem

At this time, PILOT supports graph problems such as finding the minimum spanning tree (MST), tree search algorithms (breadth first search (BFS) and depth first search (DFS)), and shortest path algorithms.

One of the main advantages of PILOT is that it is a platform independent client/server based applet that can

be run from a browser such as Netscape or Internet Explorer. Another even more important feature is its capability to successfully interact with the student by providing detailed feedback. For example, in creating a MST, if an edge is chosen incorrectly, PILOT will highlight the edge and suggest how to correct it.

With additional security, PILOT can be used for grading by allowing graders to input both problems and students' solutions. (In the current system, PILOT can only be used to check problems generated on the spot. This is to prevent students from entering their homework problems and using PILOT's problem-solving capabilities to obtain solutions.) Such security could take the form of password protection or encryption, to allow only authorized users to connect. Additional security would also allow the use of PILOT in testing situations, where it is important to ensure that each student only submits one version of the answer.

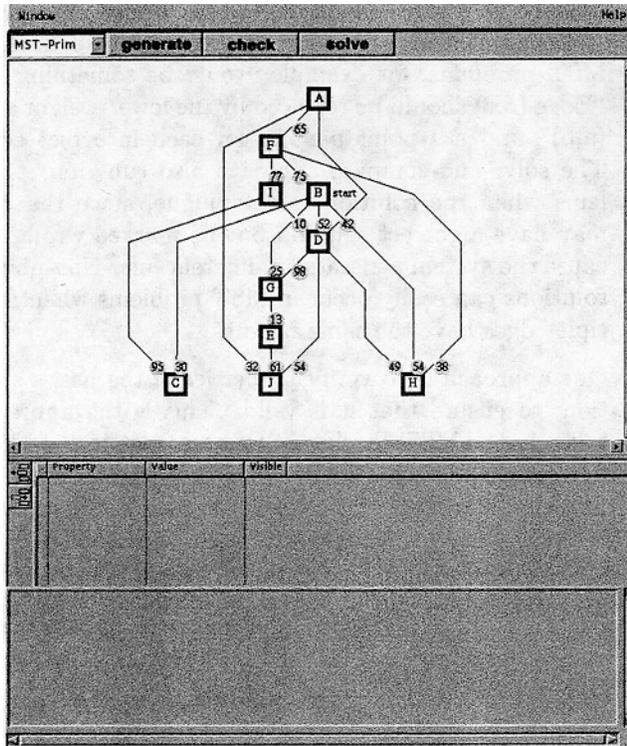
## 2 Using PILOT

In the current scenario, the user chooses a problem type from a pull-down menu and clicks the "generate" button to create a random instance of that problem. Figure 1(a) shows the result of generating an instance of MST-Prim — a minimum spanning tree problem to be solved using Prim's algorithm. PILOT easily allows testing of both general concepts ("find a minimum spanning tree of the given graph") and specific algorithms ("find a minimum spanning tree of the given graph, using Prim's algorithm"). For MST-Prim, the user is to execute Prim's algorithm, starting with the vertex marked "start"; the solution is a numbering of the edges in the order in which they were added to the MST. To indicate the solution, the user clicks on the edges belonging to the MST. The order can be adjusted in the "Edge Ordering" window; by default, the edges are listed in the order in which they are selected.

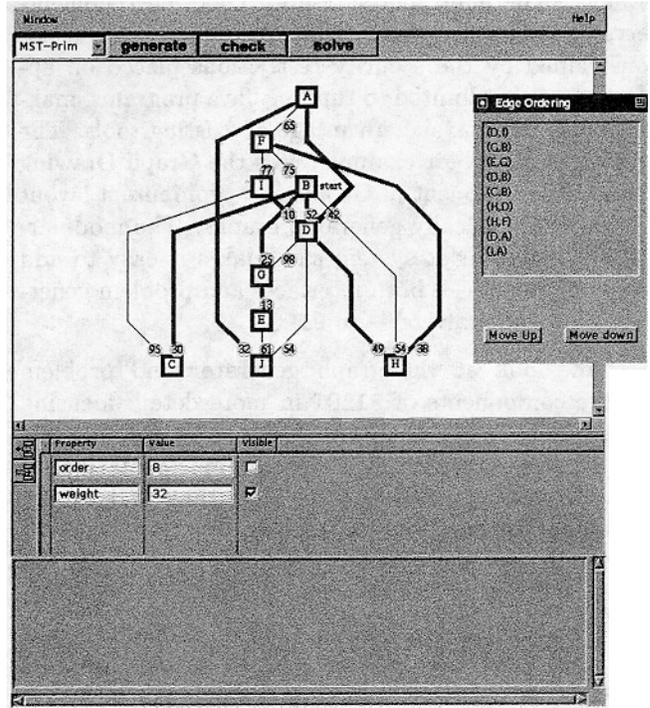
Once the user is satisfied that she has entered the correct solution (Figure 1(b)), clicking the "check" button will correct and grade the solution. The system will display the graph with the incorrect edges highlighted, along with a score and an explanation of the errors made; see Figure 1(c). Note that the actual solution is not displayed — this is because the checker may not actually compute the solution in the process of grading the user's input. A solution can be obtained at any point by clicking the "solve" button; see Figure 1(d).

## 3 PILOT Architecture

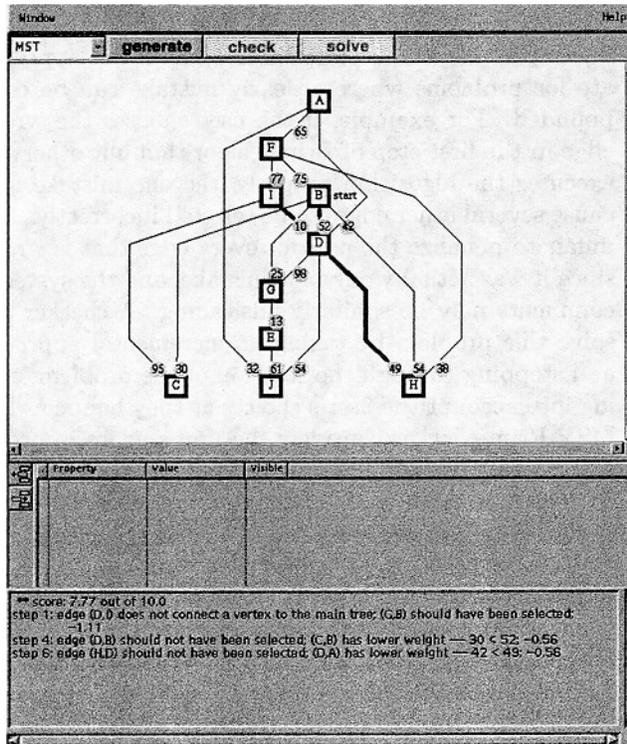
PILOT uses a client-server architecture, and is built on top of GeomNet [3]. In the GeomNet model, the client is responsible for maintaining the user interface and all of the algorithm-related computation is done on the server. For PILOT, the client is implemented as a Java



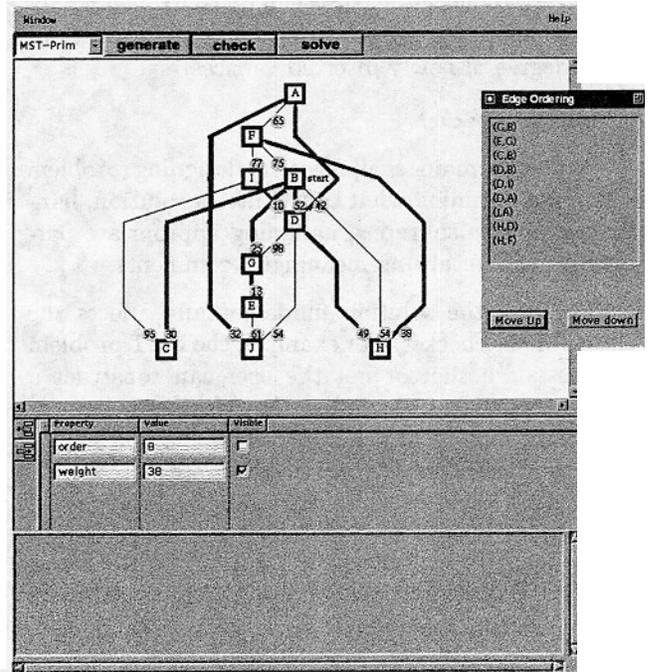
(a) random instance of MST-Prim



(b) user's solution



(c) automatically corrected solution, with incorrect edges highlighted



(d) system-generated solution

Figure 1: Example of user interaction with PILOT.

applet and the server side contains the problem generators, checkers, and solvers, currently also implemented in Java. The main motivation for choosing the client-server architecture was flexibility — the server is not constrained by the security restrictions placed on applets and is not limited to running Java programs, making it possible to take advantage of existing tools. The graph generator, for example, uses the Graph Drawing Server [9] component of GeomNet to compute a layout for the automatically generated graphs. The modularity of the GeomNet system also makes it easy to add new components — both interfaces and problem generators/checkers/solvers — to PILOT.

We now look at the graph generator and problem checker components of PILOT in more detail, focusing on minimum spanning tree problems as an example; the problem solvers are straightforward implementations of the appropriate problem solving algorithms and are not considered further.

### 3.1 Graph Generator

The graph generator uses a method similar to that of [11] to generate “realistic” graphs for experimental purposes. Graphs are built from a single vertex by repeatedly applying three operations — (1) insertion of a vertex and a random number of adjacent edges, (2) insertion of an edge between two existing vertices, and (3) splitting of an existing edge by replacing it with a new vertex and two new edges. Graph properties such as the ratio of edges to vertices can be controlled by adjusting probabilities assigned to each of the operations and the degree of newly inserted vertices.

### 3.2 Problem Checkers

There are four main challenges in designing problem checkers: determining what constitutes a solution, handling non-unique solutions, assigning appropriate partial credit, and returning meaningful comments.

The format of the solution fundamentally affects the structure of the checker. For example, the MST problem simply tests whether or not the user can construct a minimum spanning tree, and so the solution is a list of the edges belonging to the MST. The checker simply verifies whether or not the right edges were selected. In MST-Prim, the goal is to test the user’s knowledge of a specific algorithm and so more information is needed in the solution. In this case, the order in which the edges are added to the MST is sufficient to verify that the user executed the algorithm correctly, and the checker must check this order.

The last three problems are related. It is relatively easy to compute a solution and compare the user’s input to it, simply returning “correct” or “incorrect” (or “full credit”/“no credit”). However, this unfairly penalizes a

student who understands the concept but makes a small mistake, and is of limited use to a student who is trying to master a concept. More appropriate responses for MST problems, for example, would be something like “Edge (a,c) should be replaced by the lower-weight edge (a,b)” and a 1-point penalty for each incorrect edge. The solve-and-compare approach also runs into problems when the solution is not unique, since the user may have a correct solution but be marked wrong because the system generated a different one. Non-unique solutions can easily occur in MST problems when multiple edges have the same weight.

One approach is to verify properties of the user’s solution, to ensure that it is valid. This is the approach taken in the MST checker — for each edge in the MST, that edge should be the lowest-weight edge of any connecting the two vertex partitions created by the removal of the edge from the spanning tree. Each time an edge violates this property, it is marked incorrect and the appropriate replacement edge can be indicated to the user. Partial credit can be assigned according to the number of incorrect edges. (If the user’s input is not a spanning tree, cycles are broken by removing the highest-weight edge in the cycle and trees are joined by adding the lowest-weight edge between the trees. The checker then proceeds with the spanning tree produced, adding an additional penalty for non-tree input.)

This approach partially addresses the problem of meaningful comments and partial credit, but is not appropriate for problems where an early mistake can be compounded. For example, if the user chooses the wrong edge in the first step of Prim’s algorithm but otherwise executes the algorithm properly, the one mistake may cause several other edges to be selected incorrectly. It is unfair to penalize the user for every edge that is wrong since it was actually only one mistake, and the system’s comments may be similarly misleading. A checker can solve this problem by taking an incremental approach and stepping through the solution of the problem, taking into account the user’s choices as they happen. The MST-Prim checker considers the user’s edges in order, testing each edge to determine if it is valid as the next choice. An edge is valid if it connects a new vertex to the spanning-tree-in-progress and has the lowest weight of any edge connecting a new vertex to the tree. A penalty is assessed if the user’s edge is not valid, with a higher penalty if the edge does not connect to the tree. The internal data structures are then updated to include the new edge, and the checker continues with the next edge.

## 4 Future Work

The current PILOT system can be extended in many ways. Of particular use in a teaching tool would be to allow greater interactivity — as the user works through

the problem, the system can immediately provide feedback as to whether or not the user is doing the right thing. Also, if the user is unsure of what step to take next, the system can provide hints or outright statements about what to do.

Another issue is the generation of problems of approximately equal difficulty (and, related to this, the generation of appropriate special cases). For example, in Prim's algorithm the addition of an edge and vertex to the spanning tree may result in a new, lower-weight connection for an unconnected vertex and thus change the best choice for the next vertex/edge pair added to the tree. Problems with many instances of this case may be viewed as harder than problems without, since they require knowledge of particular cases in the algorithm. This is particularly relevant if PILOT is used in a testing situation, since it is undesirable for one student to get an easy case when another is faced with a much harder example. Dealing with this involves looking more carefully at the properties of the graphs produced by the graph generator.

Problem checkers can pose challenging problems of their own. The issues are the same as those mentioned in Section 3.2 — determining an appropriate format for the solution and handling partial credit and comments. Partial credit is one of the most “human” tasks of grading, and one that is very subjective, and so determining appropriate ways to handle it automatically is an important task. Implementing checkers to assign partial credit can be significantly harder than the corresponding problem solvers.

Finally, PILOT can be extended to handle additional problem types and algorithms. The mechanism for doing this is straightforward — many other graph problems, such as maximum flow, can be supported by the current interface so all that is required are additional checkers and solvers. Adding new problem types, such as sorting, requires more work to create a new interface in addition to generators/checkers/solvers. In both cases, however, the server remains the same so adding new components is only a matter of plugging in a new front- or back-end.

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